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## Tutorials for Decision Procedures Exercise sheet 14

## Exercise 1: $\pi VC$ – proving total correctness

Use  $\pi VC$  to prove total correctness of the example program InsertionSort from the  $\pi VC$ -website (https://cs.stanford.edu/people/jasonaue/pivc/samples/). Choose *one* of the following settings to solve this exercise:

- Replace the postcondition by **true** and uncheck the flag "Generate Runtime Assertions" in the "Settings" menu. Add the loop invariants and the ranking function to show correctness of the loop invariants and termination.
- Take your solution from exercise 2 on sheet 13 and extend it with the annotations needed to prove termination. Make sure that partial correctness is still given, and if necessary, adjust the loop invariants.

## **Exercise 2:** Interpolation for $T_E$

Compute the Craig interpolant for each of the following  $T_E$ -formula pairs:

(a)

$$F: a = y \land x = f(a) \land z = w \land a \neq c$$
$$G: c = b \land b = x \land f(y) \neq z \land w = b$$

(b)

$$F: g(f(x)) = a \land f(g(x)) = a \land a \neq x$$
$$G: f(g(f(b))) = x \land f(b) = x$$

## Exercise 3: Interpolation for $T_{\mathbb{Q}}$

Compute the Craig interpolant for the following  $T_{\mathbb{Q}}$ -formula pair:

$$F: x \ge a \land a \ge -2y + 1 \land 2a + y \ge 1$$
$$G: x + y \le \frac{1}{2}$$