Software Design, Modelling and Analysis in UML

Lecture 6: Class Diagrams I

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Course Map



Last Lecture:

- Object Diagrams
 - partial vs. complete; for analysis; for documentation...

This Lecture:

- Educational Objectives: Capabilities for following tasks/questions.
 - What is a class diagram?
 - For what purposes are class diagrams useful?
 - Could you please map this class diagram to a signature?
 - Could you please map this signature to a class diagram?

• Content:

- Study UML syntax.
- Prepare (extend) definition of signature.
- Map class diagram to (extended) signature.
- Stereotypes.

UML Class Diagrams: Stocktaking

Recall: Signature vs. Class Diagram



That'd Be Too Simple





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A class

- has a set of stereotypes,
- has a name,
- belongs to a package,
- can be abstract,
- can be active,
- has a set of attributes,
- has a set of **operations**.

Each attribute has

- a visibility,
- a name, a type,
- a multiplicity, an order,
- an initial value, and
- a set of properties, such as readOnly, ordered, etc.

Wanted: places in the signature to represent the information from the picture.

$$\begin{array}{l} \langle\!\langle Stereotype_1, \ldots, Stereotype_n \rangle\!\rangle \\ & \mathsf{Package::C} \\ + r : \mathsf{C}_{0,1} = expr \\ s : \mathsf{D}_* \ \{\mathsf{ordered}\} \\ - v : Int = 27 \\ w : Float \ \{\mathsf{readOnly}\} \end{array}$$





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- an initial value expression expr₀ given as a word from a language for initial value expressions, e.g. OCL, or C++ in the Rhapsody tool,

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We use $S_{\mathscr{C}}$ to denote the set $\bigcup_{C \in \mathscr{C}} S_C$ of stereotypes in \mathscr{S} .

Conventions

- We write $\langle C, S_C, a, t \rangle$ if we want to refer to all aspects of C.
- If the new aspects are irrelevant (for a given context), we simply write C i.e. old definitions are still valid.
- We write $\langle v: T, \xi, expr_0, P_v \rangle$ if we want to refer to all aspects of v.
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• Note:

All definitions we have up to now **principally still apply** as they are stated in terms of, e.g., $C \in \mathscr{C}$ — which still has a meaning with the extended view.

For instance, system states and object diagrams will remain mostly unchanged.

• The other way round: most of the newly added aspects do not contribute to the constitution of system states or object diagrams.

Mapping UML Class Diagrams to Extended Signatures

From Class Boxes to Extended Signatures

n:

A class box n induces an (extended) signature class as follows:

$$\begin{array}{c} \langle \! \langle S_1, \dots, S_k \rangle \! \rangle \\ C \\ \xi_1 \ v_1 : T_1 = expr_0^1 \ \{P_{1,1}, \dots, P_{1,m_1}\} \\ \vdots \\ \xi_\ell \ v_\ell : T_\ell = expr_0^\ell \ \{P_{\ell,1}, \dots, P_{\ell,m_\ell}\} \end{array}$$

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$$\label{eq:C(n)} \begin{cases} \\ C(n) := \langle C, \{S_1, \dots, S_k\}, a(n), t(n) \rangle \end{cases}$$

 $V(n) := \{ \langle v_1 : T_1, \xi_1, expr_0^1, \{P_{1,1}, \dots, P_{1,m_1}\} \rangle, \dots, \langle v_\ell : T_\ell, \xi_\ell, expr_0^\ell, \{P_{\ell,1}, \dots, P_{\ell,m_\ell}\} \rangle \}$ $atr(n) := \{ C \mapsto \{v_1, \dots, v_\ell\} \}$

where

• "abstract" is determined by the font:

$$a(n) = \begin{cases} \textit{true} & \text{, if } n = \boxed{\textit{C}} \text{ or } n = \boxed{\textit{C}_{\{A\}}} \\ \textit{false} & \text{, otherwise} \end{cases}$$

• "active" is determined by the frame:

$$t(n) = \begin{cases} true & , \text{ if } n = \boxed{\mathsf{C}} \text{ or } n = \boxed{\mathsf{C}} \\ false & , \text{ otherwise} \end{cases}$$

Example



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Π	x:Int

It depends.

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The type, visibility, default, multiplicity, property string may be suppressed from being displayed, even if there are values in the model."

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- **Properties**: probably safe to assume \emptyset if not given at all.

Example Cont'd

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From Class Diagrams to Extended Signatures

- We view a **class diagram** \mathcal{CD} as a graph with nodes $\{n_1, \ldots, n_N\}$ (each "class rectangle" is a node).
 - $\mathscr{C}(\mathcal{CD}) := \{C(n_i) \mid 1 \le i \le N\}$
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- In a UML model, we can have finitely many class diagrams,

$$\mathscr{CD} = \{ \mathcal{CD}_1, \ldots, \mathcal{CD}_k \},\$$

which **induce** the following signature:

$$\mathscr{S}(\mathscr{CD}) = \left(\mathscr{T}, \bigcup_{i=1}^{k} \mathscr{C}(\mathcal{CD}_{i}), \bigcup_{i=1}^{k} V(\mathcal{CD}_{i}), \bigcup_{i=1}^{k} atr(\mathcal{CD}_{i})\right).$$

(Assuming \mathscr{T} given. In "reality" (i.e. in full UML), we can introduce types in class diagrams, the class diagram then contributes to \mathscr{T} . Example: enumeration types.)

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Simply forbid the case (ii) — easy syntactical check on diagram.

(2) An attribute v may appear in multiple classes with different type:



Two approaches:

• Require **unique** attribute names.

This requirement can easily be established (implicitly, behind the scenes) by viewing v as an abbreviation for

C :: v or D :: v

depending on the context. (C::v:Bool and D::v:Int are then unique.)

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• Subtle, formalist's approach: observe that

 $\langle v: Bool, \ldots \rangle$ and $\langle v: Int, \ldots \rangle$

are different things in V. We don't follow that path...

Class Diagram Semantics

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• What is the effect on $\Sigma^{\mathscr{D}}_{\mathscr{S}}$? Little.

For now, we only **remove** abstract class instances, i.e.

 $\sigma:\mathscr{D}(\mathscr{C})\nrightarrow (V\nrightarrow (\mathscr{D}(\mathscr{T})\cup \mathscr{D}(\mathscr{C}_*)))$

is now only called system state if and only if, for all $\langle C, S_C, 1, t \rangle \in \mathscr{C}$,

$$\operatorname{dom}(\sigma) \cap \mathscr{D}(C) = \emptyset.$$

With a = 0 as default "abstractness", the earlier definitions apply directly. (We'll revisit this when discussing inheritance.)

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- **Properties**: such as readOnly, ordered, composite (Deprecated in the standard.)
 - readOnly later treated similar to visibility.
 - ordered not considered in our UML fragment (\rightarrow sets vs. sequences).
 - composite cf. lecture on associations.

Stereotypes

Stereotypes as Labels or Tags

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- Oestereich (2006):

View stereotypes as (additional) "labelling" ("tags") or as "grouping".

- Useful for documentation and model-driven development, e.g. code-generation:
 - **Documentation**: e.g. layers of an architecture.

Sometimes, packages (cf. OMG (2011a,b)) are sufficient and "right".

• Model Driven Architecture (MDA): later.

Example: Stereotypes for Documentation



- Example: Timing Diagram Viewer Schumann et al. (2008)
- Architecture has four layers:
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Stereotype "=" layer "=" colour.



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- Use stereotypes to label classes with licensing information (e.g., LGPL vs. proprietary).
- Use stereotypes 'Server_A', 'Server_B' to indicate where objects should be stored.
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- etc. etc.

Necessary: a **common idea** of what each stereotype stands for. (To be defined / agreed on by the team, not the job of the UML consortium.)

References

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