

Software Design, Modelling and Analysis in UML

Lecture 18: Live Sequence Charts II

2017-01-24

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Albert-Ludwigs-Universität Freiburg, Germany

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Content

- **Reflective Descriptions of Behaviour**

- Interactions
- A Brief History of Sequence Diagrams

- **Live Sequence Charts**

- Abstract Syntax, Well-Formedness
- Semantics

- **TBA Construction for LSC Body**

- Cuts, Firedsets
- Signal / Attribute Expressions
- Loop / Progress Conditions

- **Excursion: Büchi Automata**

- **Language of a Model**

- **Full LSCs**

- Existential and Universal
- Pre-Charts
- Forbidden Scenarios

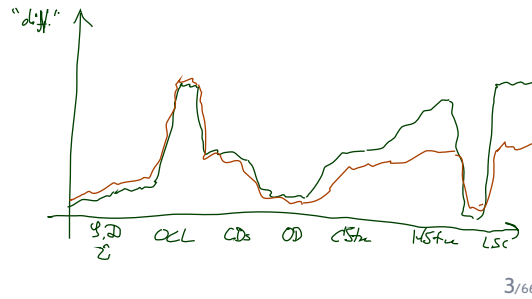
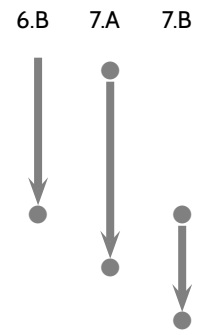
- **LSCs and Tests**

LSC	not so simple	can be concise
	<u>Sem</u>	<u>Model</u>
HStm	not so simple	may be small
CLStm	simple/short	can get large
<hr/>		
CLH	large	short
ASM	simple	may get large

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- Thu, 19. 1.: **Live Sequence Charts I**
Firstly: State-Machines Rest, Code Generation
- Tue, 24. 1.: **Live Sequence Charts II**
- Thu, 26. 1.: **Live Sequence Charts III**
- Tue, 31. 1.: **Tutorial 7**
- Thu, 2. 2.: **Model Based/Driven SW Engineering**
- **Mon, 6. 2.: Inheritance**
- Tue, 7. 2.: **Meta-Modelling** + Questions

February, 17th: **The Exam.**



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Constructive Behavioural Modelling in UML: Discussion

Pessimistic view: There are too many...

- For instance,
 - allow **absence of initial pseudo-states**
object may then “be” in enclosing state without being in any substate;
or assume one of the children states non-deterministically
 - (implicitly) **enforce determinism**, e.g.
by considering the order in which things have been added to the CASE tool's repository,
or some graphical order (left to right, top to bottom)
 - allow **true concurrency**
 - etc. etc.

Exercise: Search the standard for “semantical variation point”.

- Crane and Dingel (2007), e.g., provide an in-depth comparison of Statemate, UML, and Rhapsody state machines – the bottom line is:
 - **the intersection is not empty** (i.e. some diagrams mean the same to all three communities)
 - **none is the subset of another** (i.e. each pair of communities has diagrams meaning different things)

Optimistic view:

- tools exist with **complete and consistent** code generation.
- good modelling-guidelines can contribute to **avoiding misunderstandings**.

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Reflective Descriptions of Behaviour

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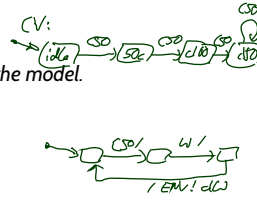
Constructive vs. Reflective Descriptions

Harel (1997) proposes to distinguish constructive and reflective descriptions:

- A constructive description tells us **how** things are computed:

"A language is **constructive** if it contributes to the dynamic semantics of the model.

That is, its constructs contain information needed in executing the model or in translating it into executable code."



- A reflective description tells us **what** shall (or shall not) be computed:

"Other languages are **reflective** or **assertive**,

and can be used by the system modeler to capture parts of the thinking that go into building the model - behavior included -, to derive and present views of the model, statically or during execution, or to set constraints on behavior in preparation for verification."



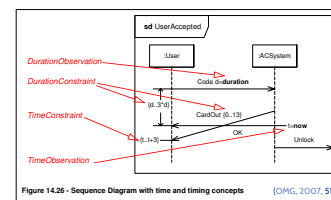
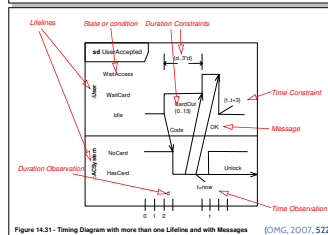
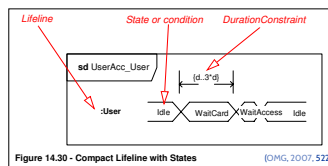
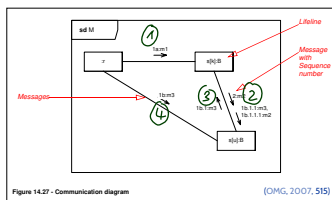
Note: No sharp boundaries! (Would be too easy.)

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Interactions as Reflective Description

- In UML, reflective (temporal) descriptions are subsumed by **interactions**.
A UML model $\mathcal{M} = (\mathcal{CD}, \mathcal{SM}, \mathcal{OD}, \mathcal{I})$ has a set of interactions \mathcal{I} .
- An interaction $\mathcal{I} \in \mathcal{I}$ can be (OMG claim: equivalently) **diagrammed** as
 - communication diagram** (formerly known as collaboration diagram),
 - timing diagram**, or
 - sequence diagram**.

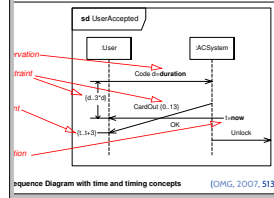
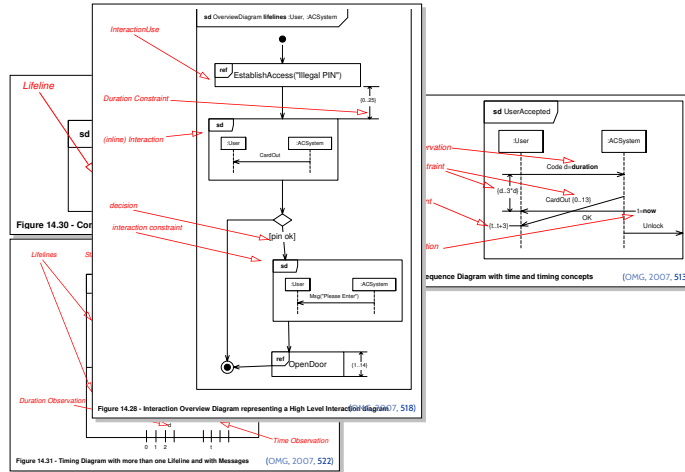
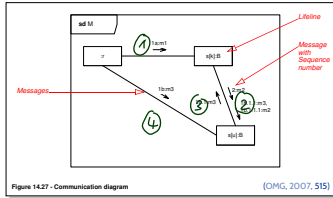


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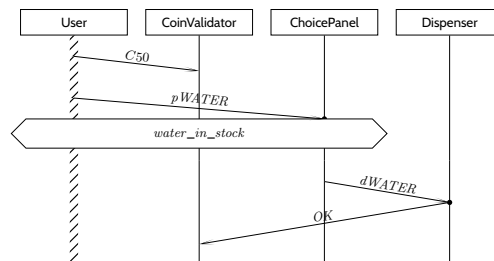
Why Sequence Diagrams?

Most Prominent: Sequence Diagrams – with **long history**:

- Message Sequence Charts**, standardized by the ITU in different versions, often accused to lack a formal semantics.
- Sequence Diagrams** of UML 1.x

Most severe **drawbacks** of these formalisms:

- unclear **interpretation**:
example scenario or invariant?
- unclear **activation**:
what triggers the requirement?
- unclear **progress** requirement:
must all messages be observed?
- conditions** merely comments
- no means to express **forbidden scenarios**

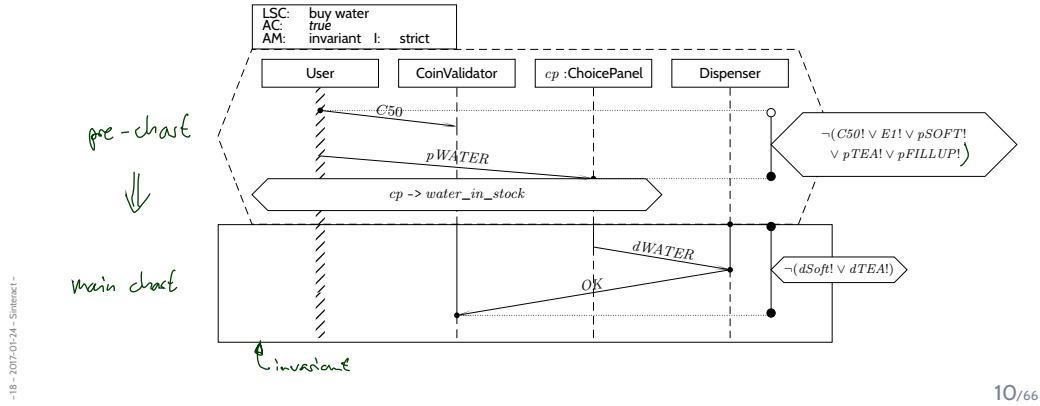


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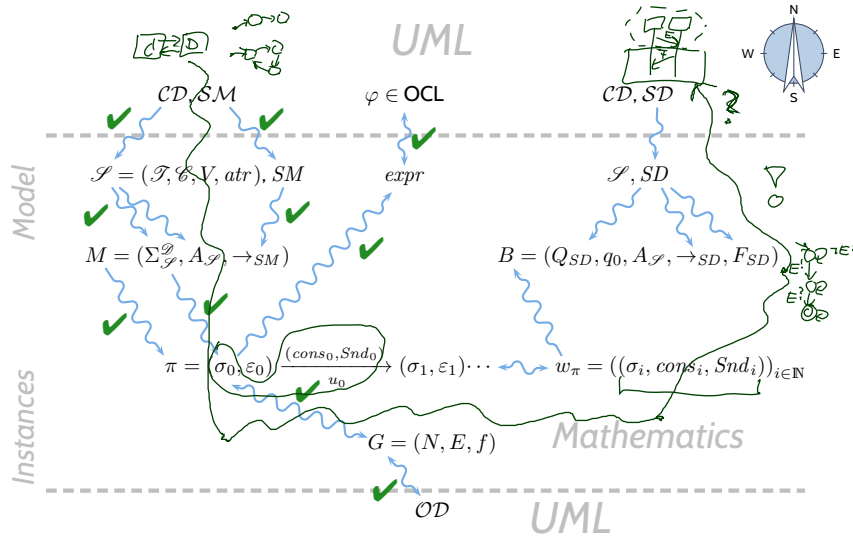
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Hence: Live Sequence Charts

- SDs of UML 2.x address some issues, yet the standard exhibits unclarities and even contradictions Harel and Maoz (2007); Störrle (2003)
- For the lecture, we consider Live Sequence Charts (LSCs) Damm and Harel (2001); Klose (2003); Harel and Marelly (2003), who have a common fragment with UML 2.x SDs Harel and Maoz (2007)
- Modelling guideline: stick to that fragment.



Course Map

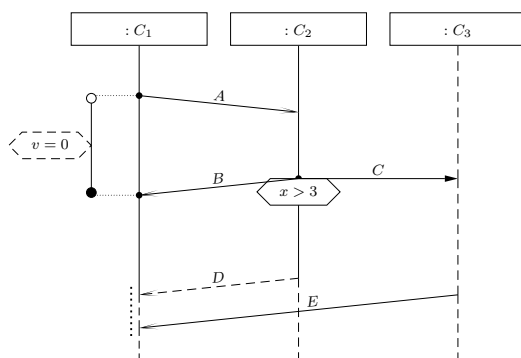


Live Sequence Charts — Syntax

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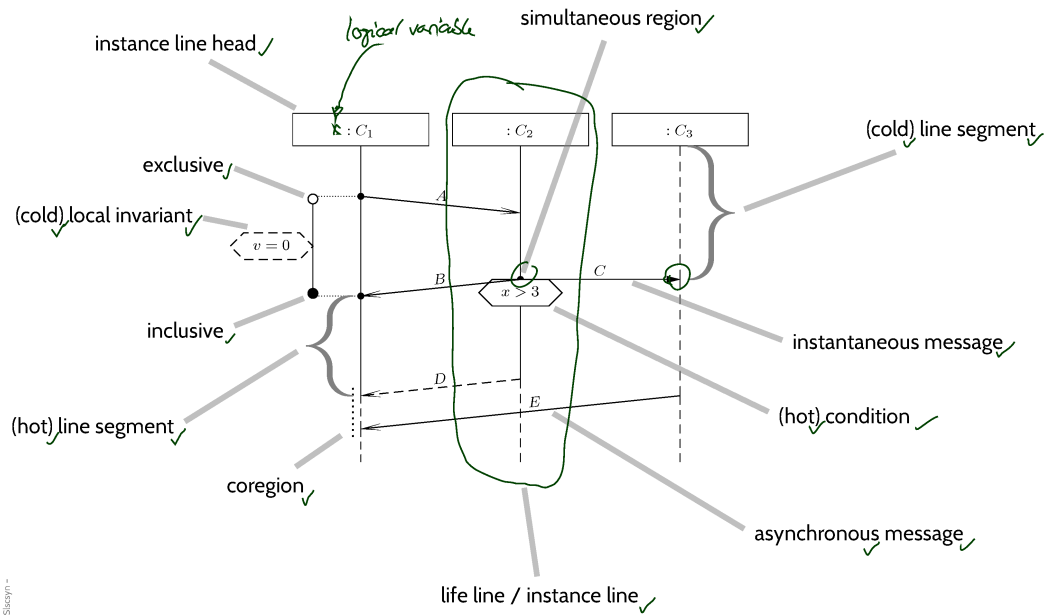
LSC Body Building Blocks



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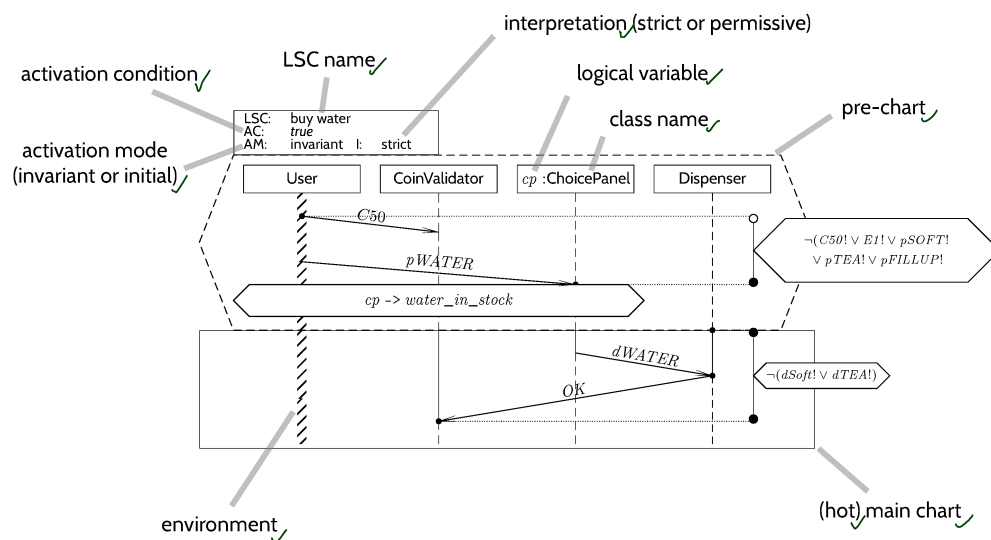
LSC Body Building Blocks



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Full LSC Building Blocks for Later



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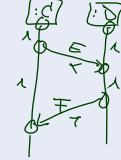
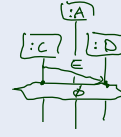
Definition. [LSC Body]

An **LSC body** over signature $\mathcal{S} = (\mathcal{T}, \mathcal{E}, V, \text{atr}, \mathcal{E})$ is a tuple

$$((L, \preceq, \sim), \mathcal{I}, \text{Msg}, \text{Cond}, \text{LocInv}, \Theta)$$

where

- L is a finite, non-empty of **locations** with
 - a **partial order** $\preceq \subseteq L \times L$,
 - a symmetric **simultaneity relation** $\sim \subseteq L \times L$ disjoint with \preceq , i.e. $\preceq \cap \sim = \emptyset$,
- $\mathcal{I} = \{I_1, \dots, I_n\}$ is a partitioning of L ; elements of \mathcal{I} are called **instance line**,
- $\text{Msg} \subseteq L \times \mathcal{E} \times L$ is a set of **messages** with $(l, E, l') \in \text{Msg}$ only if $(l, l') \in \prec \cup \sim$; message (l, E, l') is called **instantaneous** iff $l \sim l'$ and **asynchronous** otherwise,
- $\text{Cond} \subseteq (2^L \setminus \emptyset) \times \text{Expr}_{\mathcal{S}}$ is a set of **conditions** with $(L, \phi) \in \text{Cond}$ only if $l \sim l'$ for all $l \neq l' \in L$,
- $\text{LocInv} \subseteq L \times \{\circ, \bullet\} \times \text{Expr}_{\mathcal{S}} \times L \times \{\circ, \bullet\}$ is a set of **local invariants** with $(l, \iota, \phi, l', \iota') \in \text{LocInv}$ only if $l \prec l'$, \circ : exclusive, \bullet : inclusive,
- $\Theta : L \cup \text{Msg} \cup \text{Cond} \cup \text{LocInv} \rightarrow \{\text{hot}, \text{cold}\}$ assigns to each location and each element a **temperature**.

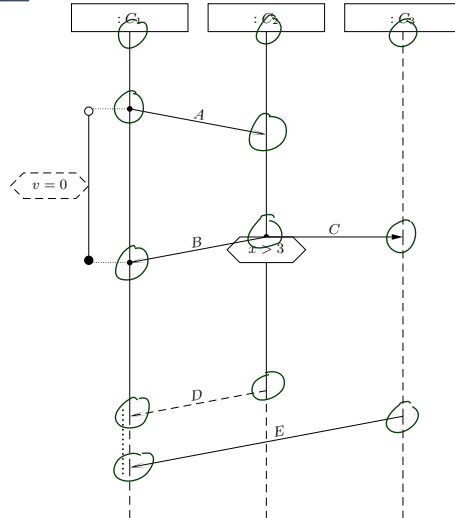


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From Concrete to Abstract Syntax

- locations L ,
- $\preceq \subseteq L \times L$, $\sim \subseteq L \times L$
- $\mathcal{I} = \{I_1, \dots, I_n\}$,
- $\text{Msg} \subseteq L \times \mathcal{E} \times L$,
- $\text{Cond} \subseteq (2^L \setminus \emptyset) \times \text{Expr}_{\mathcal{S}}$
- $\text{LocInv} \subseteq L \times \{\circ, \bullet\} \times \text{Expr}_{\mathcal{S}} \times L \times \{\circ, \bullet\}$,
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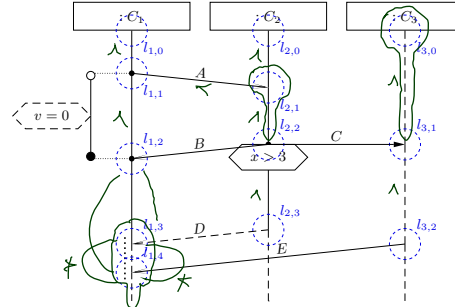


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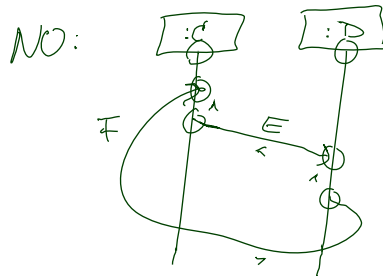
$$\begin{aligned}
 L &= \{l_{1,0}, \dots, l_{1,4}, l_{2,0}, \dots, l_{2,3}, l_{3,0}, \dots, l_{3,2}\} \\
 \preceq &= \{ (l_{1,0}, l_{1,1}), (l_{1,1}, l_{1,2}), (l_{1,2}, l_{1,3}), (l_{1,3}, l_{1,4}), \dots, (l_{1,4}, l_{2,0}), (l_{2,0}, l_{2,1}), \dots \} \\
 \leq &= \preceq^* \\
 \sim &= \{ (l_{2,1}, l_{3,1}) \} \\
 \text{Msg} &= \{ (l_{1,1}, A, l_{2,1}), \dots \} \\
 \text{Cond} &= \{ (\{l_{2,2}\}, x > 3) \} \\
 \text{LocInv} &= \{ (l_{1,1}, \circ, v=0, l_{1,2}, \bullet) \} \\
 \Theta &= \{ M \mapsto \text{hot}, C \mapsto \text{hot}, I \mapsto \text{cold}, l_{3,0} \mapsto \text{cold}, l_{2,1} \mapsto \text{hot}, \dots \}
 \end{aligned}$$

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From Concrete to Abstract Syntax

- locations L ,
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Bondedness/no floating conditions: (could be relaxed a little if we wanted to)

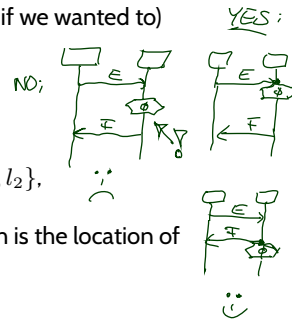
- For each location $l \in L$, **if** l is the location of

- a **condition**, i.e. $\exists (L, \phi) \in \text{Cond} : l \in L$, or
- a **local invariant**, i.e. $\exists (l_1, \iota_1, \phi, l_2, \iota_2) \in \text{LocInv} : l \in \{l_1, l_2\}$,

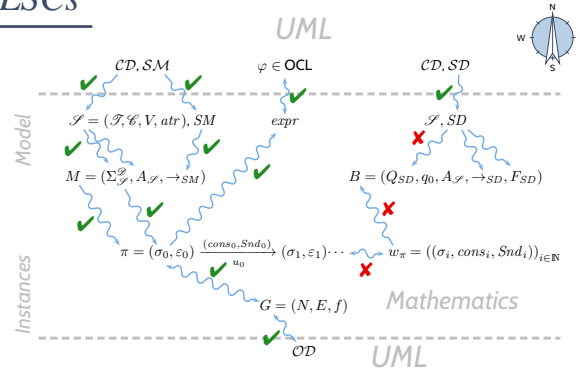
then there is a location l' **simultaneous** to l , i.e. $l \sim l'$, which is the location of

- an **instance head**, i.e. l' is minimal wrt. \preceq , or
- a **message**, i.e.

$$\exists (l_1, E, l_2) \in \text{Msg} : l \in \{l_1, l_2\}.$$



Note: if messages in a chart are **cyclic**,
then there doesn't exist a partial order
(so such diagrams **don't even have** an abstract syntax).



Plan:

- (i) Given an LSC \mathcal{L} with body

$$((L, \preceq, \sim), \mathcal{I}, \text{Msg}, \text{Cond}, \text{LocInv}, \Theta),$$
 - (ii) construct a TBA $\mathcal{B}_{\mathcal{L}}$, and
 - (iii) define language $\mathcal{L}(\mathcal{L})$ of \mathcal{L} **in terms of** $\mathcal{L}(\mathcal{B}_{\mathcal{L}})$,

in particular taking activation condition and activation mode into account.
 - (iv) define language $\mathcal{L}(\mathcal{M})$ of a UML model.
- Then $\mathcal{M} \models \mathcal{L}$ (**universal**) if and only if $\mathcal{L}(\mathcal{M}) \subseteq \mathcal{L}(\mathcal{L})$.
 And $\mathcal{M} \models \mathcal{L}$ (**existential**) if and only if $\mathcal{L}(\mathcal{M}) \cap \mathcal{L}(\mathcal{L}) \neq \emptyset$.

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Live Sequence Charts — TBA Construction

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Definition.

Let $((L, \preceq, \sim), \mathcal{I}, \text{Msg}, \text{Cond}, \text{LocInv}, \Theta)$ be an LSC body.

A non-empty set $\emptyset \neq C \subseteq L$ is called a **cut** of the LSC body iff

- it is **downward closed**, i.e. $\forall l, l' \bullet l' \in C \wedge l \preceq l' \implies l \in C$,
- it is **closed** under **simultaneity**, i.e.

$$\forall l, l' \bullet l' \in C \wedge l \sim l' \implies l \in C, \text{ and}$$

- it comprises at least **one location per instance line**, i.e.

$$\forall i \in I \exists l \in C \bullet i_l = i.$$

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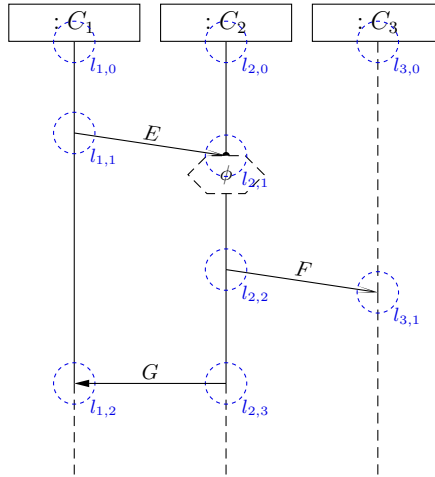
The **temperature function** is extended to cuts as follows:

$$\Theta(C) = \begin{cases} \text{hot} & , \text{ if } \exists l \in C \bullet (\nexists l' \in C \bullet l \prec l') \wedge \Theta(l) = \text{hot} \\ \text{cold} & , \text{ otherwise} \end{cases}$$

that is, C is **hot** if and only if at least one of its maximal elements is hot.

Cut Examples

$\emptyset \neq C \subseteq L$ – downward closed – simultaneity closed – at least one loc. per instance line

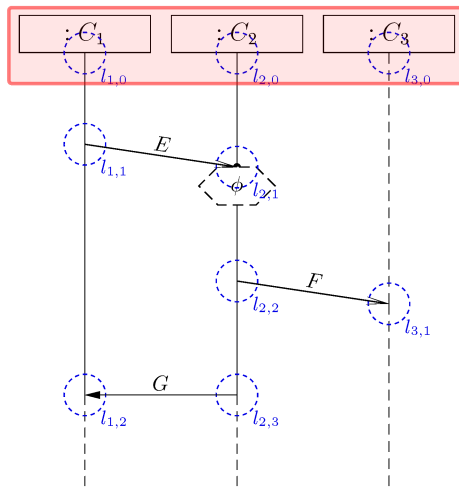


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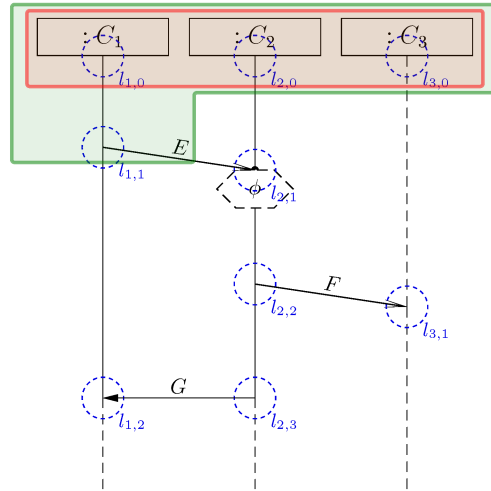


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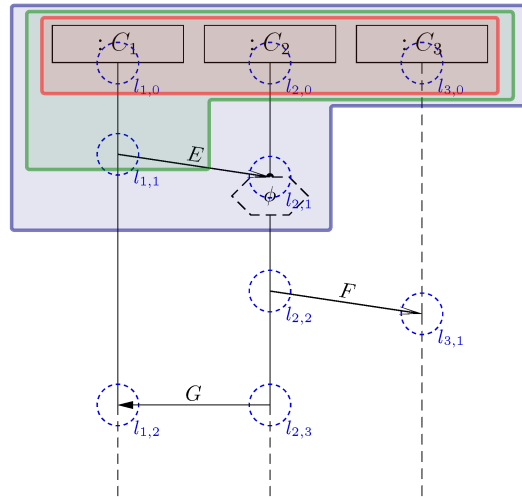


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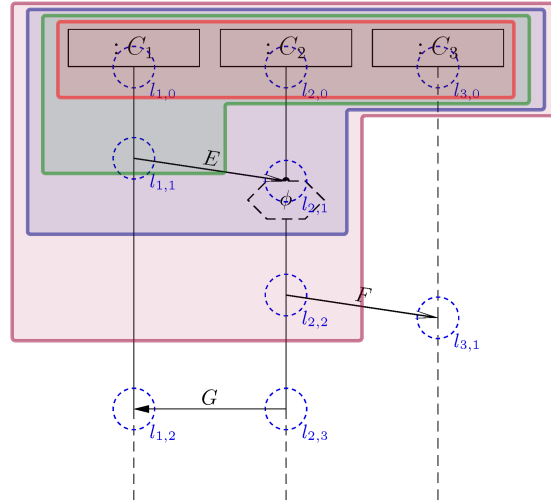


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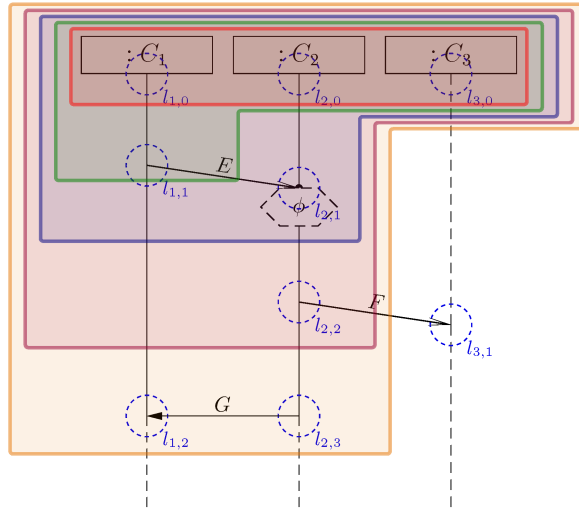


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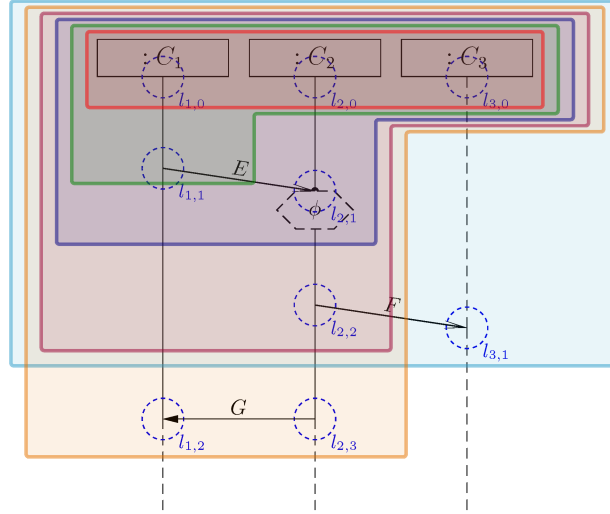


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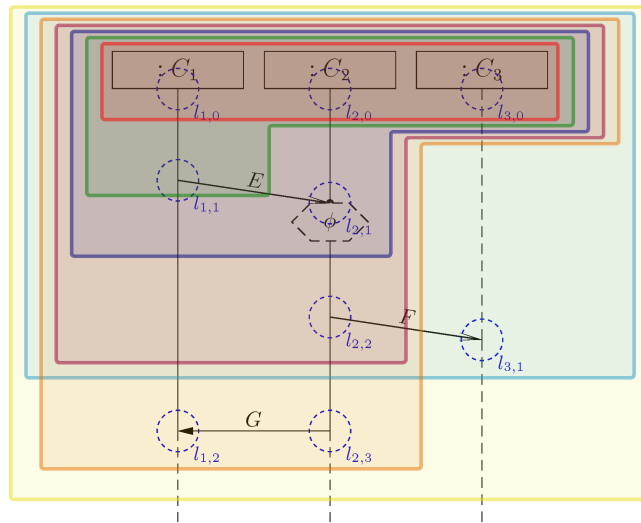


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A Successor Relation on Cuts

The partial order “ \preceq ” and the simultaneity relation “ \sim ” of locations induce a **direct successor relation** on cuts of an LSC body as follows:

Definition.

Let $C \subseteq L$ be a cut of LSC body $((L, \preceq, \sim), \mathcal{I}, \text{Msg}, \text{Cond}, \text{LocInv}, \Theta)$.

A set $\emptyset \neq F \subseteq L$ of locations is called **fired-set** F of cut C if and only if

- $C \cap F = \emptyset$ and $C \cup F$ is a cut, i.e. F is closed under simultaneity,
- all locations in F are **direct \prec -successors** of the front of C , i.e.

$$\forall l \in F \exists l' \in C \bullet l' \prec l \wedge (\nexists l'' \in C \bullet l' \prec l'' \prec l),$$
- locations in F , that lie on the same instance line, are **pairwise unordered**, i.e.

$$\forall l \neq l' \in F \bullet (\exists I \in \mathcal{I} \bullet \{l, l'\} \subseteq I) \implies l \not\prec l' \wedge l' \not\prec l,$$
- for each asynchronous (!) message reception in F ,
the corresponding **sending is already in** C ,

$$\forall (l, E, l') \in \text{Msg} \bullet l' \in F \implies l \in C.$$

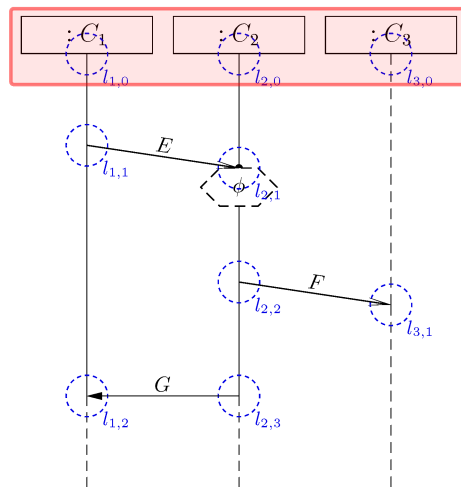
The cut $C' = C \cup F$ is called **direct successor of C via F** , denoted by $C \rightsquigarrow_F C'$.

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Successor Cut Example

$C \cap F = \emptyset - C \cup F$ is a cut – only direct \prec -successors – same instance line on front pairwise unordered – sending of asynchronous reception already in

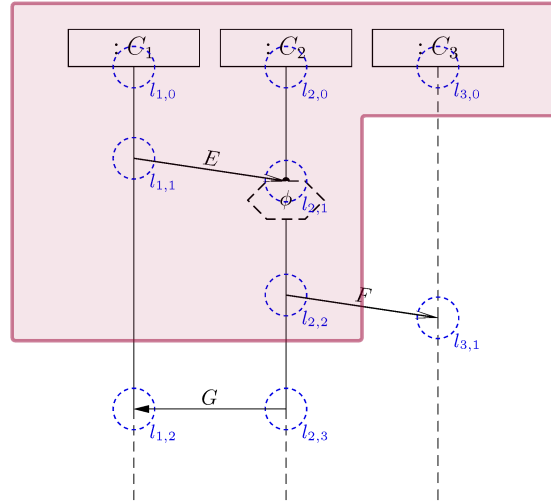


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Successor Cut Example

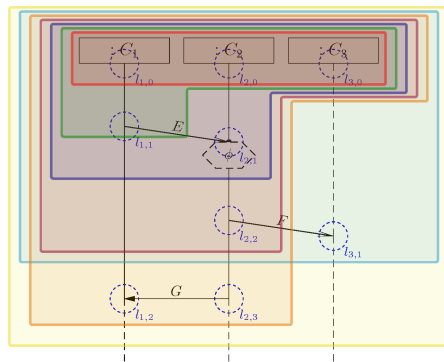
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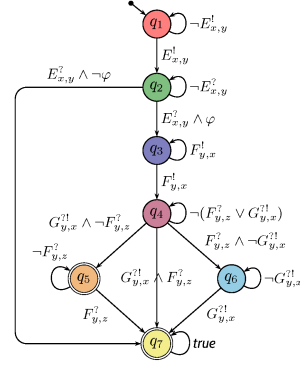
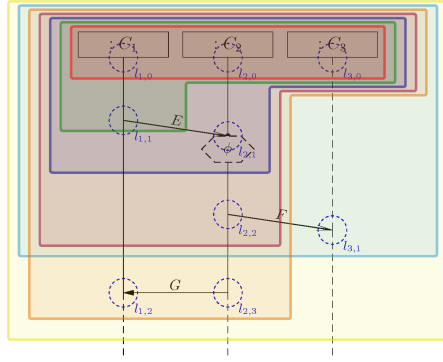
Language of LSC Body: Example



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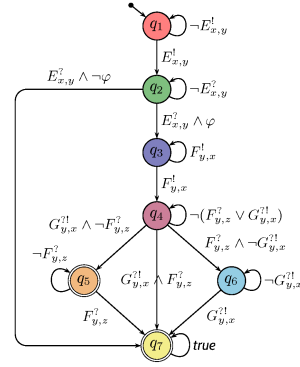
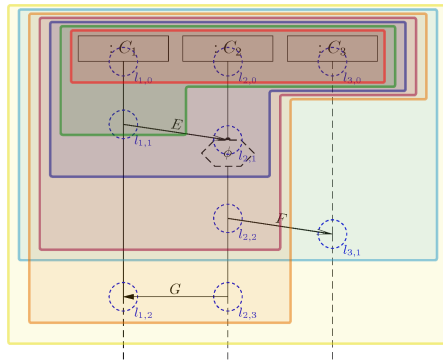
Language of LSC Body: Example



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Language of LSC Body: Example



The TBA $\mathcal{B}_{\mathcal{L}}$ of LSC \mathcal{L} over Φ and \mathcal{E} is $(Expr_{\mathcal{B}}(X), X, Q, q_{ini}, \rightarrow, Q_F)$ with

- Q is the set of cuts of \mathcal{L} , q_{ini} is the instance heads cut,
- $Expr_{\mathcal{B}}(X) = Expr_{\mathcal{S}}(\mathcal{E}, X)$ (for considered signature \mathcal{S}),
- \rightarrow consists of loops, progress transitions (by \rightsquigarrow_F), and legal exits (cold cond./local inv.),
- $Q_F = \{C \in Q \mid \Theta(C) = \text{cold} \vee C = L\}$ is the set of cold cuts and the maximal cut.

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Signal and Attribute Expressions

- Let $\mathcal{S} = (\mathcal{I}, \mathcal{E}, V, \text{atr}, \mathcal{E})$ be a signature and X a set of logical variables,
- The signal and attribute expressions $\text{Expr}_{\mathcal{S}}(\mathcal{E}, X)$ are defined by the grammar:

$$\psi ::= \text{true} \mid \psi \mid E_{x,y}^! \mid E_{x,y}^? \mid \neg\psi \mid \psi_1 \vee \psi_2,$$

where $\text{expr} : \text{Bool} \in \text{Expr}_{\mathcal{S}}, E \in \mathcal{E}, x, y \in X$ (or keyword *env*).

- We use

$$\mathcal{E}_{!?}(X) := \{E_{x,y}^!, E_{x,y}^? \mid E \in \mathcal{E}, x, y \in X\}$$

to denote the set of **event expressions** over \mathcal{E} and X .

TBA Construction Principle

Recall: The TBA $\mathcal{B}(\mathcal{L})$ of LSC \mathcal{L} is $(\text{Expr}_{\mathcal{B}}(X), X, Q, q_{ini}, \rightarrow, Q_F)$ with

- Q is the **set of cuts** of \mathcal{L} , q_{ini} is the **instance heads cut**,
- $\text{Expr}_{\mathcal{B}} = \Phi \dot{\cup} \mathcal{E}_{!?}(X)$,
- \rightarrow consists of **loops**, **progress transitions** (from \rightsquigarrow_F), and **legal exits** (cold cond./local inv.),
- $F = \{C \in Q \mid \Theta(C) = \text{cold} \vee C = L\}$ is the set of cold cuts.

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So in the following, we “only” need to construct the transitions’ labels:

$$\rightarrow = \{(q, \quad, q) \mid q \in Q\} \cup \{(q, \quad, q') \mid q \rightsquigarrow_F q'\} \cup \{(q, \quad, L) \mid q \in Q\}$$

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So in the following, we “only” need to construct the transitions’ labels:

$$\rightarrow = \{(q, \psi_{loop}(q), q) \mid q \in Q\} \cup \{(q, \psi_{prog}(q, q'), q') \mid q \rightsquigarrow_F q'\} \cup \{(q, \psi_{exit}(q), L) \mid q \in Q\}$$

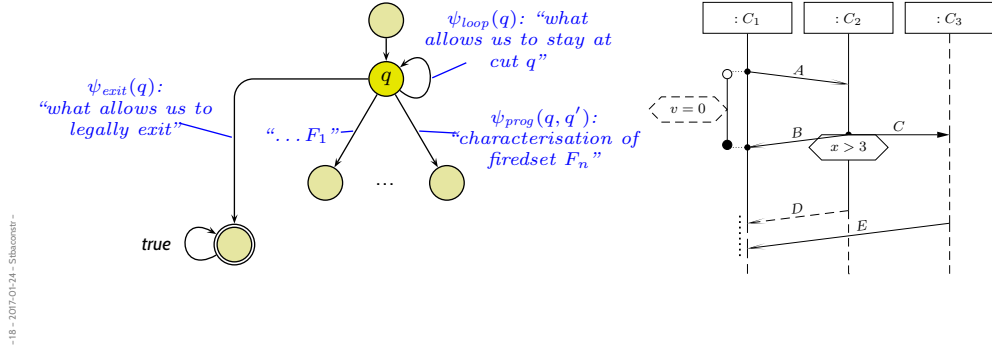
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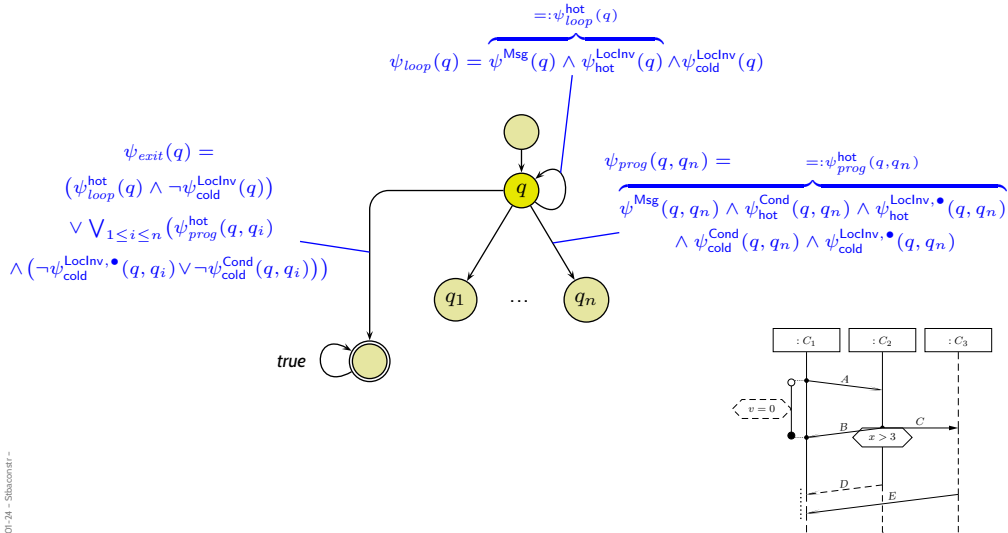


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TBA Construction Principle

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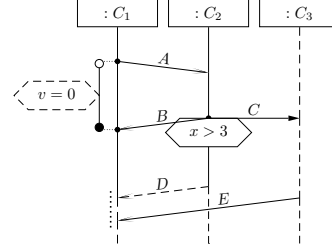


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Loop Condition

$$\psi_{loop}(q) = \psi^{Msg}(q) \wedge \psi_{hot}^{LocInv}(q) \wedge \psi_{cold}^{LocInv}(q)$$

- $\psi^{Msg}(q) = \neg \bigvee_{1 \leq i \leq n} \psi^{Msg}(q, q_i) \wedge \underbrace{\left(strict \implies \bigwedge_{\psi \in Msg(L)} \neg \psi \right)}_{=:\psi_{strict}(q)}$
- $\psi_{\theta}^{LocInv}(q) = \bigwedge_{\ell=(l, \iota, \phi, l', \iota') \in LocInv, \Theta(\ell)=\theta, \ell \text{ active at } q} \phi$
 A location l is called **front location** of cut C if and only if $\nexists l' \in L \bullet l \prec l'$.
 Local invariant $(l_0, \iota_0, \phi, l_1, \iota_1)$ is **active** at cut (!) q
 if and only if $l_0 \preceq l \prec l_1$ for some front location l of cut q or $l_1 \in q \wedge \iota_1 = \bullet$.
- $Msg(F) = \{E_{x_l, x_{l'}}^! \mid (l, E, l') \in Msg, l \in F\} \cup \{E_{x_l, x_{l'}}^? \mid (l, E, l') \in Msg, l' \in F\}$
- $x_l \in X$ is the logical variable associated with the instance line I which includes l , i.e. $l \in I$.
- $Msg(F_1, \dots, F_n) = \bigcup_{1 \leq i \leq n} Msg(F_i)$

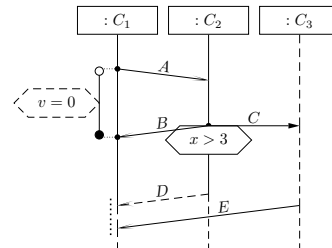


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Progress Condition

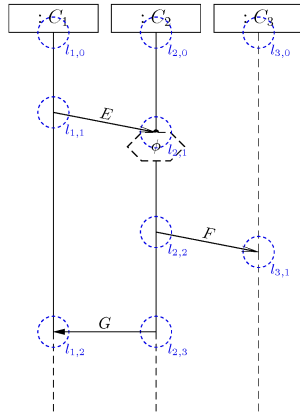
$$\psi_{prog}^{hot}(q, q_i) = \psi^{Msg}(q, q_n) \wedge \psi_{hot}^{Cond}(q, q_n) \wedge \psi_{hot}^{LocInv, \bullet}(q_n)$$

- $\psi^{Msg}(q, q_i) = \bigwedge_{\psi \in Msg(q_i \setminus q)} \psi \wedge \bigwedge_{j \neq i} \bigwedge_{\psi \in Msg(q_j \setminus q) \setminus Msg(q_i \setminus q)} \neg \psi$
 $\wedge \underbrace{\left(strict \implies \bigwedge_{\psi \in Msg(L) \setminus Msg(F_i)} \neg \psi \right)}_{=:\psi_{strict}(q, q_i)}$
- $\psi_{\theta}^{Cond}(q, q_i) = \bigwedge_{\gamma=(L, \phi) \in Cond, \Theta(\gamma)=\theta, L \cap (q_i \setminus q) \neq \emptyset} \phi$
- $\psi_{\theta}^{LocInv, \bullet}(q, q_i) = \bigwedge_{\lambda=(l, \iota, \phi, l', \iota') \in LocInv, \Theta(\lambda)=\theta, \lambda \bullet\text{-active at } q_i} \phi$
 Local invariant $(l_0, \iota_0, \phi, l_1, \iota_1)$ is **•-active** at q if and only if
 - $l_0 \prec l \prec l_1$. or
 - $l = l_0 \wedge \iota_0 = \bullet$, or
 - $l = l_1 \wedge \iota_1 = \bullet$
 for some front location l of cut (!) q .

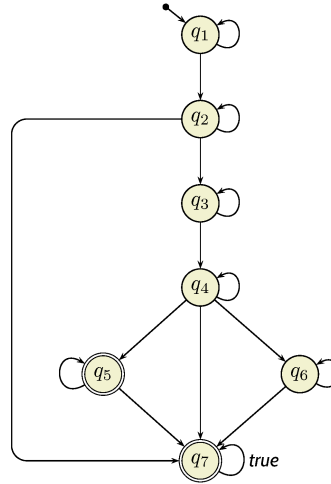


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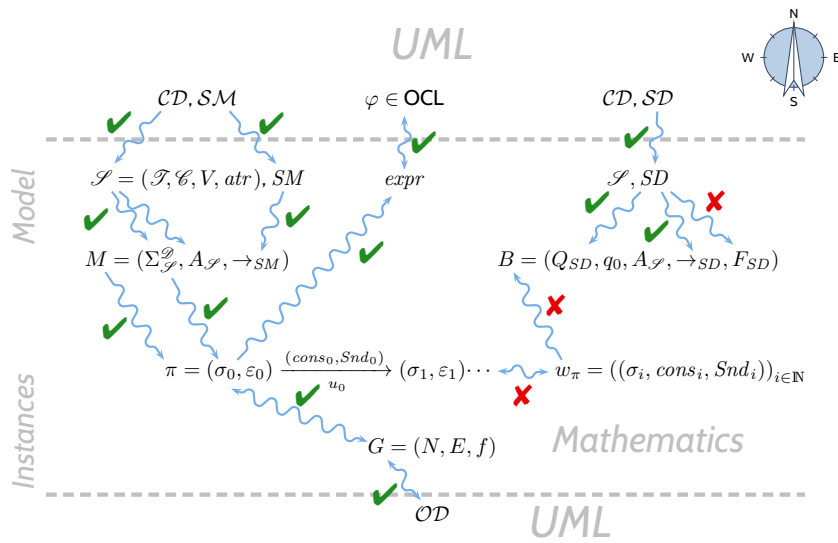
Example



Using logical variables x, y, z
for the instances lines
(from left to right).

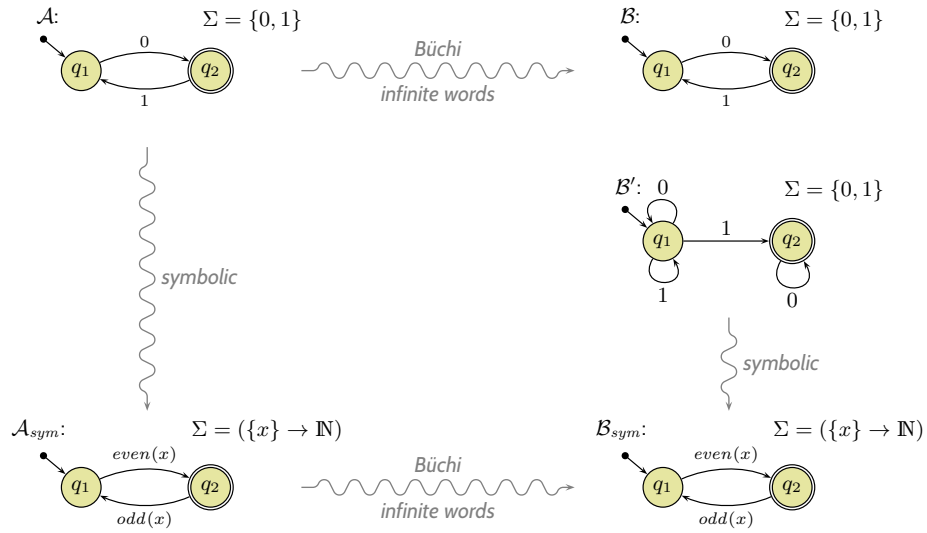


Course Map



- Interactions can be **reflective** descriptions of behaviour, i.e.
 - describe **what** behaviour is (un)desired, without (yet) defining **how** to realise it.
- One visual formalism for interactions: **Live Sequence Charts**
 - locations in diagram **induce a partial order**,
 - instantaneous and asynchronous messages,
 - conditions and local invariants
- The **meaning** of an LSC is defined using TBAs.
 - **Cuts** become states of the automaton.
 - Locations induce a **partial order on cuts**.
 - Automaton-transitions and annotations correspond to a **successor relation** on cuts.
 - Annotations use **signal / attribute expressions**.
- **Later:**
 - TBA have **Büchi acceptance** (of infinite words (of a model)).
 - **Full LSC semantics**.
 - **Pre-Charts**.

Excursion: Büchi Automata



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Symbolic Büchi Automata

Definition. A **Symbolic Büchi Automaton** (TBA) is a tuple

$$\mathcal{B} = (Expr_{\mathcal{B}}(X), X, Q, q_{ini}, \rightarrow, Q_F)$$

where

- X is a set of logical variables,
- $Expr_{\mathcal{B}}(X)$ is a set of Boolean expressions over X ,
- Q is a finite set of **states**,
- $q_{ini} \in Q$ is the initial state,
- $\rightarrow \subseteq Q \times Expr_{\mathcal{B}}(X) \times Q$ is the **transition relation**. Transitions (q, ψ, q') from q to q' are labelled with an expression $\psi \in Expr_{\mathcal{B}}(X)$.
- $Q_F \subseteq Q$ is the set of **fair** (or accepting) states.

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Definition. Let X be a set of logical variables and let $Expr_{\mathcal{B}}(X)$ be a set of Boolean expressions over X .

A set $(\Sigma, \cdot \models \cdot)$ is called an **alphabet** for $Expr_{\mathcal{B}}(X)$ if and only if

- for each $\sigma \in \Sigma$,
- for each expression $expr \in Expr_{\mathcal{B}}$, and
- for each valuation $\beta : X \rightarrow \mathcal{D}(X)$ of logical variables,

either $\sigma \models_{\beta} expr$ **or** $\sigma \not\models_{\beta} expr$.

(σ **satisfies** (or does not satisfy) $expr$ under valuation β)

An **infinite sequence**

$$w = (\sigma_i)_{i \in \mathbb{N}_0} \in \Sigma^{\omega}$$

over $(\Sigma, \cdot \models \cdot)$ is called **word** (for $Expr_{\mathcal{B}}(X)$).

Run of TBA over Word

Definition. Let $\mathcal{B} = (Expr_{\mathcal{B}}(X), X, Q, q_{ini}, \rightarrow, Q_F)$ be a TBA and

$$w = \sigma_1, \sigma_2, \sigma_3, \dots$$

a word for $Expr_{\mathcal{B}}(X)$. An infinite sequence

$$\varrho = q_0, q_1, q_2, \dots \in Q^{\omega}$$

is called **run of \mathcal{B} over w** under valuation $\beta : X \rightarrow \mathcal{D}(X)$ if and only if

- $q_0 = q_{ini}$,
- for each $i \in \mathbb{N}_0$ there is a transition

$$(q_i, \psi_i, q_{i+1}) \in \rightarrow$$

such that $\sigma_i \models_{\beta} \psi_i$.

Run of TBA over Word

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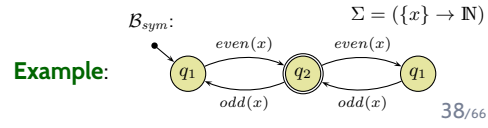
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such that $\sigma_i \models_{\beta} \psi_i$.



The Language of a TBA

Definition.

We say TBA $\mathcal{B} = (\text{Expr}_{\mathcal{B}}(X), X, Q, q_{ini}, \rightarrow, Q_F)$ **accepts** the word

$$w = (\sigma_i)_{i \in \mathbb{N}_0} \in (\text{Expr}_{\mathcal{B}} \rightarrow \mathbb{B})^\omega$$

if and only if \mathcal{B} **has** a run

$$\varrho = (q_i)_{i \in \mathbb{N}_0}$$

over w such that fair (or accepting) states are **visited infinitely often** by ϱ , i.e., such that

$$\forall i \in \mathbb{N}_0 \exists j > i : q_j \in Q_F.$$

We call the set $\mathcal{L}(\mathcal{B}) \subseteq (\text{Expr}_{\mathcal{B}} \rightarrow \mathbb{B})^\omega$ of words that are accepted by \mathcal{B} the **language of \mathcal{B}** .

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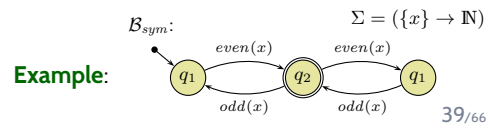
if and only if \mathcal{B} **has** a run

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Language of UML Model

The Language of a Model

Recall: A UML model $\mathcal{M} = (\mathcal{C}\mathcal{D}, \mathcal{SM}, \mathcal{O}\mathcal{D})$ and a structure \mathcal{D} denote a set $\llbracket \mathcal{M} \rrbracket$ of (initial and consecutive) **computations** of the form

$$(\sigma_0, \varepsilon_0) \xrightarrow{a_0} (\sigma_1, \varepsilon_1) \xrightarrow{a_1} (\sigma_2, \varepsilon_2) \xrightarrow{a_2} \dots \text{ where}$$

$$a_i = (\text{cons}_i, \text{Snd}_i, u_i) \in \underbrace{2^{\mathcal{D}(\mathcal{E})} \times 2^{(\mathcal{D}(\mathcal{E}) \dot{\cup} \{*,+\}) \times \mathcal{D}(\mathcal{C})}}_{=: \tilde{A}} \times \mathcal{D}(\mathcal{C}).$$

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For the connection between models and interactions, we **disregard** the configuration of **the ether**, and define as follows:

Definition. Let $\mathcal{M} = (\mathcal{C}\mathcal{D}, \mathcal{SM}, \mathcal{O}\mathcal{D})$ be a UML model and \mathcal{D} a structure. Then

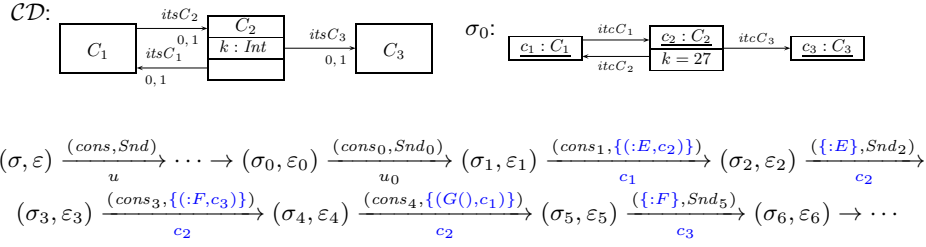
$$\mathcal{L}(\mathcal{M}) := \{(\sigma_i, u_i, \text{cons}_i, \text{Snd}_i)_{i \in \mathbb{N}_0} \in (\Sigma_{\mathcal{D}}^{\mathcal{D}} \times \tilde{A})^\omega \mid$$

$$\exists (\varepsilon_i)_{i \in \mathbb{N}_0} : (\sigma_0, \varepsilon_0) \xrightarrow[u_0]{(\text{cons}_0, \text{Snd}_0)} (\sigma_1, \varepsilon_1) \cdots \in \llbracket \mathcal{M} \rrbracket\}$$

is the **language** of \mathcal{M} .

Example: Language of a Model

$$\mathcal{L}(\mathcal{M}) := \{(\sigma_i, u_i, \text{cons}_i, \text{Snd}_i)_{i \in \mathbb{N}_0} \mid \exists (\varepsilon_i)_{i \in \mathbb{N}_0} : (\sigma_0, \varepsilon_0) \xrightarrow[u_0]{(\text{cons}_0, \text{Snd}_0)} (\sigma_1, \varepsilon_1) \cdots \in \llbracket \mathcal{M} \rrbracket\}$$



Words over Signature

Definition. Let $\mathcal{S} = (\mathcal{I}, \mathcal{C}, V, \text{atr}, \mathcal{E})$ be a signature and \mathcal{D} a structure of \mathcal{S} .

A **word** over \mathcal{S} and \mathcal{D} is an infinite sequence

$$(\sigma_i, u_i, \text{cons}_i, \text{Snd}_i)_{i \in \mathbb{N}_0} \in \Sigma_{\mathcal{S}}^{\mathcal{D}} \times \mathcal{D}(\mathcal{C}) \times 2^{\mathcal{D}(\mathcal{E})} \times 2^{(\mathcal{D}(\mathcal{E}) \cup \{*, +\}) \times \mathcal{D}(\mathcal{C})}$$

- The language $\mathcal{L}(\mathcal{M})$ of a UML model $\mathcal{M} = (\mathcal{CD}, \mathcal{SM}, \mathcal{OD})$ is a word over the signature $\mathcal{S}(\mathcal{CD})$ induced by \mathcal{CD} and \mathcal{D} , given structure \mathcal{D} .

Satisfaction of Signal and Attribute Expressions

- Let $(\sigma, u, cons, Snd) \in \Sigma_{\mathcal{D}} \times \tilde{A}$ be a tuple consisting of **system state**, **object identity**, **consume set**, and **send set**.
- Let $\beta : X \rightarrow \mathcal{D}(\mathcal{C})$ be a valuation of the logical variables.

Then

- $(\sigma, u, cons, Snd) \models_{\beta} \text{true}$
- $(\sigma, u, cons, Snd) \models_{\beta} \psi$ if and only if $I[\![\psi]\!](\sigma, \beta) = 1$
- $(\sigma, u, cons, Snd) \models_{\beta} \neg\psi$ if and only if $(\sigma, cons, Snd) \not\models_{\beta} \psi$
- $(\sigma, u, cons, Snd) \models_{\beta} \psi_1 \vee \psi_2$ if and only if $(\sigma, u, cons, Snd) \models_{\beta} \psi_1$ or $(\sigma, u, cons, Snd) \models_{\beta} \psi_2$
- $(\sigma, u, cons, Snd) \models_{\beta} E_{x,y}^1$ if and only if $\beta(x) = u \wedge \exists e \in \mathcal{D}(E) \bullet (e, \beta(y)) \in Snd$
- $(\sigma, u, cons, Snd) \models_{\beta} E_{x,y}^2$ if and only if $\beta(y) = u \wedge cons \subset \mathcal{D}(E)$

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Satisfaction of Signal and Attribute Expressions

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- Let $\beta : X \rightarrow \mathcal{D}(\mathcal{C})$ be a valuation of the logical variables.

Then

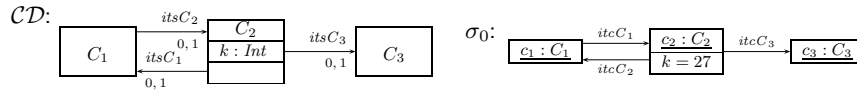
- $(\sigma, u, cons, Snd) \models_{\beta} \text{true}$
- $(\sigma, u, cons, Snd) \models_{\beta} \psi$ if and only if $I[\![\psi]\!](\sigma, \beta) = 1$
- $(\sigma, u, cons, Snd) \models_{\beta} \neg\psi$ if and only if $(\sigma, cons, Snd) \not\models_{\beta} \psi$
- $(\sigma, u, cons, Snd) \models_{\beta} \psi_1 \vee \psi_2$ if and only if $(\sigma, u, cons, Snd) \models_{\beta} \psi_1$ or $(\sigma, u, cons, Snd) \models_{\beta} \psi_2$
- $(\sigma, u, cons, Snd) \models_{\beta} E_{x,y}^1$ if and only if $\beta(x) = u \wedge \exists e \in \mathcal{D}(E) \bullet (e, \beta(y)) \in Snd$
- $(\sigma, u, cons, Snd) \models_{\beta} E_{x,y}^2$ if and only if $\beta(y) = u \wedge cons \subset \mathcal{D}(E)$

Observation: we don't use all information from the computation path.

We could, e.g., also keep track of event identities between send and receive.

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$$\begin{aligned}
 (\sigma, \varepsilon) &\xrightarrow[u]{(cons, Snd)} \dots \rightarrow (\sigma_0, \varepsilon_0) \xrightarrow[u_0]{(cons_0, Snd_0)} (\sigma_1, \varepsilon_1) \xrightarrow[c_1]{(cons_1, \{(:E, c_2)\})} (\sigma_2, \varepsilon_2) \xrightarrow[c_2]{(\{(:E)\}, Snd_2)} \\
 (\sigma_3, \varepsilon_3) &\xrightarrow[c_2]{(cons_3, \{(:F, c_3)\})} (\sigma_4, \varepsilon_4) \xrightarrow[c_2]{(cons_4, \{(G(), c_1)\})} (\sigma_5, \varepsilon_5) \xrightarrow[c_3]{(\{(:F)\}, Snd_5)} (\sigma_6, \varepsilon_6) \rightarrow \dots
 \end{aligned}$$

- $\beta = \{x \mapsto c_1, y \mapsto c_2, z \mapsto c_3\}$
- $(\sigma_0, u_0, cons_0, Snd_0) \models_{\beta} y.k > 0$
- $(\sigma_0, u_0, cons_0, Snd_0) \models_{\beta} x.k > 0$
- $(\sigma_1, c_1, cons_1, \{(:E, c_2)\}) \models_{\beta} E_{x,y}^!$
- $(\sigma_1, c_1, cons_1, \{(:E, c_2)\}) \models_{\beta} F_{x,y}^!$
- $\dots \models_{\beta} E_{x,y}^?$
- We set $(\sigma_4, c_2, cons_4, \{(G(), c_1)\}) \models_{\beta} G_{y,x}! \wedge G_{y,x}?$ (triggered operation or method call).

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TBA over Signature

Definition. A TBA

$$\mathcal{B} = (Expr_{\mathcal{B}}(X), X, Q, q_{ini}, \rightarrow, Q_F)$$

where $Expr_{\mathcal{B}}(X)$ is the set of **signal and attribute expressions** $Expr_{\mathcal{S}}(\mathcal{E}, X)$ over signature \mathcal{S} is called **TBA over \mathcal{S}** .

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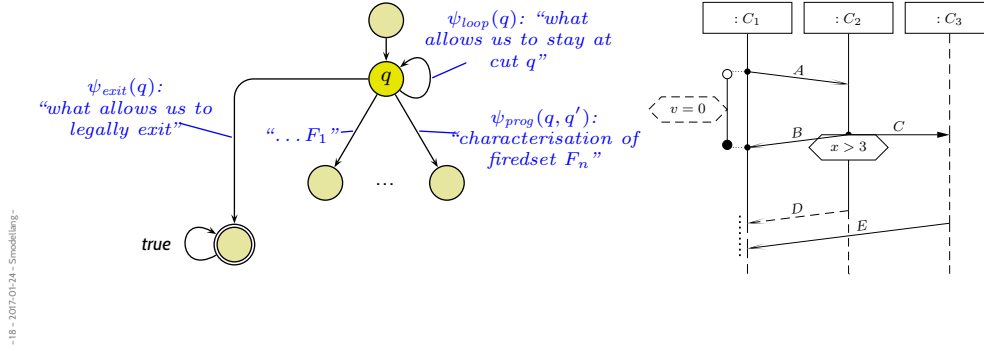
TBA Construction Principle

Recall: The TBA $\mathcal{B}(\mathcal{L})$ of LSC \mathcal{L} is $(Expr_{\mathcal{B}}(X), X, Q, q_{ini}, \rightarrow, Q_F)$ with

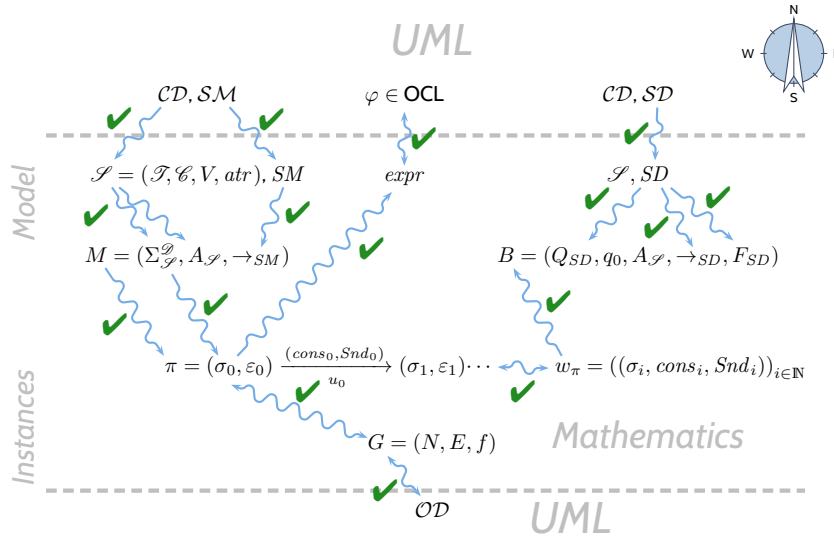
- Q is the **set of cuts** of \mathcal{L} , q_{ini} is the **instance heads cut**,
- $Expr_{\mathcal{B}} = \Phi \cup \mathcal{E}_{1?}(X)$,
- \rightarrow consists of **loops**, **progress transitions** (from \rightsquigarrow_F), and **legal exits** (cold cond./local inv.),
- $F = \{C \in Q \mid \Theta(C) = \text{cold} \vee C = L\}$ is the set of cold cuts.

So in the following, we “only” need to construct the transitions’ labels:

$$\rightarrow = \{(q, \psi_{loop}(q), q) \mid q \in Q\} \cup \{(q, \psi_{prog}(q, q'), q') \mid q \rightsquigarrow_F q'\} \cup \{(q, \psi_{exit}(q), L) \mid q \in Q\}$$



Course Map



Live Sequence Charts — Semantics Cont'd

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Full LSCs

A **full LSC** $\mathcal{L} = (((L, \preceq, \sim), \mathcal{I}, \text{Msg}, \text{Cond}, \text{LocInv}, \Theta), ac_0, am, \Theta_{\mathcal{L}})$ consists of

- **body** $((L, \preceq, \sim), \mathcal{I}, \text{Msg}, \text{Cond}, \text{LocInv}, \Theta)$,
- **activation condition** $ac_0 \in \text{Expr}_{\mathcal{L}}$,
- **strictness flag** *strict* (if *false*, \mathcal{L} is called **permissive**)
- **activation mode** $am \in \{\text{initial}, \text{invariant}\}$,
- **chart mode** **existential** ($\Theta_{\mathcal{L}} = \text{cold}$) or **universal** ($\Theta_{\mathcal{L}} = \text{hot}$).

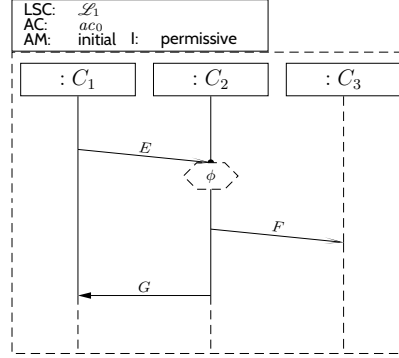
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A **full LSC** $\mathcal{L} = (((L, \preceq, \sim), \mathcal{I}, \text{Msg}, \text{Cond}, \text{LocInv}, \Theta), ac_0, am, \Theta_{\mathcal{L}})$ consists of

- **body** $((L, \preceq, \sim), \mathcal{I}, \text{Msg}, \text{Cond}, \text{LocInv}, \Theta)$,
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- **activation mode** $am \in \{\text{initial}, \text{invariant}\}$,
- **chart mode** **existential** ($\Theta_{\mathcal{L}} = \text{cold}$) or **universal** ($\Theta_{\mathcal{L}} = \text{hot}$).

Concrete syntax:

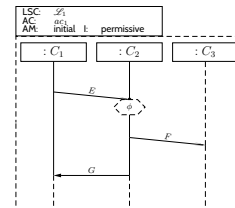


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A **full LSC** $\mathcal{L} = (((L, \preceq, \sim), \mathcal{I}, \text{Msg}, \text{Cond}, \text{LocInv}, \Theta), ac_0, am, \Theta_{\mathcal{L}})$ consists of

- **body** $((L, \preceq, \sim), \mathcal{I}, \text{Msg}, \text{Cond}, \text{LocInv}, \Theta)$,
- **activation condition** $ac_0 \in \text{Expr}_{\mathcal{L}}$,
- **strictness flag** *strict* (if *false*, \mathcal{L} is called **permissive**)
- **activation mode** $am \in \{\text{initial}, \text{invariant}\}$,
- **chart mode** **existential** ($\Theta_{\mathcal{L}} = \text{cold}$) or **universal** ($\Theta_{\mathcal{L}} = \text{hot}$).



A **set of words** $W \subseteq (\text{Expr}_{\mathcal{B}} \rightarrow \mathbb{B})^\omega$ is **accepted** by \mathcal{L} if and only if

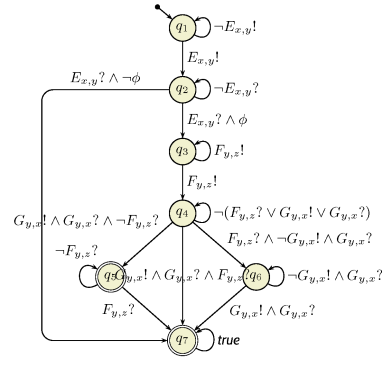
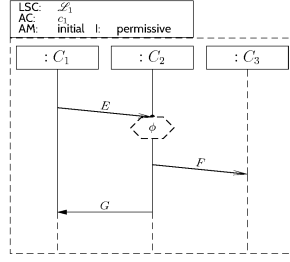
$\Theta_{\mathcal{L}}$	$am = \text{initial}$	$am = \text{invariant}$
cold	$\exists w \in W \bullet w^0 \models ac \wedge \neg \psi_{\text{exit}}(C_0)$ $\wedge w^0 \models \psi_{\text{prog}}(\emptyset, C_0) \wedge w/1 \in \mathcal{L}(\mathcal{B}(\mathcal{L}))$	$\exists w \in W \exists k \in \mathbb{N}_0 \bullet w^k \models ac \wedge \neg \psi_{\text{exit}}(C_0)$ $\wedge w^k \models \psi_{\text{prog}}(\emptyset, C_0) \wedge w/k + 1 \in \mathcal{L}(\mathcal{B}(\mathcal{L}))$
hot	$\forall w \in W \bullet w^0 \models ac \wedge \neg \psi_{\text{exit}}(C_0)$ $\implies w^0 \models \psi_{\text{prog}}(\emptyset, C_0) \wedge w/1 \in \mathcal{L}(\mathcal{B}(\mathcal{L}))$	$\forall w \in W \forall k \in \mathbb{N}_0 \bullet w^k \models ac \wedge \neg \psi_{\text{exit}}(C_0)$ $\implies w^k \models \psi_{\text{hot}}^{\text{Cond}}(\emptyset, C_0) \wedge w/k + 1 \in \mathcal{L}(\mathcal{B}(\mathcal{L}))$

where C_0 is the minimal (or **instance heads**) cut.

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Full LSC Semantics: Example

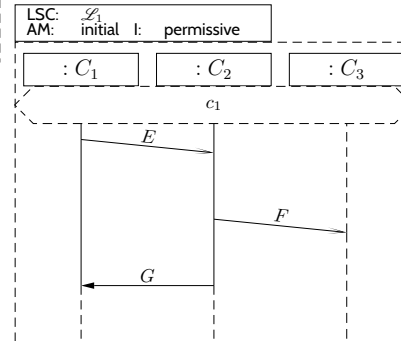
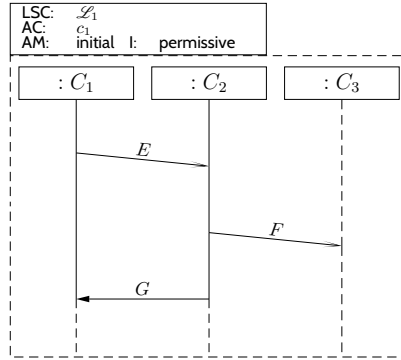


$$\begin{aligned}
 (\sigma, \varepsilon) &\xrightarrow[u]{(cons, Snd)} \dots \rightarrow (\sigma_0, \varepsilon_0) \xrightarrow[u_0]{(cons_0, Snd_0)} (\sigma_1, \varepsilon_1) \xrightarrow[c_1]{(cons_1, \{(:E, c_2)\})} (\sigma_2, \varepsilon_2) \xrightarrow[c_2]{(\{ :E \}, Snd_2)} \\
 (\sigma_3, \varepsilon_3) &\xrightarrow[c_2]{(cons_3, \{(:F, c_3)\})} (\sigma_4, \varepsilon_4) \xrightarrow[c_2]{(cons_4, \{(G(), c_1)\})} (\sigma_5, \varepsilon_5) \xrightarrow[c_3]{(\{ :F \}, Snd_5)} (\sigma_6, \varepsilon_6) \rightarrow \dots
 \end{aligned}$$

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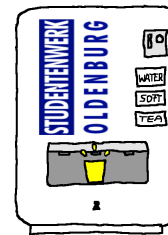
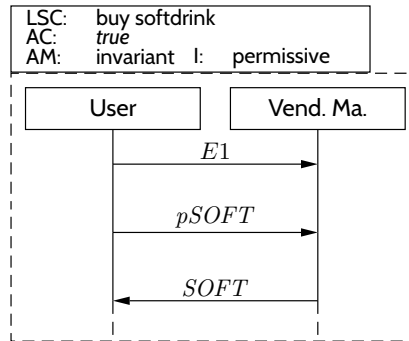
Note: Activation Condition



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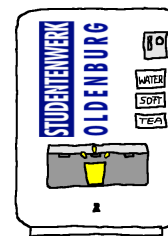
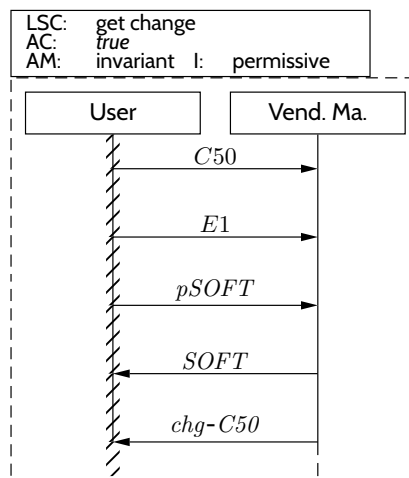
Existential LSC Example: Buy A Softdrink



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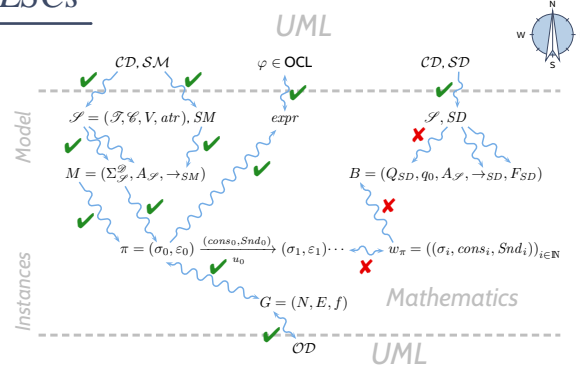
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Existential LSC Example: Get Change



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Plan:

- (i) Given an LSC \mathcal{L} with body

$$((L, \preceq, \sim), \mathcal{I}, \text{Msg}, \text{Cond}, \text{LocInv}, \Theta),$$
 - (ii) construct a TBA $\mathcal{B}_{\mathcal{L}}$, and
 - (iii) define language $\mathcal{L}(\mathcal{L})$ of \mathcal{L} **in terms of** $\mathcal{L}(\mathcal{B}_{\mathcal{L}})$,

in particular taking activation condition and activation mode into account.
 - (iv) define language $\mathcal{L}(\mathcal{M})$ of a UML model.
- Then $\mathcal{M} \models \mathcal{L}$ (**universal**) if and only if $\mathcal{L}(\mathcal{M}) \subseteq \mathcal{L}(\mathcal{L})$.
 And $\mathcal{M} \models \mathcal{L}$ (**existential**) if and only if $\mathcal{L}(\mathcal{M}) \cap \mathcal{L}(\mathcal{L}) \neq \emptyset$.

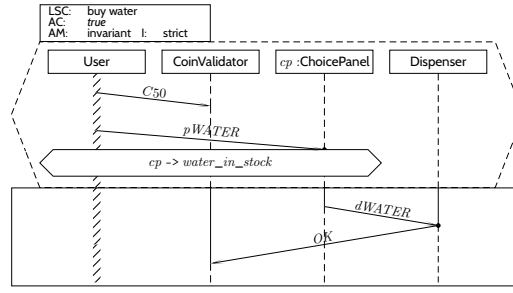
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Live Sequence Charts — Precharts

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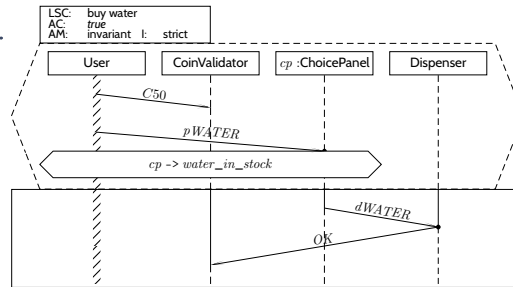
A full LSC $\mathcal{L} = (PC, MC, ac_0, am, \Theta_{\mathcal{L}})$ actually consist of

- **pre-chart** $PC = ((L_P, \preceq_P, \sim_P), \mathcal{I}_P, \mathcal{S}, \text{Msg}_P, \text{Cond}_P, \text{LocInv}_P, \Theta_P)$ (possibly empty),
- **main-chart** $MC = ((L_M, \preceq_M, \sim_M), \mathcal{I}_M, \mathcal{S}, \text{Msg}_M, \text{Cond}_M, \text{LocInv}_M, \Theta_M)$ (non-empty),
- **activation condition** $ac_0 : \text{Bool} \in \text{Expr}_{\mathcal{S}}$,
- **strictness flag** *strict* (otherwise called **permissive**)
- **activation mode** $am \in \{\text{initial}, \text{invariant}\}$,
- **chart mode** **existential** ($\Theta_{\mathcal{L}} = \text{cold}$) or **universal** ($\Theta_{\mathcal{L}} = \text{hot}$).

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Pre-Charts Semantics

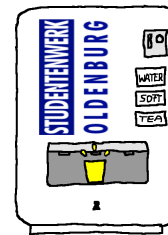
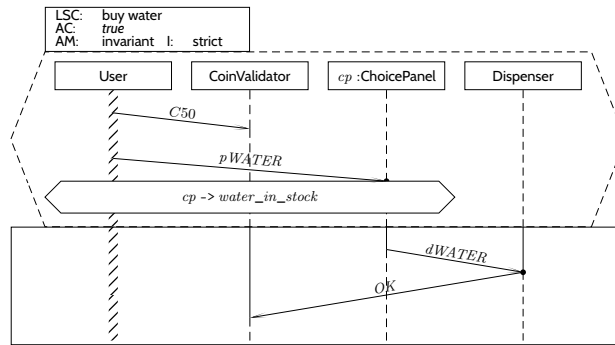


	$am = \text{initial}$	$am = \text{invariant}$
$\Theta_{\mathcal{L}} = \text{cold}$	$\exists w \in W \exists m \in \mathbb{N}_0 \bullet$ $\wedge w^0 \models ac \wedge \neg \psi_{\text{exit}}(C_0^P) \wedge \psi_{\text{prog}}(\emptyset, C_0^P)$ $\wedge w^1, \dots, w^m \in \mathcal{L}(\mathcal{B}(PC))$ $\wedge w^{m+1} \models \neg \psi_{\text{exit}}(C_0^M)$ $\wedge w^{m+1} \models \psi_{\text{prog}}(\emptyset, C_0^M)$ $\wedge w/m + 2 \in \mathcal{L}(\mathcal{B}(MC))$	$\exists w \in W \exists k < m \in \mathbb{N}_0 \bullet$ $\wedge w^k \models ac \wedge \neg \psi_{\text{exit}}(C_0^P) \wedge \psi_{\text{prog}}(\emptyset, C_0^P)$ $\wedge w^{k+1}, \dots, w^m \in \mathcal{L}(\mathcal{B}(PC))$ $\wedge w^{m+1} \models \neg \psi_{\text{exit}}(C_0^M)$ $\wedge w^{m+1} \models \psi_{\text{prog}}(\emptyset, C_0^M)$ $\wedge w/m + 2 \in \mathcal{L}(\mathcal{B}(MC))$
$\Theta_{\mathcal{L}} = \text{hot}$	$\forall w \in W \forall m \in \mathbb{N}_0 \bullet$ $\wedge w^0 \models ac \wedge \neg \psi_{\text{exit}}(C_0^P) \wedge \psi_{\text{prog}}(\emptyset, C_0^P)$ $\wedge w^1, \dots, w^m \in \mathcal{L}(\mathcal{B}(PC))$ $\wedge w^{m+1} \models \neg \psi_{\text{exit}}(C_0^M)$ $\implies w^{m+1} \models \psi_{\text{prog}}(\emptyset, C_0^M)$ $\wedge w/m + 2 \in \mathcal{L}(\mathcal{B}(MC))$	$\forall w \in W \forall k \leq m \in \mathbb{N}_0 \bullet$ $\wedge w^k \models ac \wedge \neg \psi_{\text{exit}}(C_0^P) \wedge \psi_{\text{prog}}(\emptyset, C_0^P)$ $\wedge w^{k+1}, \dots, w^m \in \mathcal{L}(\mathcal{B}(PC))$ $\wedge w^{m+1} \models \neg \psi_{\text{exit}}(C_0^M)$ $\implies w^{m+1} \models \psi_{\text{prog}}(\emptyset, C_0^M)$ $\wedge w/m + 2 \in \mathcal{L}(\mathcal{B}(MC))$

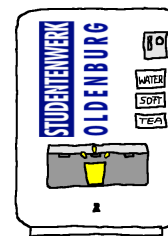
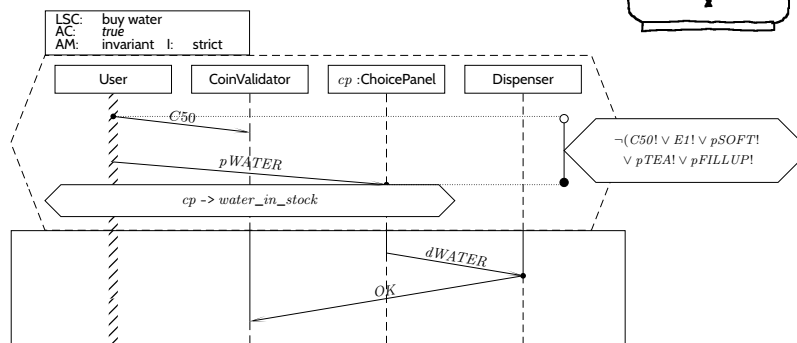
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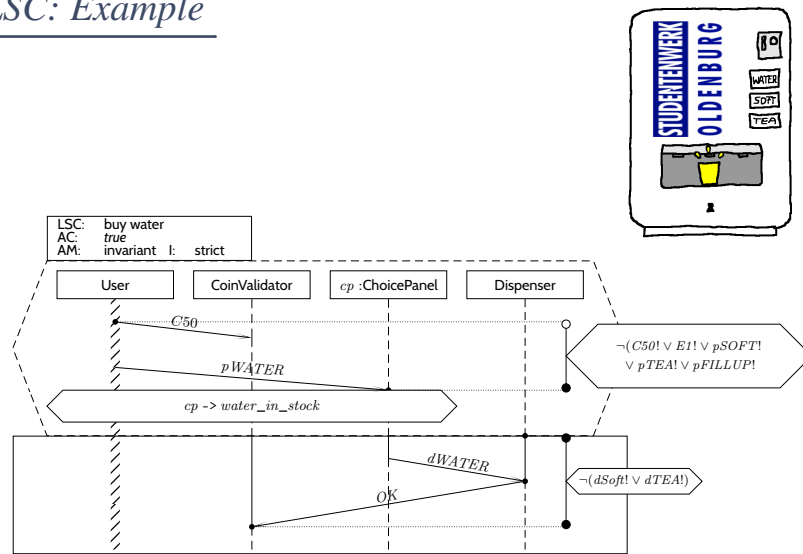
Universal LSC: Example



Universal LSC: Example



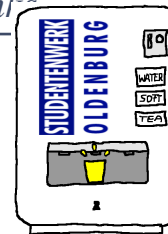
Universal LSC: Example



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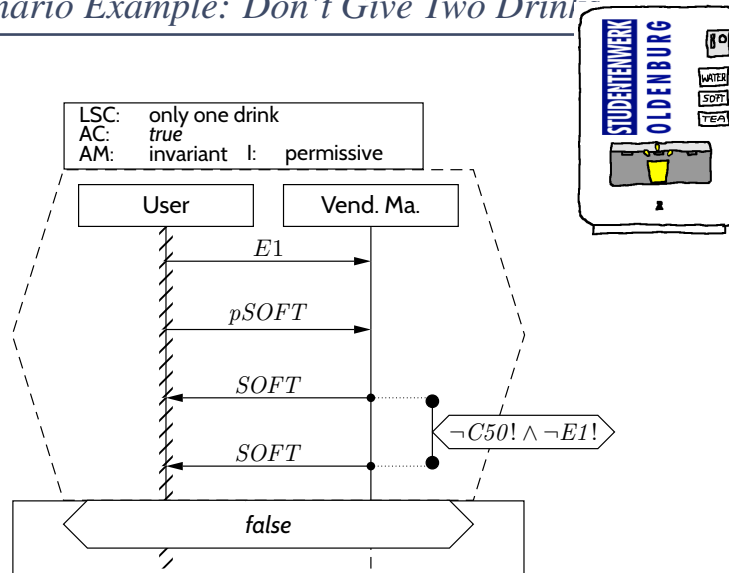
Forbidden Scenario Example: Don't Give Two Drinks



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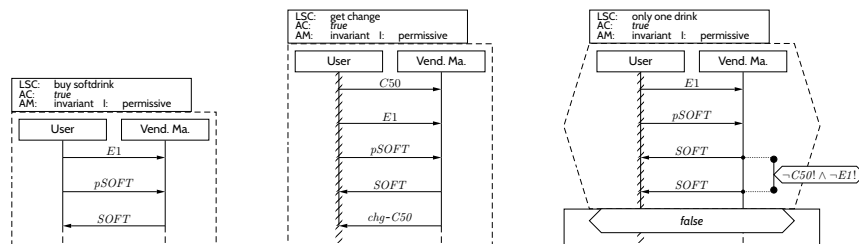
Forbidden Scenario Example: Don't Give Two Drinks



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Note: Sequence Diagrams and (Acceptance) Test



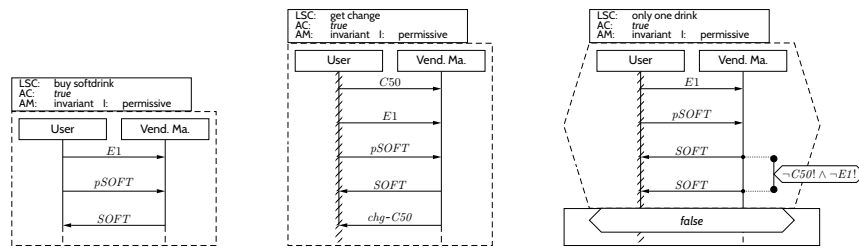
- Existential LSCs* may hint at **test-cases** for the **acceptance test!**

(*: as well as (positive) scenarios in general, like use-cases)

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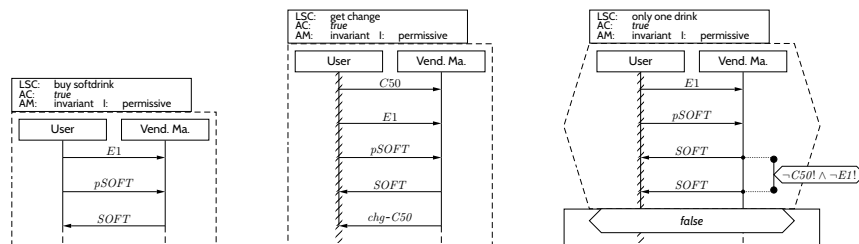
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Note: Sequence Diagrams and (Acceptance) Test

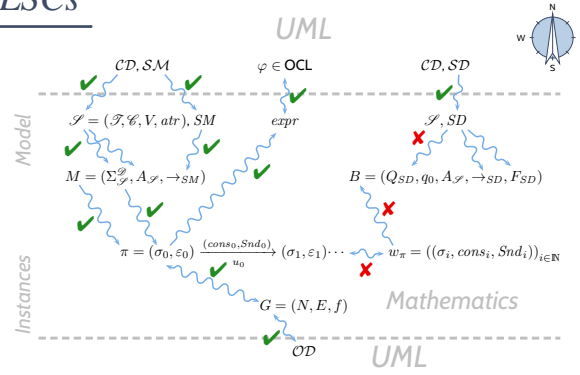


- **Existential** LSCs* may hint at **test-cases** for the **acceptance test!**
(*: as well as (positive) scenarios in general, like use-cases)
- **Universal** LSCs (and negative/anti-scenarios) in general need **exhaustive analysis!**

Note: Sequence Diagrams and (Acceptance) Test



- **Existential** LSCs* may hint at **test-cases** for the **acceptance test!**
(*: as well as (positive) scenarios in general, like use-cases)
- **Universal** LSCs (and negative/anti-scenarios) in general need **exhaustive analysis!**
(Because they require that the software **never ever** exhibits the unwanted behaviour.)



Plan:

(i) Given an LSC \mathcal{L} with body

$$((L, \preceq, \sim), \mathcal{I}, \text{Msg}, \text{Cond}, \text{LocInv}, \Theta),$$

(ii) construct a TBA $\mathcal{B}_{\mathcal{L}}$, and

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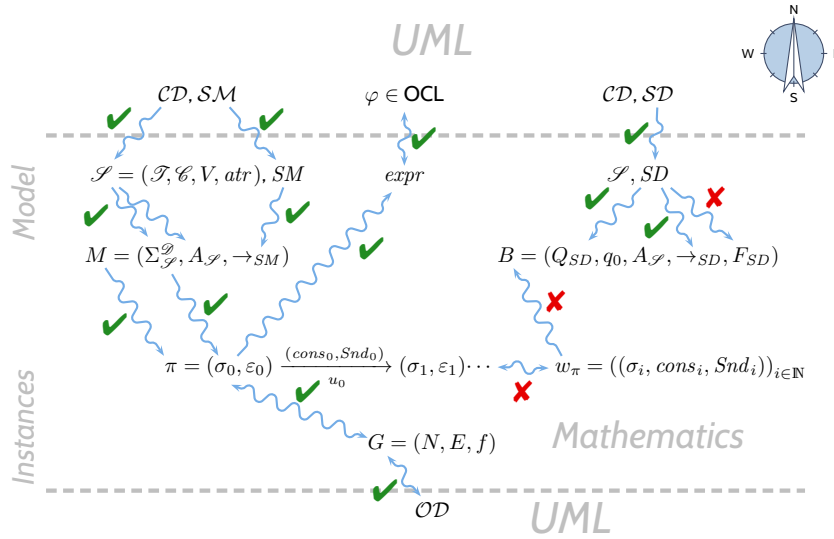
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Course Map



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- Büchi automata accept infinite words
 - if there exists is a run over the word,
 - which visits an accepting state infinitely often.
- The language of a model is just a rewriting of computations into words over an alphabet.
- An LSC accepts a word (of a model) if
 - Existential: at least on word (of the model) is accepted by the constructed TBA,
 - Universion: all words (of the model) are accepted.
- Activation mode initial activates at system startup (only), invariant with each satisfied activation condition (or pre-chart).
- Pre-charts can be used to state forbidden scenarios.
- Sequence Diagrams can be useful for testing.

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