Software Design, Modelling and Analysis in UML Lecture 18: Live Sequence Charts II

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Semantic Variation Points

- Pessimistic view: There are too many...

Constructive Behavioural Modelling in UML: Discussion

- allow absence of initial pseudo-states
  object may be the "En en acknowled state without being in any substate,
  or assume one of the chieflow state non-deterministically
  or assume one of the chieflow state non-deterministically
  is considering the outer which things have been added to the CASE tools repository,
  or some graphical order fleft to right top to bottom)
- Exercise: Search the standard for "semantical variation point".
- $\label{thm:comparison} Cane and Depet(2007), e.g., provide an in-depth comparison of Statemate, UML and Rhapsody state machines the bottom line is:$
- the intersection is not empty (i.e. some diagrams mean the same to all three communities)
   none is the subset of another (i.e. each pair of communities has diagrams meaning different things)

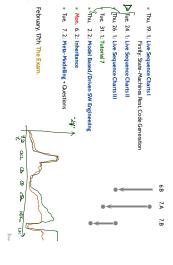
tools exist with complete and consistent code generation.
 good modelling-guidelines can contribute to avoiding misunderstandings.

Content

 Live Sequence Charts
 Abstract Syntax Well-Formedness
 Semantics
 TBA Construction for LSC Body interactions

• A Brief History of Sequence Diagrams e Excursion: Büchi Automata
le Language of a Model
Full LSCs Reflective Descriptions of Behavious -(e Existential and Universal -(e Pre-Charts -(e Forbidden Scenarios -(e Cuts, Firedsets
-(e Signal / Attribute Expressions
-(e Loop / Progress Conditions → LSCs and Tests Come single congress of the co 72 of the and a

## The Plan



Reflective Descriptions of Behaviour

# Constructive vs. Reflective Descriptions

 A reflective description tells us what shall (or shall not) be computed: "Other languages are reflective or assertive, and can be used by the system modeler to capture parts of the thinking and can be used by the system modeler to capture parts of the that go into building the model - behavior be culted -, to derive and prosent views of the model, statically or during execution, or to set constraints on behavior in preparation for verification."



Note: No sharp boundaries! (Would be too easy.)

# Interactions as Reflective Description

- In UML, reflective (temporal) descriptions are subsumed by interactions. A UML model  $\mathcal{M}=(\mathscr{CG},\mathscr{SM},\mathscr{GG},\mathscr{F})$  has a set of interactions  $\mathscr{F}$ . An interaction  $\mathcal{I}\in\mathscr{F}$  can be (OMG claim: equivalently) diagrammed as
- communication diagram (formerly known as collaboration diagram).
   timing diagram, or
   sequence diagram.



## Hence: Live Sequence Charts

Why Sequence Diagrams?

Most Prominent: Sequence Diagrams – with long history:

- Message Sequence Charts: standardized by the ITU in different versions often accused to lake a lognoistic standard sequence Diagrams of UML 1x.

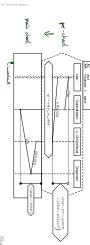
Most severe drawbacks of these formalisms:

User Cornhibitator ChoicePanel Dispersion

conditions merely comments

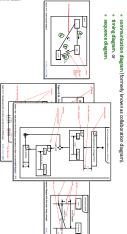
no means to express forbidden scenarios undear progress requirement: must all messages be observed? undear activation: what triggers the requirement? unclear interpretation: example scenario or invariant?

- SDs of UML 2.x address some issues.
   yet the standard exhibits unclarities and even contradictions Harel and Maoz (2007); Si6rile (2003)
- For the lecture, we consider Live Sequence Charts (LSCs) Damm and Harel (2001); Klose (2003); Harel and Marelly (2003).
- who have a common fragment with UML 2x SDs Harel and Maoz (2007)
  Modelling guideline: stick to that fragment.

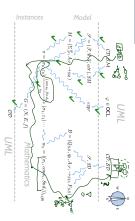


# Interactions as Reflective Description

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## Course Map



logical variable/

Full LSC Building Blocks for Later

LSC Body: Abstract Syntax

Definition. [LSC Body]  $\text{An LSC body over signature } \mathcal{S} = (\mathcal{T}, \mathscr{C}, V, atr, \mathcal{E}) \text{ is a tuple}$ 

 $((L,\preceq,\sim),\mathcal{I},\mathsf{Msg}\,,\mathsf{Cond},\mathsf{LocInv},\Theta)$ 

\* L is a finite, non-empty of locations with \* a partial order  $\preceq \subseteq L \times L$ . \* a symmetric simultaneity relation  $\sim \subseteq L \times L$  disjoint with  $\preceq$  i.e.  $\preceq \cap \sim = \emptyset$ .  $=\mathcal{I}=\{I_1,\ldots,I_n\}$  is a partitioning of L; elements of  $\mathcal{I}$  are called instance line,

Cond  $\subseteq (2^L \setminus \emptyset) \times Expr_{\mathscr{S}}$  is a set of conditions with  $(L,\phi) \in \mathsf{Cond}$  only if  $l \sim l'$  for all  $l \neq l' \in L$ ,

 $\begin{array}{l} \mathsf{LocInv} \subseteq L \times \{\diamond, \bullet\} \times Expr_{\mathscr{S}} \times L \times \{\diamond, \bullet\} \text{ is a set of local invariants} \\ \mathsf{with} \ (l, \iota, \phi, l', \iota') \in \mathsf{LocInv} \ \mathsf{only} \ \mathsf{if} \ l \prec l', \circ \ \mathsf{exclusive}, \bullet \ \mathsf{inclusive}. \end{array}$ 

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\* Meg  $\subseteq L \times \mathscr{E} \times L$  is a set of messages with  $(l,E,l') \in \mathsf{Meg}$  only if  $(l,l') \in \neg \cup \neg$  message (l,E,l') is called instantaneous iff  $l \sim l'$  and asynchronous otherwise.

Live Sequence Charts — Syntax

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LSC Body Building Blocks

LSC Body Building Blocks

instance line head /

life line / instance line /

(hot).condition /

From Concrete to Abstract Syntax  $\begin{aligned} & \text{Sociators} L, \\ & & \leq L \times L, \\ & & \leq L \times L, \\ & & = \{1, \dots, n_i\}, \\ & & \text{Mag} \left( L \times \mathcal{E} \times L, \\ & & \text{Cond} \left( \frac{n^2 \cdot (\mathbf{e})}{2} \times \text{Barr}_{\mathcal{F}} \times L \times \{\mathbf{e}, \mathbf{e}\}, \\ & & \text{Loding} \left( L \times (\mathbf{e} \times L) \times \text{Barr}_{\mathcal{F}} \times L \times \{\mathbf{e}, \mathbf{e}\}, \\ & & \quad \oplus : L \cup \text{Mag} \cup \text{Cond} \cup \text{Lodinv} \to \{\text{tot}, \text{codd}\}. \end{aligned}$ 

~ { ((a, b, b) } M Mg = { ((a, b, a, b, c), - } Cond - { ((ba), x-2)} Lectur - { ((a, 0, x-0, ba, - ))} Cyroad Cygradd 0 = { M is life, C is life. I'm cold. Cybradd Cygradd From Concrete to Abstract Syntax Observed:  $\sim \subseteq L \times L$   $\preceq \subseteq L \times L$ ,  $\sim \subseteq L \times L$   $Z = \{I_1, \dots, I_k\}$ ,  $Mag \subseteq L \times \times X$ ,  $Mag \subseteq L \times X$ ,  $Mag \subseteq$ ~ = { ((21. (4.)) }

TBA-based Semantics of LSCs (ii) construct a TBA  $E_{\mathcal{S}_c}$  and (iii) define hegauge  $\mathcal{L}(\mathcal{S})$  of  $\mathcal{S}'$  in terms of  $\mathcal{L}(B_{\mathcal{S}'})$ , in juricular taking extraction condition and activation mode into account. (iv) define language  $\mathcal{L}(\mathcal{M})$  of a UML model. (i) Given an LSC  $\mathscr L$  with body  $((L, \preceq, \sim), \mathcal{I}, \mathsf{Msg}, \mathsf{Cond}, \mathsf{LocInv}, \Theta),$ 

Live Sequence Charts — Semantics

• Then  $\mathcal{M} \models \mathscr{L}$  (universal) if and only if  $\mathcal{L}(\mathcal{M}) \subseteq \mathcal{L}(\mathscr{L})$ . And  $\mathcal{M} \models \mathscr{L}$  (existential) if and only if  $\mathcal{L}(\mathcal{M}) \cap \mathcal{L}(\mathscr{L}) \neq \emptyset$ .

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Well-Formedness

From Concrete to Abstract Syntax

\* locations L. \*  $\leq \subseteq X \times L$ .  $\sim \subseteq L \times L$ \*  $A = \{(1, \dots, I_n)\}$ . \*  $Mag \subseteq L \times \{(1, \dots, I_n)\}$ . \*  $Mag \subseteq L \times \{(1, \dots, I_n)\}$ . \*  $Code \subseteq L \times \{(1, \dots, I_n)\}$ . \*  $B : L \cup Mag \cup Conid \cup Locher \rightarrow \{(n_1, n_2)\}$ . \*  $B : L \cup Mag \cup Conid \cup Locher \rightarrow \{(n_1, n_2)\}$ .

Š

Bondedness/no floating conditions: (could be relaxed a little  $i^{t}$  we wanted to)

\* For each location  $i \in I$ , if i is the location of

\* a condition, i.e.  $\exists (I_{i}, b) \in \text{Cond}: i \in L$ , or

\* a local invariant. i.e.  $\exists (I_{i+1}, b, I_{b+1}) \in \text{Lociny}: I \in \{I_{i+1}, I_{b}\}$ .

\*  $\supseteq I \subseteq I$  a message, i.e. • a local formula in  $t = J(i_1, i_1, i_2, i_3, i_4) \in locator : t \in \{i_1, i_2\},$ then there is a location if simultaneous to l, i.e.  $l \sim l'$ , which is the location of  $\frac{l}{2}$ • an instance had, i.e. l is minimal wit  $\preceq$  or

::  $\exists \, (l_1, E, l_2) \in \mathsf{Msg} : l \in \{l_1, l_2\}.$ 

Note: if messages in a chart are cyclic, then there doesn't exist a partial order (so such diagrams don't even have an abstract syntax).

Live Sequence Charts — TBA Construction

# Definition $\operatorname{Let}((L,\preceq \sim),\mathcal{I}_{i}\operatorname{Mag}_{i}\operatorname{Cond}_{i}\operatorname{Locinv}, \Theta) \text{ be an LSC body},$ A non-empty set $\Psi_{i}$ $C\subseteq L$ is called a out of the LSC body iff $\bullet \text{ it is downward dose} i.e. \forall I, f'\bullet i' \in C \land I \preceq I' \Longrightarrow I \in C,$ $\bullet \text{ it is dosed under simultaneity}, i.e. <math display="block">\forall I, I'\bullet i' \in C \land I \sim I' \Longrightarrow I \in C, \text{ and}$ $\bullet \text{ it comprises at least one location per instance line, i.e.}$ $\forall i \in I \exists I \in C \bullet i_{I} = i.$

Formal LSC Semantics: It's in the Cuts!

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# Formal LSC Semantics: It's in the Cuts!

 $\emptyset 
eq C \subseteq L$  – downward closed – simultaneity closed – at least one loc, per instance line

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## Cut Examples

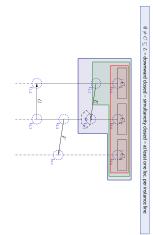
Cut Examples

 $\emptyset \neq C \subseteq L \text{ --} \text{ downward closed -- simultaneity closed -- at least one loc, per instance line}$ 

# $\emptyset \neq C \subseteq L - \text{downward closed} - \text{simultaneity closed} - \text{at least one for, per instance line}$

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## Cut Examples

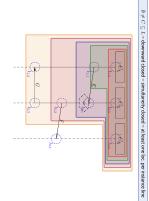


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 $\emptyset \neq C \subseteq L - \mathsf{downward} \ \mathsf{closed} - \mathsf{simultane} \mathsf{ity} \ \mathsf{closed} - \mathsf{at} \ \mathsf{least} \ \mathsf{one} \ \mathsf{loc}. \ \mathsf{per} \ \mathsf{instance} \ \mathsf{line}$ 

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Cut Examples



Successor Cut Example

A Successor Relation on Cuts

The partial order " $\preceq$  " and the simultaneity relation " $\sim$  " of locations induce a direct successor relation on cuts of an LSC body as follows:

\*  $C \cap F = \emptyset$  and  $C \cup F$  is a cut, i.e. F is closed under simultaneity, \* all locations in F are direct  $\leftarrow$  successors of the front of C, i.e.  $\forall I \in F \ni I' \in C \circ I' \prec I \land (\exists I'' \in C \circ I'' \prec I),$ 

The cut  $C' = C \cup F$  is called direct successor of C via F , denoted by  $C \leadsto_F C'$  . for each asynchronous (!) message reception in F, the corresponding sending is already in C.  $\forall (l,E,l') \in \mathsf{Msg} \bullet l' \in F \implies l \in C.$ cations in F, that the on the same instance line, are pairwise unordered, i.e.  $\forall l \neq l' \in F \bullet (\exists I \in \mathcal{I} \bullet \{l, l'\} \subseteq I) \implies l \not\preceq l' \land l' \not\preceq l,$ 

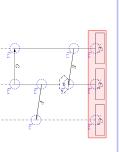
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 $\begin{array}{l} \mbox{Definition} \\ \mbox{Let $C\subseteq L$ bet a cut of LSC body} ((U,\underline{\prec},\sim),Z, \mbox{Msg}, \mbox{Cond}, \mbox{Locinv}, \Theta). \\ \mbox{A set } \emptyset \neq F \subseteq L \mbox{of botations is called fired-set $F$ of cut $C$ if and only if} \\ \end{array}$ 

Cut Examples

 $\emptyset \neq C \subseteq L - \mathsf{downward} \ \mathsf{closed-simultaneity} \ \mathsf{closed-at} \ \mathsf{least} \ \mathsf{one} \ \mathsf{loc}. \ \mathsf{per} \ \mathsf{instance} \ \mathsf{line}$ 

 $C\cap F=\emptyset-C\cup F$  is a cut – only direct  $\prec$ -successors – same instance line on front pairwise unordered – sending of asynchronous reception already in



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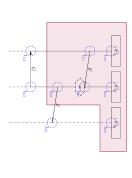
Cut Examples

 $\emptyset \neq C \subseteq L$  – downward closed – simultaneity closed – at least one loc. per instance line

## Successor Cut Example

Language of LSC Body: Example

 $C\cap F=\emptyset$  –  $C\cup F$  is a cut – only direct  $\prec$ -successors – same instance line on front pairwise unordered – sending of asynchronous reception already in



# Signal and Attribute Expressions

Language of LSC Body: Example

- $\bullet \ \ {\rm Let} \ \mathscr{S} = (\mathscr{T},\mathscr{C},V,atr,\mathscr{E})$  be a signature and X a set of logical variables,
- $\circ$  The signal and attribute expressions  $Expr_{\mathscr{S}}(\mathscr{E},X)$  are defined by the grammar:
- $\psi ::= \mathit{true} \mid \psi \mid E_{x,y}^{1} \mid E_{x,y}^{2} \mid \neg \psi \mid \psi_{1} \lor \psi_{2},$
- where  $expr:Bool\in Expr_{\mathscr{S}}, E\in\mathscr{E}, x,y\in X$  (or keyword env).
- $\mathcal{S}_{7}(X):=\{E_{x,y}^{1},E_{x,y}^{?}\mid E\in\mathscr{E},x,y\in X\}$  to denote the set of event expressions over  $\mathscr{E}$  and X .

The TBA  $Q_p$  of LSC P over 4 and C is  $(\operatorname{Expr}_p(X), X, Q, q_{\min}, \rightarrow, Q_p)$  with Q the set of cost of Z  $q_{\min}$  be insumer beats on Q in the set of Q in the set of Q in the set of Q in Q

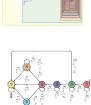
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## TBA Construction Principle

Recall: The TBA  $B(\mathscr{L})$  of LSC.  $\mathscr{L}$  is  $(Earr_{B}(X), X, Q, q_{min}, \rightarrow, Q_{F})$  with \* Q is the and of a and  $\mathscr{L}$ ,  $q_{min}$  is the instance heads out. \*  $Earr_{B} = \Phi \cup d_{B}(X)$ . \*  $\bot$  constant of loops, proportional form  $\neg p_{A}$  and  $\log_{B}$  in its ladd conducted in \*  $F = \{C \in Q \mid \Theta(C) = \operatorname{cold} \vee C = L\}$  is the set of cold out.

Language of LSC Body: Example



## TBA Construction Principle

- Recall: The TBA  $\mathcal{B}(\mathcal{L})$  of LSC  $\mathcal{L}$  is  $(Espr_B(X), X, Q, q_{mi}, \rightarrow, Q_F)$  with \* Q is the and case of  $\mathcal{L}$ ,  $q_m$  is the instance heads out. \*  $Espr_B = 9 \cup d_F(X)$ . \* constanted began parameters (from  $\rightarrow_F$ ) and legal exist (add and /bcd inv). \*  $F = \{C \in Q \mid \Theta(C) = \text{cold } V \in -L\}$  is the exist of cold cast.
- So in the following, we "only" need to construct the transitions' labels:

 $,q)\mid q\in Q\}\cup \{(q, \qquad \qquad ,q')\mid q\leadsto_{F}q'\}\cup \{(q, \qquad \qquad ,L)\mid q\in Q\}$ 

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## TBA Construction Principle

TBA Construction Principle

Recall: The TBA  $B(\mathcal{F})$  of LSC  $\mathcal{F}$  is  $(Expr_{\mathcal{F}}(X), X, Q, q_{mn}, \rightarrow, Q_{\mathcal{F}})$  with \* Q is the set of cota of  $\mathcal{F}_{*}$  q<sub>m</sub> is the instance heads out. \*  $Expr_{\mathcal{F}} = \Phi \cup \Phi_{\mathbb{F}}(X)$ , \*  $\rightarrow$  consists of loops, propositional form,  $p_{\mathbb{F}}$  and  $|\mathbf{r}_{\mathbb{F}}|$  entitle (odd conduction). \*  $\mathcal{F} = \{C \in Q \mid \Theta(C) = \operatorname{cold} V C = L\}$  is the set of cold outs.

So in the following, we "only" need to construct the transitions' labels:

 $\rightarrow = \{(q,\psi_{loop}(q),q) \mid q \in Q\} \cup \{(q,\psi_{proy}(q,q'),q') \mid q \leadsto_F q'\} \cup \{(q,\psi_{orit}(q),L) \mid q \in Q\}$ 

- Recall: The TBA  $B(\mathcal{L})$  of LSC  $\mathcal{L}'$  is  $(Expr_B(X), X, Q, q_{min}, \rightarrow, Q_F)$  with \* Q is the set of onto  $d \mathcal{L}' q_{min}$  is the notance heads on \*  $Expr_B = \Phi \circ d \circ f_{\mathbb{R}}(X)$ , \*  $\rightarrow$  consist of doops, proper transform (from  $\rightarrow p$ ), and legal entitled cond/hool inv.), \*  $F = \{C \in Q \mid \Phi(C) = \operatorname{cold} V : C = L\}$  is the set of cold onto.

# So in the following, we "only" need to construct the transitions' labels:

 $\rightarrow = \{(q, \psi_{\text{loop}}(q), q) \mid q \in Q\} \cup \{(q, \psi_{\text{prog}}(q, q'), q') \mid q \leadsto_{P} q'\} \cup \{(q, \psi_{\text{ext}}(q), L) \mid q \in Q\}$ 

Loop Condition

TBA Construction Principle

 $\begin{array}{l} \text{"Only" construct the transitions' labels:} \\ \longrightarrow = \{(q,\psi_{loop}(q),q) \mid q \in Q\} \cup \{(q,\psi_{loop}(q,q'),q') \mid q \leadsto_P q'\} \cup \{(q,\psi_{loo}(q),L) \mid q \in Q\} \end{array}$ 

 $\bullet \ \psi^{\mathsf{Mog}}(q) = \neg \bigvee_{1 \leq i \leq n} \psi^{\mathsf{Mog}}(q,q_i) \wedge \underbrace{\left( strict \implies \bigwedge_{\psi \in \mathsf{Mog}(L)} \neg \psi \right)}$ 

 $\psi_{loop}(q) = \psi^{\mathsf{MN}}(q) \wedge \psi^{\mathsf{Lodin}}_{\mathsf{Mat}}(q) \wedge \psi^{\mathsf{Lodin}}_{\mathsf{codd}}(q)$ 

- \*  $\psi_{g^{color}}^{(i)}(i) = \Lambda_{l=(1,i,\phi,l',L') \in Lodes}, \otimes_{(i)=\theta}, \ell \text{ extrest}_{\theta} \circ \Lambda$ A location it salled front boation of art  $C^{i}$  and only if  $\beta l' \in L \bullet l \prec l'$ .
  Local invariant  $(l_{i,i,\phi}, l_{i,j-1})$  is a these art  $\alpha l^{i} l_{i} = \Lambda$ .
  If and only if  $l_{i,j} \leq l \cdot l_{i} = 1$  for some front location l of art q or  $l_{i} \in q \wedge l_{i} = \bullet$ .
- $\bullet \ \operatorname{Msg}(F) = \{E^1_{x_l,x_{l'}} \mid (l,E,l') \in \operatorname{Msg}, \ l \in F\} \cup \{E^2_{x_l,x_{l'}} \mid (l,E,l') \in \operatorname{Msg}, \ l' \in F\}$
- $x_l \in X$  is the logical variable associated with the instance line I which includes l, i.e.  $l \in I$ .
- \*  $\mathsf{Msg}(F_1,\ldots,F_n) = \bigcup_{1 \leq i \leq n} \mathsf{Msg}(F_i)$



# $\psi_{prog}^{\mathsf{hot}}(q,q_i) = \psi^{\mathsf{Msg}}(q,q_n) \wedge \psi_{\mathsf{loc}}^{\mathsf{Conf}}(q,q_n) \wedge \psi_{\mathsf{loc}}^{\mathsf{Locfer}, \bullet}(q_n)$

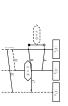
Progress Condition

 $* \ \psi^{\mathsf{Mod}}(q,q_i) = \bigwedge_{\phi \in \mathsf{Mod}(q_i \setminus q)} \psi \land \bigwedge_{j \neq i} \bigwedge_{\phi \in \mathsf{Mod}(q_j \setminus q) \setminus \mathsf{Mod}(q_i \setminus q)} \neg \psi$ 

- $\bullet \ \psi_{\theta}^{\mathsf{Cond}}(q,q_i) = \bigwedge_{\gamma = (L,\phi) \in \mathsf{Cond}, \ \Theta(\gamma) = \theta, \ L \cap (q_i \setminus q) \neq \emptyset} \phi$
- $\psi_{i}^{\text{locked}}(q,q) = \bigwedge_{i=1,i,j}(L_{i},L_{i}) \in \text{cachy } a(q) = d \land v \text{ extens } a(q)$ Local invariant  $((u_{i},u_{i},\phi_{i},l_{i},L_{i}))$  is active at q if and only if

    $l_{i} < l < l_{i}, c$   $l = l_{i} \land \lambda \land a = v \land c$ for some front location l of cat (0,q)



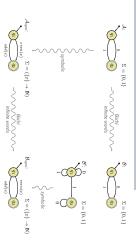


Example

Course Map

OD UML

From Finite Automata to Symbolic Büchi Automata



Excursion: Büchi Automata

Tell Them What You've Told Them...

- Interactions can be reflective descriptions of behaviour, i.e.
   describe what behaviour is (un)desired,
   without (yet) defining how to realise it
- One visual formalism for interactions: Live Sequence Charts
   Iccations in degram induce a partial order;
   Instantaneous and aprohironous messages.
   conditions and local invariants
- The meaning of an LSC is defined using TBAs.

- Cuts become states of the automaton.
  Locations induce a partial order on cuts.
  Automation-transitions and amoutations correspond to a successor relation on cuts.
  Amoutations use signal / attribute expressions.

TBA have Büchi acceptance (of infinite words (of a model)).
 Full LSC semantics.
 Pre-Charts.

Symbolic Büchi Automata

\*  $Expr_{B}(X)$  is a set of Boolean expressions over X. 
\* Q is a finite set of states. Definition. A Symbolic Būchi Automaton (TBA) is a tuple  $* o \subseteq Q \times Expr_B(X) \times Q$  is the transition relation. Transitions  $(q,\psi,q')$  from q to q' are labelled with an expression  $\psi \in Expr_B(X)$ . •  $q_{ini} \in Q$  is the initial state, X is a set of logical variables.  $\mathcal{B} = (\mathit{Expr}_{\mathcal{B}}(X), X, Q, q_{ini}, \rightarrow, Q_F)$ 

 $\circ \ Q_F \subseteq Q$  is the set of fair (or accepting) states.

Run of TBA over Word

Definition. Let  $\mathcal{B}=(Expr_{\mathcal{B}}(X),X,Q,q_{ini},\rightarrow,Q_F)$  be a TBA and

a word for  $\mathit{Expr}_{\mathcal{B}}(X).$  An infinite sequence

is called run of  $\mathcal B$  over w under valuation  $\beta:X\to \mathscr D(X)$  if and only if

 $\varrho=q_0,q_1,q_2,\ldots\in Q^\omega$  $w = \sigma_1, \sigma_2, \sigma_3, \dots$ 

• for each  $i \in \mathbb{N}_0$  there is a transition

 $(q_i,\psi_i,q_{i+1}) \in \rightarrow$ 

such that  $\sigma_i \models_\beta \psi_i$ .

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over (\Sigma,\cdot\models\cdot\cdot) is called word (for \mathit{Expr}_{\mathcal{B}}(X) ).
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  Definition. Let X be a set of logical variables and let Expr_B(X) be a set of Boolean expressions over X. A set (\Sigma, \cdot \models \cdot, \cdot) is called an alphabet for Expr_B(X) if and only if
                                                                                                            An infinite sequence
                                                                                                                                                                                                                                                                                                                                                                                                         \bullet \mbox{ for each expression } expr \in Expr_B, \mbox{and} \\ \bullet \mbox{ for each valuation } \beta: X \to \mathcal{D}(X) \mbox{ of logical variables},
                                                                                                                                                                                                                                           either \sigma \models_{\beta} expr or \sigma \not\models_{\beta} expr.
es (or does not satisfy) expr undervaluation \beta)
                                                      w = (\sigma_i)_{i \in \mathbb{N}_0} \in \Sigma^{\omega}
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## The Language of a TBA

The Language of a TBA

```
We call the set \mathcal{L}(\mathcal{B})\subseteq (Expr_{\mathcal{B}}\to \mathbf{B})^\omega of words that are accepted by \mathcal{B} the language of \mathcal{B}
                                                                                                                                                           \varrho=(q_i)_{i\in\mathbb{N}_0} over w such that fair (or accepting) states are visited in finitely often by \varrho, i.e. such that
                                                                                                                                                                                                                                                                                                                                                                   Definition. We say TBA \mathcal{B}=(Expr_{\mathcal{B}}(X),X,Q,q_{mi},\rightarrow,Q_F) accepts the word
                                                                                                                                                                                                                                                                                   if and only if \mathcal{B} has a run
                                                                                                              \forall i \in \mathbb{N}_0 \; \exists \; j > i : q_j \in Q_F.
                                                                                                                                                                                                                                                                                                                                     w = (\sigma_i)_{i \in \mathbb{N}_0} \in (Expr_B \to \mathbb{B})^{\omega}
```

 $\varrho=(q_i)_{i\in\mathbb{N}_0}$  over w such that fair (or accepting) states are visited infinitely often by  $\varrho,$  i.e. such that

 $\forall \, i \in \mathbb{N}_0 \, \exists \, j > i : q_i \in Q_F.$ 

if and only if  ${\cal B}$  has a run

Definition. Definition. We say TBA  $\mathcal{B}=(Expr_{\mathcal{B}}(X),X,Q,q_{ini},\rightarrow,Q_F)$  accepts the word

 $w = (\sigma_i)_{i \in \mathbb{N}_0} \in (Expr_B \to \mathbb{B})^{\omega}$ 

We call the set  $\mathcal{L}(\mathcal{B})\subseteq (Expr_S\to \mathbf{B})^\omega$  of words that are accepted by  $\mathcal{B}$  the language of  $\mathcal{B}$ .

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Language of UML Model

Run of TBA over Word

is called run of  $\mathcal B$  over w under valuation  $\beta\colon X\to \mathscr D(X)$  if and only if Definition. Let  $\mathcal{B}=(Expr_{\mathcal{B}}(X),X,Q,q_{ini},\rightarrow,Q_F)$  be a TBA and • for each  $i \in \mathbb{N}_0$  there is a transition a word for  $\mathit{Expr}_{\mathcal{B}}(X)$  . An infinite sequence such that  $\sigma_i \models_{\beta} \psi_i$ .  $\varrho=q_0,q_1,q_2,\ldots\in Q^\omega$  $w = \sigma_1, \sigma_2, \sigma_3, \dots$  $(q_i,\psi_i,q_{i+1}) \in \rightarrow$ 

Example:  $\underbrace{S_{\text{over}}(z)}_{\text{odd}(z)}\underbrace{\underbrace{cren(z)}_{\text{odd}(z)}}_{3!}$  $\Sigma = (\{x\} \rightarrow \mathbb{N})$ 

## The Language of a Model

Recall: A UML model  $\mathcal{M}=(\mathscr{CD},\mathscr{SM},\mathscr{OD})$  and a structure  $\mathscr{D}$  denote a set  $[\![\mathcal{M}]\!]$  of (initial and consecutive) computations of the form

 $a_i = \big( \cos s_i, \operatorname{Sn} d_i, u_i \big) \in \underbrace{2^{\mathscr{D}(\mathscr{E})} \times 2^{(\mathscr{D}(\mathscr{E}) \cup \{*,+\}) \times \mathscr{D}(\mathscr{E})} \times \mathscr{D}(\mathscr{E})}_{.}.$  $(\sigma_0,\varepsilon_0) \xrightarrow{a_0} (\sigma_1,\varepsilon_1) \xrightarrow{a_1} (\sigma_2,\varepsilon_2) \xrightarrow{a_2} \dots \text{ where }$ 

Words over Signature

Definition, Let  $\mathscr{S}=(\mathscr{T},\mathscr{C},V,atr,\mathscr{E})$  be a signature and  $\mathscr{D}$  a structure of  $\mathscr{S}.$  A word over  $\mathscr{S}$  and  $\mathscr{D}$  is an infinite sequence

 $(\sigma_i, u_i, cons_i, Snd_i)_{i \in \mathbb{N}_0} \in \Sigma_{\mathscr{P}}^{\mathscr{D}} \times \mathscr{D}(\mathscr{C}) \times 2^{\mathscr{D}(\mathscr{C})} \times 2^{(\mathscr{D}(\mathscr{C}) \cup \{\bullet, +\}) \times \mathscr{D}(\mathscr{C})}$ 

• The language  $L(\mathcal{M})$  of a UML model  $\mathcal{M}=(\mathscr{CG},\mathscr{SM},\mathscr{CG})$  is a word over the signature  $\mathscr{S}(\mathscr{CG})$  induced by  $\mathscr{CG}$  and  $\mathscr{Q},$  given structure  $\mathscr{Q}.$ 

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The Language of a Model

Recall: A UML model  $\mathcal{M}=(\mathscr{C}\mathscr{D},\mathscr{SM},\mathscr{O}\mathscr{D})$  and a structure  $\mathscr{D}$  denote a set  $[\![\mathcal{M}]\!]$  of (initial and consecutive) computations of the form

Example: Language of a Model

 $(\sigma_0,\varepsilon_0) \xrightarrow{a_0} (\sigma_1,\varepsilon_1) \xrightarrow{a_1} (\sigma_2,\varepsilon_2) \xrightarrow{a_2} \dots \text{ where }$ 

 $a_i = (cons_i, Snd_i, u_i) \in \underbrace{2^{\mathscr{D}(\mathscr{E})} \times 2^{(\mathscr{D}(\mathscr{E}) \, \cup \, \{*,+\}) \times \mathscr{D}(\mathscr{E})} \times \mathscr{D}(\mathscr{E})}_{}.$ 

For the connection between models and interactions, we disregard the configuration of the ether, and define as follows:  $\frac{1}{2} \int_{-\infty}^{\infty} \frac{1}{2} \left( \frac{1}{2} \int_{-\infty}^{\infty} \frac{1}{2} \int_{-\infty}^{\infty} \frac{1}{2} \left( \frac{1}{2} \int_{-\infty}^{\infty} \frac$ 

Definition. Let  $\mathcal{M} = (\mathscr{CG}_{\mathcal{N}}\mathscr{M}_{i},\mathscr{CG}_{\mathcal{S}})$  be a UML model and  $\mathscr{G}$  a structure. Then  $\mathcal{L}(\mathcal{M}) := \{(G_{i},u_{i},\sigma ms_{i},Snd_{i})_{i}\in G_{i}, \in (\Sigma_{\mathcal{S}}^{\mathcal{G}}\times A)^{\mathcal{G}} \mid \\ \exists \{\varepsilon_{i}\}_{i\in \mathcal{D}_{i}}: \{\sigma_{0},\varepsilon_{0}\} \ \ \underbrace{(\sigma ms_{i})_{i}\otimes d_{i}}_{s_{0}}, \sigma_{i},\varepsilon_{1},\varepsilon_{1},\cdots_{i}\in [\mathcal{M}]\}$ 

 $(\sigma_{t},\varepsilon_{1})\xrightarrow{(cons,Sud)}\cdots\rightarrow(\sigma_{0},\varepsilon_{0})\xrightarrow{(cons_{0},Sud_{0})}(\sigma_{1},\varepsilon_{1})\xrightarrow{(cons_{1}\{(E\cap S)\})}(\sigma_{2},\varepsilon_{2})\xrightarrow{((E),Sud_{0})}(\sigma_{3},\varepsilon_{4})$ 

 $\mathcal{L}(\mathcal{M}) := \{(\sigma_i, u_i, \, \mathit{cons}_i, \mathit{Snd}_i)_{i \in \mathbb{N}_0} \mid \exists \, (\varepsilon_i)_{i \in \mathbb{N}_0} : (\sigma_0, \varepsilon_0) \xrightarrow[u_0]{(\mathit{cons}_0, \mathit{Snd}_0)} (\sigma_1, \varepsilon_1) \cdots \in \llbracket \mathcal{M} \rrbracket \}$ 

is the language of M.

# Satisfaction of Signal and Attribute Expressions

Satisfaction of Signal and Attribute Expressions

• Let  $(\sigma, u, cons, Snd) \in \Sigma_{\mathcal{S}}^{\mathcal{S}} \times A$  be a tuple consisting of system state, object identity, consume set, and send set Let  $\beta: X \to \mathcal{S}(\mathcal{C})$  be a valuation of the logical variables.

- Let  $(\sigma, u, cons, Snd) \in \Sigma_{\mathcal{S}}^0 \times A$  be a tuple consisting of system state, object identity, consume set, and send set, Let  $\beta: X \to \mathscr{D}(\mathcal{C})$  be a valuation of the logical variables.

- (σ, u, cons, Snd) |=<sub>β</sub> true
- $(\sigma, u, cons, Snd) \models_{\beta} \psi$  if and only if  $I[\psi](\sigma, \beta) = 1$
- $\bullet \ \ (\sigma, u, cons, Snd) \models_{\beta} \neg \psi \text{ if and only if not } (\sigma, cons, Snd) \models_{\beta} \psi$
- $\bullet \ \ (\sigma,u,\varpi ns,Snd)\models_{\beta}\psi_{1}\vee\psi_{2} \text{ if and only if } (\sigma,u,\varpi ns,Snd)\models_{\beta}\psi_{1} \text{ or } (\sigma,u,cons,Snd)\models_{\beta}\psi_{2}$
- $\bullet \ \, (\sigma,u,\varpi ns,Snd)\models_{\beta} E^{1}_{x,y} \text{ if and only if } \beta(x)=u \wedge \exists \, e \in \mathscr{D}(E) \bullet (e,\beta(y)) \in Snd$  $\bullet \ \ (\sigma,u,\infty ns\,,Snd\,) \models_{\beta} E^?_{x,y} \text{ if and only if } \beta(y) = u \wedge \infty ns \subset \mathscr{D}(E)$

 $\bullet \ \, (\sigma,u,cons\,,Snd) \models_{\beta} E^{?}_{x,y} \text{ if and only if } \beta(y) = u \wedge cons \subset \mathscr{D}(E)$  $\bullet \ \ (\sigma,u,cons,Snd) \models_{\beta} E^{1}_{x,y} \text{ if and only if } \beta(x) = u \land \exists e \in \mathscr{D}(E) \bullet (e,\beta(y)) \in Snd$   $\bullet \ \, (\sigma,u,cons,Snd) \models_{\beta} \psi_1 \lor \psi_2 \text{ if and only if } (\sigma,u,cons,Snd) \models_{\beta} \psi_1 \text{ or } (\sigma,u,cons,Snd) \models_{\beta} \psi_2$ 

 $\bullet \ \ (\sigma,u,cons,Snd) \models_{\beta} \neg \psi \text{ if and only if not } (\sigma,\infty ns,Snd) \models_{\beta} \psi$ •  $(\sigma, u, cons, Snd) \mid =_{\beta} \psi$  if and only if  $I[\![\psi]\!](\sigma, \beta) = 1$  •  $(\sigma, u, cons, Snd) \models_{\beta} true$ 

Observation: we don't use all information from the computation path.

We could, e.g., also keep track of event identities between send and receive.

# Example: Model Language and Signal / Attribute Expresions

•  $\beta = \{x \mapsto c_1, y \mapsto c_2, z \mapsto c_3\}$ 

 $(\sigma_{\ell}, \varepsilon) \xrightarrow{(\operatorname{cons}, \operatorname{Sud})} \cdots \to (\sigma_{\ell}, \varepsilon_{\ell}) \xrightarrow{(\operatorname{cons}, \operatorname{Sud})} (\sigma_{\ell}, \varepsilon_{\ell}) \xrightarrow{(\operatorname{cons}, \operatorname{Sud})} (\sigma_{\ell}, \varepsilon_{\ell}) \xrightarrow{(\varepsilon_{\ell}, \varepsilon_{\ell})} (\sigma_{\ell}, \varepsilon_{\ell}) \xrightarrow{(\varepsilon_{\ell}, \varepsilon_{\ell})} (\sigma_{\ell}, \varepsilon_{\ell}) \xrightarrow{\varepsilon_{\ell}} (\sigma_{\ell}, \varepsilon_{\ell}) \xrightarrow{\varepsilon_{\ell}$ 

- $(\sigma_0, u_0, cons_0, Snd_0) \models_{\beta} y.k > 0$
- $(\sigma_0, u_0, cons_0, Snd_0) \models_{\beta} x.k > 0$
- $(\sigma_1, c_1, cons_1, \{(: E, c_2)\}) \models_{\beta} E_{x,y}^!$
- $(\sigma_1, c_1, cons_1, \{(: E, c_2)\}) \models_{\beta} F_{x,y}^!$

• We set  $(\sigma_4, c_2, cons_4, \{G(), c_1\}) \models_{\beta} G_{y,x}! \land G_{y,x}?$  (triggered operation or method call). •  $\cdots \models_{\beta} E_{x,y}^{?}$ 

## TBA over Signature

TBA Construction Principle

Recall: The TBA  $B(\mathcal{F})$  of LSC  $\mathcal{F}$  is  $(Expr_{\mathcal{F}}(X), X, Q, q_{mn}, \rightarrow, Q_{\mathcal{F}})$  with \* Q is the set of cota of  $\mathcal{F}_{*}$  q<sub>m</sub> is the instance heads out. \*  $Expr_{\mathcal{F}} = \Phi \cup \Phi_{\mathbb{F}}(X)$ , \*  $\rightarrow$  consists of loops, propositional form,  $p_{\mathbb{F}}$  and  $|\mathbf{r}_{\mathbb{F}}|$  entitle (odd conduction). \*  $\mathcal{F} = \{C \in Q \mid \Theta(C) = \operatorname{cold} V C = L\}$  is the set of cold outs.

So in the following, we "only" need to construct the transitions' labels:

 $\rightarrow = \{(q,\psi_{loop}(q),q) \mid q \in Q\} \cup \{(q,\psi_{prog}(q,q'),q') \mid q \leadsto_{P} q'\} \cup \{(q,\psi_{art}(q),L) \mid q \in Q\}$ 

## Definition. ATBA

 $\mathcal{B} = (Expr_{\mathcal{B}}(X), X, Q, q_{ini}, \rightarrow, Q_F)$ 

where  $Expr_{\mathcal{B}}(X)$  is the set of signal and attribute expressions  $Expr_{\mathscr{S}}(\mathscr{E},X)$  over signature  $\mathscr{S}$  is called TBA over  $\mathscr{S}$ .

## Full LSCs

Course Map

(CD, SM)

→ (CD,

G = (N, E, J) Mathematics TWN ao

 $w_{\pi} = ((\sigma_i, cons_i, Snd_i))_{i \in \mathbb{N}}$ 

- A full LSC  $\mathscr{L}=(((L,\preceq,\sim),I.$  Mag, Cond, Lodiny,  $\Theta),ac_0,am,\Theta_{\mathscr{L}})$  consists of body  $((L,\preceq,\sim),I.$  Mag, Cond, Lodiny,  $\Theta)$ , and the substantial condition and E for G and G and G and G and G and G and G are alternating and if false  $\mathscr{L}$  is called permissive) and abstract mode one classified G (First Linearity) and the condition mode one of First Linearity G and G are conditional G and G and G are conditional G

Live Sequence Charts — Semantics Cont'd

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## Full LSCs

- A full LSC  $\mathscr{L}=(((L,\preceq,\sim),\mathcal{I},\operatorname{Mag},\operatorname{Cond},\operatorname{Lodiny},\Theta),ac_0,am_0\Theta_{\mathscr{L}})$  consists of a body  $((L,\preceq,\sim),\mathcal{I},\operatorname{Mag},\operatorname{Cond},\operatorname{Lodiny},\Theta)$ , a carbon condition one (Extry  $\omega$ ), a satisfactor condition one (Extry  $\omega$ ) as attitudes flag arcd (if face,  $\mathscr{L}$  is all of jerminaria) a station mode one (Extry  $\omega$ ).



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## Full LSCs

Full LSC Semantics: Example

- $\begin{array}{ll} \textbf{Aful LSC}\,\mathcal{L}' = (((L_i,\preceq_i,\sim_i),\mathbb{Z},\,\text{Mag},\,\text{Cord},\,\text{LocInv},\,\Theta),\,ac_0,\,am,\,\Theta_{\mathcal{L}'})\,\,\text{consists of} \\ \textbf{a body}\,\,((L_i,\preceq_i,\sim_i),\mathbb{Z},\,\text{Mag},\,\text{Cord},\,\text{LocInv},\,\Theta),\\ \textbf{a activation condition so, of <math>Exp_{\mathcal{L}'},\,\\ \textbf{a strices files artist}\,\,(\text{if}\,das,\,\mathcal{L}'\text{is called permissive})\\ \textbf{a strices files artist}\,\,(\text{if}\,das,\,\mathcal{L}'\text{is called permissive})\\ \textbf{a chart mode activation}\,\,(\text{if}\,das,\,\mathcal{L}'\text{is called permissive})\\ \textbf{a chart mode permissive})\\ \textbf{a chart mode activation}\,\,(\text{if}\,das,\,\mathcal{L}'\text{is called permissive})\\ \textbf{a chart$



A set of words  $W\subseteq (Expr_B\to \mathbb{B})^\omega$  is accepted by  $\mathscr L$  if and only if

	cold	$\Theta_{\mathscr{L}}$
$\forall w \in W \bullet w^0 \models ac \land \neg w \rightarrow (C_{\alpha})$	$\exists w \in W \bullet w^0 \models ac \land \neg \psi_{crit}(C_0)$ $\land w^0 \models \psi_{prog}(\emptyset, C_0) \land w/1 \in \mathcal{L}(\mathcal{B}(\mathcal{L}))$	am = intal
$\forall w \in W \forall k \in \mathbb{N} \land w^k \models ac \land \neg \psi \rightarrow (G)$	$\exists w \in W \exists k \in \mathbb{N}_0 \bullet w^k \models ac \land \neg \psi_{ext}(C_0)$ $\land w^k \models \psi_{prog}(\emptyset, C_0) \land w/k + 1 \in \mathcal{L}(\mathcal{B}(\mathscr{L}))$	am = invariant

where  $C_0$  is the minimal (or instance heads) cut.

 $(\sigma,\varepsilon)\xrightarrow{(cons,Sud)}\cdots\rightarrow (\sigma_0,\varepsilon_0)\xrightarrow{(cons_0,Sud_0)}(\sigma_{1},\varepsilon_1)\xrightarrow{(cons_1,((C_0,c_0)))}(\sigma_{2},\varepsilon_2)\xrightarrow{(c_1,\varepsilon_1)}(\sigma_{2},\varepsilon_2)\xrightarrow{(c_2,\varepsilon_2)}((\varepsilon_1,\varepsilon_2)\xrightarrow{(c_2,\varepsilon_2)}(\sigma_{3},\varepsilon_1)\rightarrow\cdots$ 

bot  $\Rightarrow w^0 \models \psi_{proy}(\emptyset, C_0) \land w/1 \in \mathcal{L}(\mathcal{B}(\mathcal{L})) \Rightarrow w^k \models \psi_{proy}^k(\emptyset, C_0) \land w/k + 1 \in \mathcal{L}(\mathcal{B}(\mathcal{L}))$ 

Existential LSC Example: Buy A Softdrink

Note: Activation Condition

LSC: buy softdrink
AC: true
AM: invariant I: permissive
User
User
Vend. M SOFT

Avi: initial t permissive  $C_1$   $C_2$   $C_3$ 

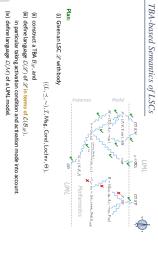
STUDENTERWERK OLDENBURG

Existential LSC Example: Get Change



pSOFT





Live Sequence Charts — Precharts

$$\begin{split} & \textbf{A full LSC} \,\, \mathscr{L} = (PC, MC, ae_0, am, \Theta_{\mathscr{L}}) \,\, \textbf{actually consist of} \\ & \bullet \,\, \textbf{pre-chart} \, PC = ((L_P, \preceq_P, \sim_P), I_P, \mathscr{S}, \mathsf{Msg}_P, \mathsf{Cond}_P, \mathsf{LocInv}_P, \Theta_P) \, \text{(possibly empty)}. \end{split}$$

 $\mathbf{main\text{-}chart}\ MC = ((L_M, \preceq_M, \sim_M), \mathcal{I}_M, \mathscr{S}, \mathsf{Msg}_M, \mathsf{Cond}_M, \mathsf{LocInv}_M, \Theta_M) \ (\mathsf{non\text{-}empty}).$ 

activation condition  $ac_0:Bool\in Expr_{\mathscr{S}},$  strictness flag strict (otherwise called permissive) activation mode on  $\in$  (initial, invariant), chart mode existential  $(\Theta_{\mathscr{L}}=\operatorname{cold})$  or universal  $(\Theta_{\mathscr{L}}=\operatorname{hot})$ .

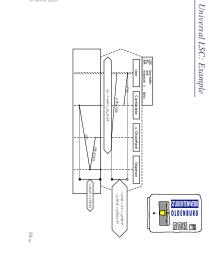
Pre-Charts

 $\bullet \ \, \text{Then } \mathcal{M} \models \mathscr{L} \text{ (universal) if and only if } \mathcal{L}(\mathcal{M}) \subseteq \mathcal{L}(\mathscr{L}).$  And  $\mathcal{M} \models \mathscr{L} \text{ (existential) if and only if } \mathcal{L}(\mathcal{M}) \cap \mathcal{L}(\mathscr{L}) \neq \emptyset.$ 

Universal LSC: Example

Pre-Charts Semantics

Universal LSC: Example STUDENTERWERK OLDENBURG



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Forbidden Scenario Example: Don't Give Two Drin!

STUDENTERWEEK OLDENBURG

Forbidden Scenario Example: Don't Give Two Drin'

- STUDENTERWEEK OLDENBURG

Note: Sequence Diagrams and (Acceptance) Test



- Existential LSGs\* may hint at test-cases for the acceptance test!
  (+: as well as (positive) scenarios in general. like use-cases)
- (Because they require that the software  $\frac{1}{2}$  never exhibits the unwanted behaviour.) Universal LSCs (and negative/anti-scenarios) in general need exhaustive analysis!

(\*: as well as (positive) scenarios in general, like use-cases)

Note: Sequence Diagrams and (Acceptance) Test

Note: Sequence Diagrams and (Acceptance) Test

Existential LSCs\* may hint at test-cases for the acceptance test!

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Universal LSCs (and negative/anti-scenarios) in general need exhaustive analysis!

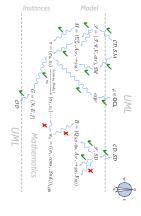
61/66

Existential LSCs\* may hint at test-cases for the acceptance test!
 (\*: as well as (positive) scenarios in general, like use-cases)

## TBA-based Semantics of LSCs (ii) constant a TBA $E_{\mathcal{S}_n}$ and (iii) define language $\mathcal{L}(\mathcal{S})$ of $\mathcal{L}$ in terms of $\mathcal{L}(E_{\mathcal{S}})$ , in particular taking activation condition and activation mode into account. (iv) define language $\mathcal{L}(\mathcal{M})$ of a UML model. (i) Given an LSC ℒ with body $((L, \preceq, \sim), \mathcal{I}, \mathsf{Msg}, \mathsf{Cond}, \mathsf{LocInv}, \Theta),$

References

## Course Map



• Then  $\mathcal{M} \models \mathscr{L}$  (universal) if and only if  $\mathcal{L}(\mathcal{M}) \subseteq \mathcal{L}(\mathscr{L})$ . And  $\mathcal{M} \models \mathscr{L}$  (existential) if and only if  $\mathcal{L}(\mathcal{M}) \cap \mathcal{L}(\mathscr{L}) \neq \emptyset$ .

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# Tell Them What You've Told Them...

- Büchi automata accept infinite words
- if there exists is a run over the word,
   which visits an accepting state infinitely often.
- The language of a model is just a rewriting of computations into words over an alphabet.
- An LSC accepts a word (of a model) if
- Existential: at least on word (of the model) is accepted by the constructed TBA. Universion: all words (of the model) are accepted.
- Activation mode initial activates at system startup (only).
   invariant with each satisfied activation condition (or pre-chart).
- Pre-charts can be used to state forbidden scenarios.

Sequence Diagrams can be useful for testing.