# Real-Time Systems Lecture 11: Timed Automata

2017-12-07

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# Content

- Timed Automata Syntax
- • Channels, Actions, Clock Constraints
- • Pure Timed Automaton
- Graphical Representation of TA
- Timed Automata (Operational) Semantics
- -- Clock Valuations, Time Shift, Modification
- The Labelled Transition System
  - Configurations
  - Delay transitions
- └ Action transitions
- Transition Sequences, Reachability
- Computation Paths
- Timelocks and Zeno behaviour
- L₀ Runs

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(Pure) Timed Automata Syntax

# Channel Names and Actions

To define timed automata formally, we need the following sets of symbols:

- A set  $(a, b \in)$  Chan of channel names or channels.
- For each channel a ∈ Chan, two visible actions:
   a? and a! denote input and output on the channel (a?, a! ∉ Chan).
- $\tau \notin$  Chan represents an internal action, not visible from outside.
- $(\alpha, \beta \in) Act := \{a? \mid a \in Chan\} \cup \{a! \mid a \in Chan\} \cup \{\tau\}$  is the set of actions.
- An alphabet B is a set of channels, i.e.  $B \subseteq$  Chan.
- For each alphabet B, we define the corresponding action set

$$B_{?!} := \{a? \mid a \in B\} \cup \{a! \mid a \in B\} \cup \{\tau\}.$$

• Note:  $Chan_{?!} = Act$ .

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## Example: Desktop Lamp

- $B = \{press\}$  alphabet of the desktop lamp model
- channel 'press' models the single button of the desktop lamp
- Output: press! ("send a message onto channel press")

models "the button is pressed"

- Input: *press*? ("receive a message from channel *press*")
  - models "button pressed is recognised"
- Actions:

$$\{press!, press?, \tau\} = B_{!?}$$

# Simple Clock Constraints

- Let  $(x, y \in) X$  be a set of clock variables (or clocks).
- The set  $(\varphi \in) \Phi(X)$  of (simple) clock constraints (over X) is defined by the following grammar:

```
\varphi ::= x \sim c \mid x - y \sim c \mid \varphi_1 \land \varphi_2
```

where

- $x, y \in X$ ,
- $c\in \mathbb{Q}_0^+$  , and
- $\sim \in \{<,>,\leq,\geq\}.$
- Clock constraints of the form  $x y \sim c$  are called difference constraints.

```
Examples: Let X = \{x, y\}.
```

- $x \le 3, x > 3$  (strictly speaking not a clock constraint:  $3 \ge x$ )
- y < 2, y > 3

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x ≤ 3 ∕

## Timed Automaton

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Definition 4.3. [*Timed automaton*] A (pure) timed automaton  $\mathcal{A}$  is a structure  $\mathcal{A} = (L, B, X, I, E, \ell_{ini})$ where •  $(\ell \in) L$  is a finite set of locations (or control states), •  $B \subseteq$  Chan is an alphabet, • X is a finite set of clocks, •  $I : L \rightarrow \Phi(X)$  assigns to each location a clock constraint, its invariant, •  $E \subseteq L \times B_{?!} \times \Phi(X) \times 2^{X} \times L$  a finite set of directed edges. Edges  $(\ell, \alpha, \varphi, Y, \ell')$  from location  $\ell$  to  $\ell'$  are labelled with an action  $\alpha$ , a guard  $\varphi$ , and a set Y of clocks that will be reset. •  $\ell_{ini}$  is the initial location.

 $\begin{aligned} \mathcal{A} &= (L,B,X,I,E,\ell_{ini}) \\ \bullet \ I: L \to \Phi(X), \\ \bullet \ E \subseteq L \times B_{?!} \times \Phi(X) \times 2^X \times L \end{aligned}$ 

- Locations:  $L = \{off, light, bright\}$
- Alphabet:  $B = \{press\}$ ,
- **Clocks**:  $X = \{x\}$ ,

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- Invariants:  $I = \{ off \mapsto true, light \mapsto true, bright \mapsto true \}$
- Edges:  $E = \{$  (off, press?, true,  $\{x\}$ , light), (light, press?,  $x > 3, \emptyset, \text{off}$ ), (light, press?,  $x \le 3, \emptyset, \text{bright}$ ), (bright, press?, true,  $\emptyset, \text{off}$ ) $\}$
- Initial Location:  $\ell_{ini} = off$

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Graphical Representation of Timed Automata

$$\mathcal{A} = (L, B, X, I, E, \ell_{ini})$$
  
•  $I : L \to \Phi(X)$   
•  $E \subseteq L \times B_{?!} \times \Phi(X) \times 2^X \times L$ 

• Locations (control states)  $\ell$  and their invariants  $I(\ell)$ :









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- Locations: L = {off, light, bright}
  Alphabet: B = {press},
- **Clocks**:  $X = \{x\}$ ,
- Invariants:  $I = \{ off \mapsto true, light \mapsto true, bright \mapsto true \}$
- Edges: 
  $$\begin{split} \textbf{E} &= \{ \hspace{0.1cm} (\textit{off},\textit{press?},\textit{true},\{x\},\textit{light}),(\textit{light},\textit{press?},x>3,\emptyset,\textit{off}),\\ &(\textit{light},\textit{press?},x\leq3,\emptyset,\textit{bright}),(\textit{bright},\textit{press?},\textit{true},\emptyset,\textit{off}) \} \end{split}$$
- Initial Location:  $\ell_{ini} = off$



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• Locations:  $L = \{ off, light, bright \}$ • Alphabet:  $B = \{ press \}$ , • Clocks:  $X = \{x\}$ , • Invariants:  $I = \{ off \mapsto true, light \mapsto true, bright \mapsto true \}$ • Edges:  $E = \{ (off, press?, true, \{x\}, light), (light, press?, x > 3, \emptyset, off), (light, press?, x \le 3, \emptyset, bright), (bright, press?, true, \emptyset, off) \}$ 

• Initial Location:  $\ell_{ini} = off$ 



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### Example

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- Locations:  $L = \{off, light, bright\}$
- Alphabet:  $B = \{press\},\$
- **Clocks**:  $X = \{x\}$ ,
- Invariants:  $I = \{ off \mapsto true, light \mapsto true, bright \mapsto true \}$
- Edges:  $E = \{ (off, press?, true, \{x\}, light), (light, press?, x > 3, \emptyset, off), (light, press?, x \le 3, \emptyset, bright), (bright, press?, true, \emptyset, off) \}$
- Initial Location:  $\ell_{ini} = off$



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Locations: L = {off, light, bright}
Alphabet: B = {press},
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Invariants: I = {off → true, light → true, bright → true}
Edges: E = { (off, press?, true, {x}, light), (light, press?, x > 3, Ø, off),

- $(light, press?, x \le 3, \emptyset, bright), (bright, press?, true, \emptyset, off)$
- Initial Location:  $\ell_{ini} = off$



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### Example

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- Locations: L = {off, light, bright}
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- **Clocks**:  $X = \{x\}$ ,
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- Edges:  $E = \{ (off, press?, true, \{x\}, light), (light, press?, x > 3, \emptyset, off), (light, press?, x \le 3, \emptyset, bright), (bright, press?, true, \emptyset, off) \}$
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#### Timed Automata (Operational) Semantics

- Clock Valuations, Time Shift, Modification

#### - The Labelled Transition System

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# Clock Valuations

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• Let X be a set of clocks. A valuation  $\nu$  of clocks in X is a mapping

 $\nu:X\to \mathsf{Time}$ 

assigning each clock  $x \in X$  the current time  $\nu(x)$ .

• Let  $\varphi$  be a clock constraint. The satisfaction relation between clock valuations  $\nu$  and clock constraints  $\varphi$ , denoted by  $\nu \models \varphi$ , is defined inductively:

•  $\nu \models x \sim c$  iff  $\nu(\mathbf{x}) \stackrel{\sim}{\sim} \hat{c}$ •  $\nu \models x - y \sim c$  iff  $\nu(\mathbf{x}) \stackrel{\sim}{\sim} \nu(\mathbf{y}) \stackrel{\sim}{\sim} \hat{c}$ •  $\nu \models \varphi_1 \land \varphi_2$  iff  $\nu \models \varphi_1$  and  $\nu \models \varphi_2$ 

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• Let X be a set of clocks. A valuation  $\nu$  of clocks in X is a mapping

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assigning each clock  $x \in X$  the current time  $\nu(x)$ .

• Let  $\varphi$  be a clock constraint. The satisfaction relation between clock valuations  $\nu$  and clock constraints  $\varphi$ , denoted by  $\nu \models \varphi$ , is defined inductively:

•  $\nu \models x \sim c$  iff  $\nu(x) \sim c$ •  $\nu \models x - y \sim c$  iff  $\nu(x) - \nu(y) \sim c$ •  $\nu \models \varphi_1 \land \varphi_2$  iff  $\nu \models \varphi_1$  and  $\nu \models \varphi_2$ 

• Two clock constraints  $\varphi_1$  and  $\varphi_2$  are called (logically) equivalent if and only if for all clock valuations  $\nu$ , we have

 $\nu \models \varphi_1$  if and only if  $\nu \models \varphi_2$ .

In that case we write  $\models \varphi_1 \iff \varphi_2$ .

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# **Operations on Clock Valuations**

Let  $\nu$  be a valuation of clocks in X and  $t \in$ Time.

Time Shift

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We write  $\nu + t$  to denote the clock valuation (for X) with

$$(\underbrace{\nu+t})(x) = \nu(x) + t.$$

$$\underbrace{\nu: \xi_{\times} \mapsto 3.6\zeta}_{(\nu_{+} 0.27)(\times)} = \underbrace{\nu(x) + 0.27}_{= 3.0 + 0.27} = 3.22$$

for all  $x \in X$ ,

• Modification / Update

Let  $Y \subseteq X$  be a set of clocks. We write<sub>t</sub> $\nu[Y := t]$  to denote the clock valuation with

$$(\nu[Y:=t])(x) = \begin{cases} t & \text{, if } x \in Y \\ \nu(x) & \text{, otherwise} \end{cases}$$

Special case reset: t = 0.

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**Definition 4.4.** The operational semantics of a timed automaton  $\mathcal{A} = (L, B, X, I, E, \ell_{ini})$  is defined by the (labelled) transition system  $\mathcal{T}(\mathcal{A}) = (Conf(\mathcal{A}), \text{Time} \cup B_{?!}, \{\stackrel{\lambda}{\rightarrow} | \lambda \in \text{Time} \cup B_{?!}\}, C_{ini})$ where •  $Conf(\mathcal{A}) = \{\langle \ell, \nu \rangle | \ell \in L, \nu : X \to \text{Time}, \nu \models I(\ell)\}$ • Time  $\cup B_{?!}$  are the transition labels. • there are delay transition relations  $\langle \ell, \nu \rangle \stackrel{\lambda}{\rightarrow} \langle \ell', \nu' \rangle, \quad \lambda \in \text{Time} \quad (\to \text{ in a minute})$ and action transition relations  $\langle \ell, \nu \rangle \stackrel{\lambda}{\rightarrow} \langle \ell', \nu' \rangle, \quad \lambda \in B_{?!}. \quad (\to \text{ in a minute})$ •  $C_{ini} = \{\langle \ell_{ini}, \nu_0 \rangle\} \cap Conf(\mathcal{A})$  with  $\nu_0(x) = 0$  for all  $x \in X$ is the set of initial configurations.

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Operational Semantics of TA Cont'd

 $\mathcal{A} = (L, B, X, I, E, \ell_{ini})$  $\mathcal{T}(\mathcal{A}) = (Conf(\mathcal{A}), \mathsf{Time} \cup B_{?!}, \{\stackrel{\lambda}{\rightarrow} \mid \lambda \in \mathsf{Time} \cup B_{?!}\}, C_{ini})$ 

• Time or delay transition:

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 $\left( \langle \ell, \nu \rangle, \langle \ell, \nu + \ell \rangle \right) \in \xrightarrow{\ell}$  $\left\langle \ell, \nu \right\rangle \xrightarrow{t} \left\langle \ell, \nu + t \right\rangle$ 

 $\text{ if and only if } \forall \, t' \in [0,t] : \underbrace{\nu+t'}_{} \models I(\ell).$ 

"Some time  $t \in \text{Time}$  elapses respecting invariants, location unchanged."

• Action or discrete transition:  $\begin{array}{c}
\langle \ell, \nu \rangle \xrightarrow{\alpha} \langle \ell', \nu' \rangle \\
\downarrow \\
\text{if and only if there is } (\ell, \alpha, \varphi, Y, \ell') \in E \text{ such that} \\
\nu \models \varphi, \quad \nu' = \nu[Y := 0], \quad \text{and } \nu' \models I(\ell').
\end{array}$ 

"An action occurs, location may change, some clocks may be reset, time does not elapse."



• Configurations:

 $Conf(\mathcal{A}) = \{ \langle \textit{off}, \nu \rangle, \langle \textit{light}, \nu \rangle, \langle \textit{light}, \nu \rangle \mid \nu : X \rightarrow \mathsf{Time} \}$ 

• Initial Configurations:

$$\{\langle \mathbf{off}, \nu_0 \rangle\} \cap Conf(\mathcal{A}) = \{\langle \mathsf{off}, \forall x \mapsto 0 \rangle \}$$

• Delay Transition:

$$\langle \text{off}, \{x \mapsto 0\} \rangle \xrightarrow{27} \langle \text{off}, \{x \mapsto 27\} \rangle$$

• Action Transition:

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$$\langle \mathsf{off}, \{x \mapsto 27\} \rangle \xrightarrow{press?} \langle \mathsf{light}, \{x \mapsto 0\} \rangle \checkmark$$

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# **Transition Sequences**

• A transition sequence of  $\mathcal{A}$  is any finite or infinite sequence of the form

$$\langle \ell_0, \nu_0 \rangle \xrightarrow{\lambda_1} \langle \ell_1, \nu_1 \rangle \xrightarrow{\lambda_2} \langle \ell_2, \nu_2 \rangle \xrightarrow{\lambda_3} \dots$$

with

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• 
$$\langle \ell_0, \nu_0 \rangle \in C_{ini}$$
,

• for all  $i \in \mathbb{N}$ , there is  $\xrightarrow{\lambda_{i+1}}$  in  $\mathcal{T}(\mathcal{A})$  with  $\langle \ell_i, \nu_i \rangle \xrightarrow{\lambda_{i+1}} \langle \ell_{i+1}, \nu_{i+1} \rangle$ 



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# Reachability

 A configuration (*l*, *ν*) is called reachable (in *A*) if and only if there is a transition sequence of the form

$$\langle \ell_0, \nu_0 \rangle \xrightarrow{\lambda_1} \langle \ell_1, \nu_1 \rangle \xrightarrow{\lambda_2} \langle \ell_2, \nu_2 \rangle \xrightarrow{\lambda_3} \dots \xrightarrow{\lambda_n} \langle \ell_n, \nu_n \rangle = \langle \ell, \nu \rangle$$

A location *l* is called reachable if and only if any configuration (*l*, *ν*) is reachable, i.e. there exists a valuation *ν* such that (*l*, *ν*) is reachable.

# Location Invariants

**Recall:** 
$$Conf(\mathcal{A}) = \{ \langle \ell, \nu \rangle \mid \ell \in L, \nu : X \to \text{Time}, \nu \models I(\ell) \}$$

Example:

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$$\begin{array}{c} & \overbrace{\ell_{0} \quad press!} & \overbrace{\ell_{1} \quad press!} & \overbrace{\ell_{2} \quad press!} \\ & y < 2 \end{array} \xrightarrow{(1)} & y := 0 \end{array} \xrightarrow{(1)} & \overbrace{\ell_{2} \quad press!} & \overbrace{\ell_{2} \quad press!} \\ & \overbrace{\ell_{2} \quad r_{2} \quad$$

- $\langle \ell_1, y \mapsto 27 \rangle$  is not a configuration,
- $\langle \ell_0, y \mapsto 0 \rangle \xrightarrow{0.707} \langle \ell_0, y \mapsto 0.707 \rangle \xrightarrow{press!} \langle \ell_1, y \mapsto 0.707 \rangle$  is a transition sequence
- $\langle \ell_0, y \mapsto 0 \rangle \xrightarrow{27} \langle \ell_0, y \mapsto 27 \rangle$  is a transition sequence

• 
$$\langle \ell_0, y \mapsto 0 \rangle \xrightarrow{27} \langle \ell_0, y \mapsto 27 \rangle \xrightarrow{press!} \langle \ell_1, y \mapsto 27 \rangle$$
 is not a transition sequence

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# Two Approaches to Exclude "Bad" Configurations

- The approach taken for TA:
  - Rule out bad configurations in the step from A to T(A).
     "Bad" configurations are not even configurations!
  - Recall Definition 4.4:
    - $Conf(\mathcal{A}) = \{ \langle \ell, \nu \rangle \mid \ell \in L, \nu : X \to \mathsf{Time}, \nu \models I(\ell) \}$
    - $C_{ini} = \{ \langle \ell_{ini}, \nu_0 \rangle \} \cap Conf(\mathcal{A})$

#### • The approach not taken for TA:

• consider every  $\langle \ell, \nu \rangle$  to be a configuration, i.e. have

• "bad" configurations not in transition relation with others, i.e. have, e.g.,

$$\langle \ell, \nu \rangle \xrightarrow{t} \langle \ell, \nu + t \rangle$$

if and only if  $\forall t' \in [0, t] : \nu + t' \models I(\ell)$  and  $\nu + t' \models I(\ell')$ .

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Computation Path, Run

- $\langle \ell, \nu \rangle, t$  is called time-stamped configuration
- Time-stamped delay transition:

$$\langle \ell, \nu \rangle, t \xrightarrow{t'} \langle \ell, \nu + t' \rangle, t + t' \quad \text{iff } t' \in \text{Time and } \langle \ell, \nu \rangle \xrightarrow{t'} \langle \ell, \nu + t' \rangle.$$

• Time-stamped action transition:

$$\langle \ell, \nu \rangle, t \xrightarrow{\alpha} \langle \ell', \nu' \rangle, t \quad \text{iff } \alpha \in B_{?!} \text{ and } \langle \ell, \nu \rangle \xrightarrow{\alpha} \langle \ell', \nu' \rangle$$

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# Computation Paths

• A sequence of time-stamped configurations

$$\xi = \langle \ell_0, \nu_0 \rangle, t_0 \xrightarrow{\lambda_1} \langle \ell_1, \nu_1 \rangle, t_1 \xrightarrow{\lambda_2} \langle \ell_2, \nu_2 \rangle, t_2 \xrightarrow{\lambda_3} \dots$$

is called

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• computation path (or path) of A

• starting in  $\langle \ell_0, \nu_0 \rangle, t_0$ 

if and only if it is <u>either infinite or maximally finite</u> (wrt. the time stamped transition relations).

- A computation path (or path) of  $\mathcal{A}$  is a computation path
  - starting in  $\langle \ell_0, \nu_0 \rangle, 0$
  - with  $\langle \ell_0, \nu_0 \rangle \in C_{ini}$ .

Timelocks and Zeno Behaviour



a?

- Configuration  $\langle \ell, \nu \rangle$  is called **timelock** iff no delay transitions with t > 0 from  $\langle \ell, \nu \rangle$ Examples:

  - $\langle \ell, x = 0 \rangle, 0 \xrightarrow{2} \langle \ell, x = 2 \rangle, 2$   $\langle \ell', x = 0 \rangle, 0 \xrightarrow{3} \langle \ell', x = 3 \rangle, 3 \xrightarrow{a?} \langle \ell', x = 3 \rangle, 3 \xrightarrow{a?} \dots$

• Zeno behaviour:

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- $\langle \ell, x = 0 \rangle, 0 \xrightarrow{\frac{1}{2}} \langle \ell, x = \frac{1}{2} \rangle, \frac{1}{2} \xrightarrow{\frac{1}{4}} \langle \ell, x = \frac{3}{4} \rangle, \frac{3}{4} \dots \xrightarrow{\frac{1}{2^n}} \langle \ell, x = \frac{2^n 1}{2^n} \rangle, \frac{2^n 1}{2^n} \dots$
- $\langle \ell, x = 0 \rangle, 0 \xrightarrow{0.1} \langle \ell, x = 0.1 \rangle, 0.1 \xrightarrow{0.01} \langle \ell, x = 0.11 \rangle, 0.11 \xrightarrow{0.001} \langle \ell, x = 0.111 \rangle, 0.111 \dots$

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**Real-Time Sequence** 

Definition 4.9. An infinite sequence  $t_0, t_1, t_2, \ldots$ of values  $t_i \in \text{Time for } i \in \mathbb{N}_0$  is called real-time sequence if and only if it has the following properties: Monotonicity:  $\forall i \in \mathbb{N}_0 : t_i \le t_{i+1}$ • Non-Zeno behaviour (or unboundedness (or progress)):  $\forall t \in \mathsf{Time} \, \exists \, i \in \mathbb{N}_0 : t < t_i$ 

### Run

Definition 4.10. A run of  $\mathcal{A}$  starting in  $\langle \ell_0, \nu_0 \rangle, t_0$ is an infinite computation path  $\xi = \langle \ell_0, \nu_0 \rangle, t_0 \xrightarrow{\lambda_1} \langle \ell_1, \nu_1 \rangle, t_1 \xrightarrow{\lambda_2} \langle \ell_2, \nu_2 \rangle, t_2 \xrightarrow{\lambda_3} \dots$ of  $\mathcal{A}$  where  $(t_i)_{i \in \mathbb{N}_0}$  is a real-time sequence. We call  $\xi$  a run of  $\mathcal{A}$  if and only if  $\xi$  is a computation path of  $\mathcal{A}$ .

Example:

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- A timed automaton is basically a finite automaton with
  - actions,
  - guards, invariants, and resets of clocks
- The (operational) semantics of TA is a labelled transition system with
  - delay transitions (where locations do not change), and
  - action transitions (where time does not elapse)
- We distinguish
  - Transition Sequences: without timestamps
  - Computation Paths: with timestamps,
  - Runs: timestamps form a real-time sequence.
- The reachability problem is an important decision problem for timed automata.

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References

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# References

Olderog, E.-R. and Dierks, H. (2008). <u>Real-Time Systems - Formal Specification and Automatic Verification</u>. Cambridge University Press.

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