

# *Software Design, Modelling and Analysis in UML*

## *Lecture 07: Class Diagrams II*

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# *Contents & Goals*

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## Last Lectures:

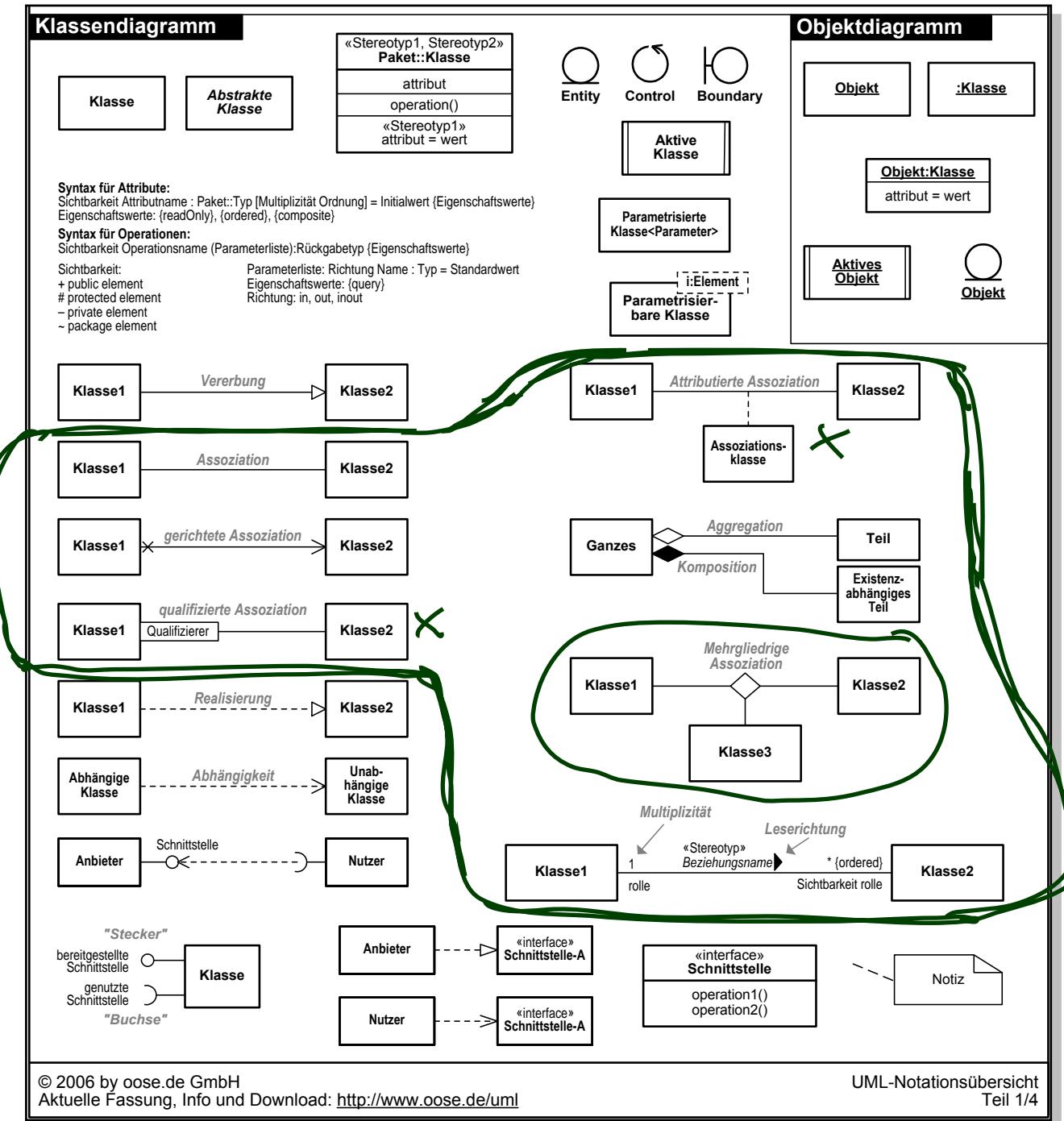
- VL 05: class diagram — except for associations
- VL 06: semantics of visibility within OCL type system

## This Lecture:

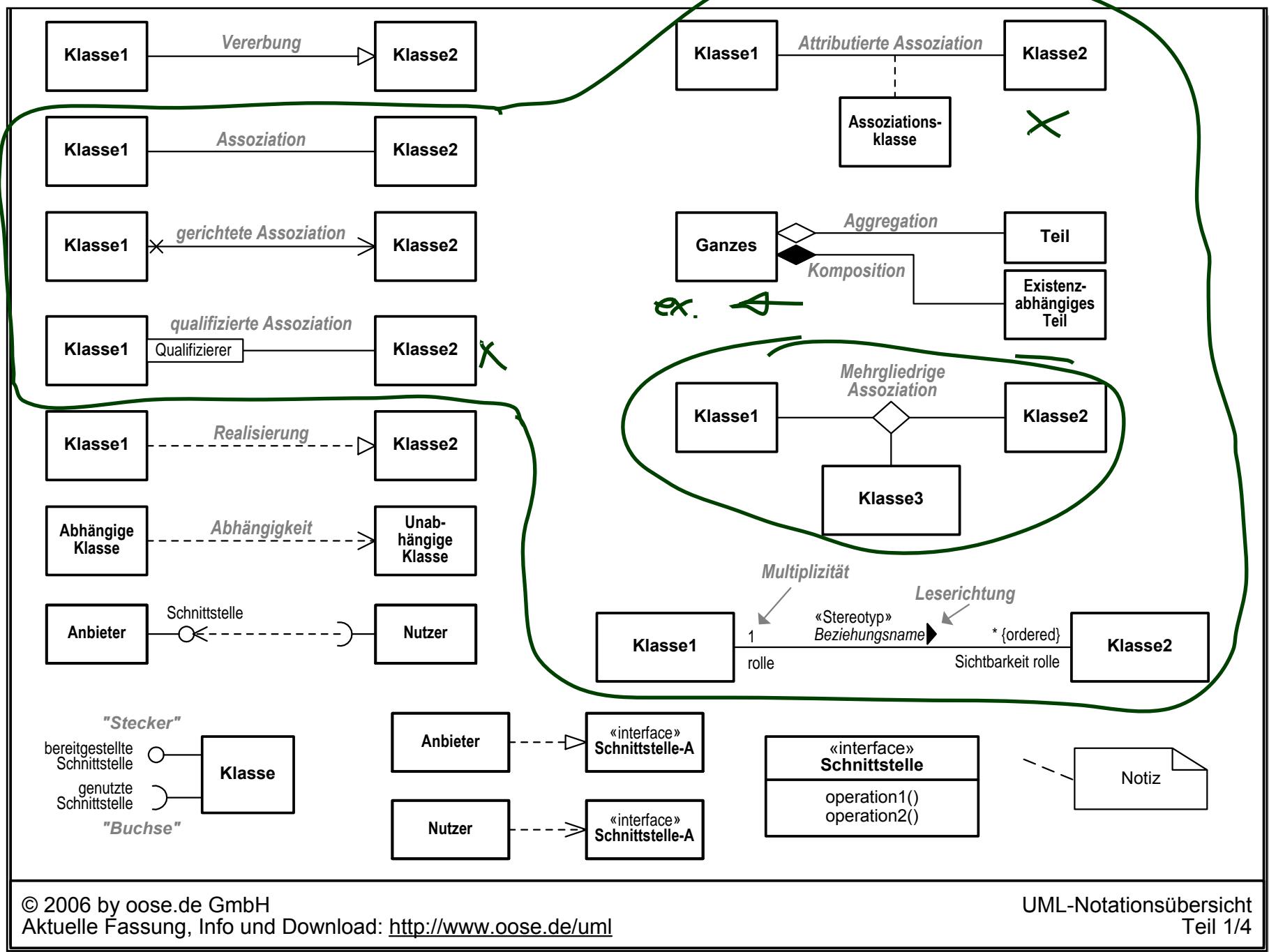
- **Educational Objectives:** Capabilities for following tasks/questions.
  - Please explain this class diagram with associations.
  - Which annotations of an association arrow are semantically relevant?
  - What's a role name? What's it good for?
  - What's “multiplicity”? How did we treat them semantically?
  - What is “reading direction”, “navigability”, “ownership”, . . . ?
  - What's the difference between “aggregation” and “composition” ?
- **Content:**
  - Study concrete syntax for “associations” .
  - (**Temporarily**) extend signature, define mapping from diagram to signature.
  - Study effect on OCL.
  - Where do we put OCL constraints?

## *Associations: Syntax*

# UML Class Diagram Syntax [?]



# UML Class Diagram Syntax [?]



# UML Class Diagram Syntax [?, 61;43]

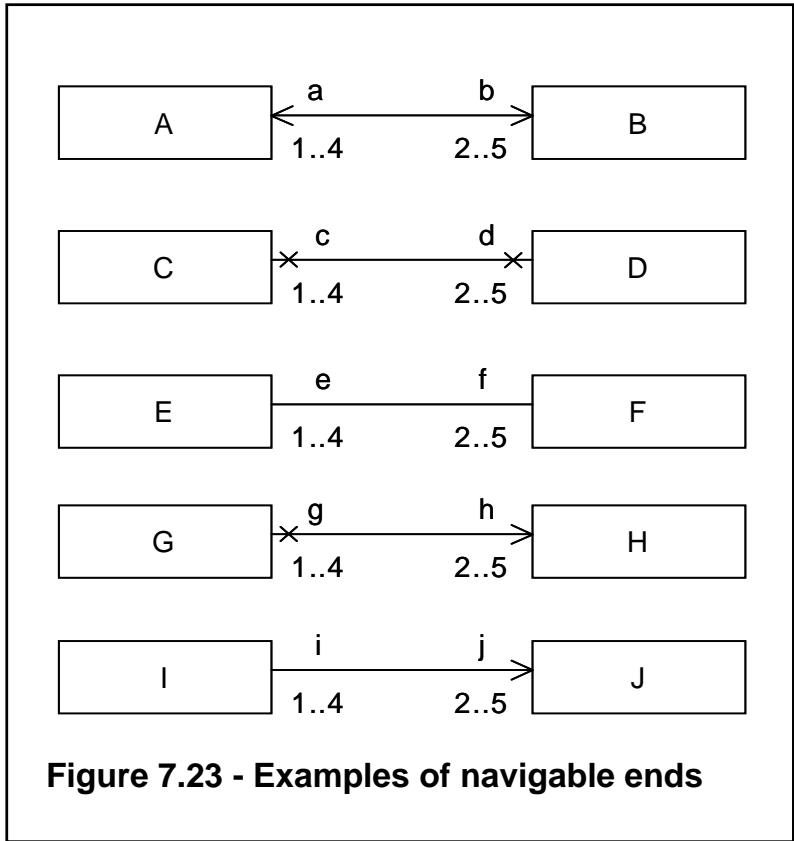
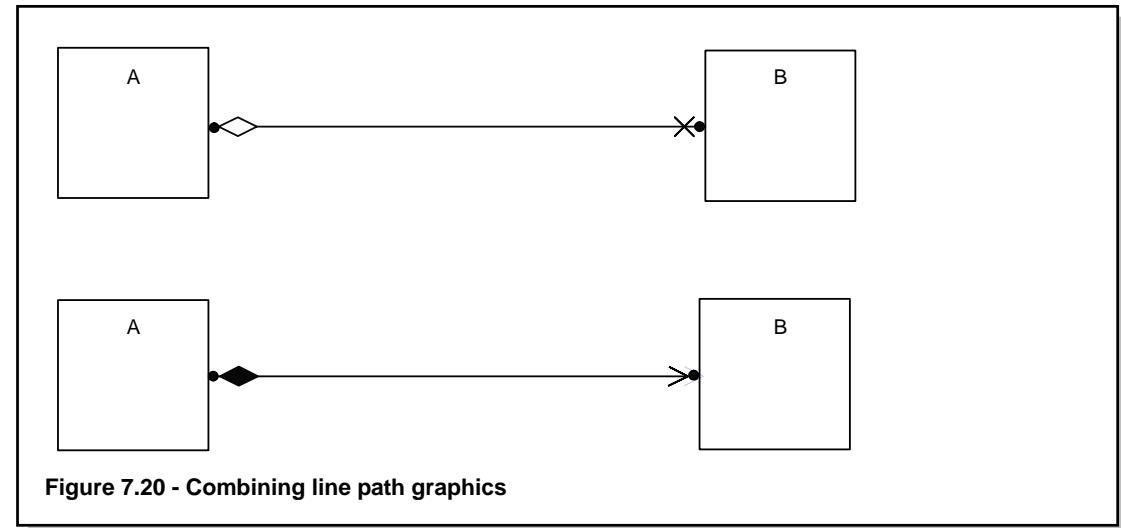
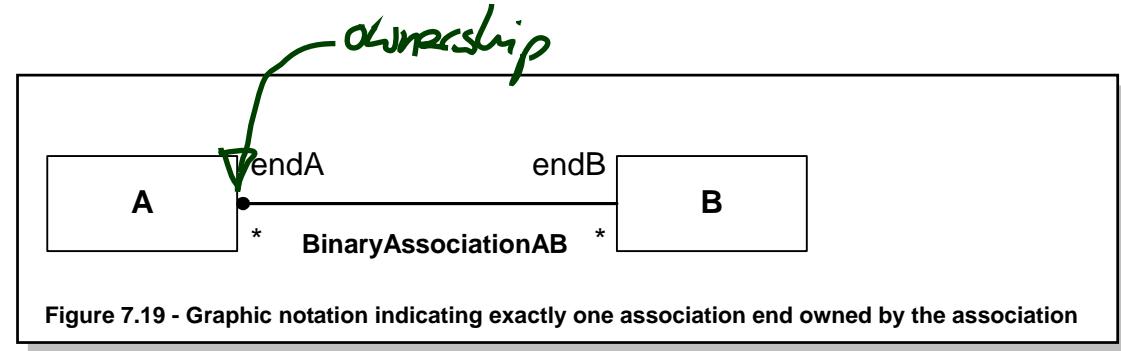


Figure 7.23 - Examples of navigable ends



# What Do We (Have to) Cover?

An **association** has

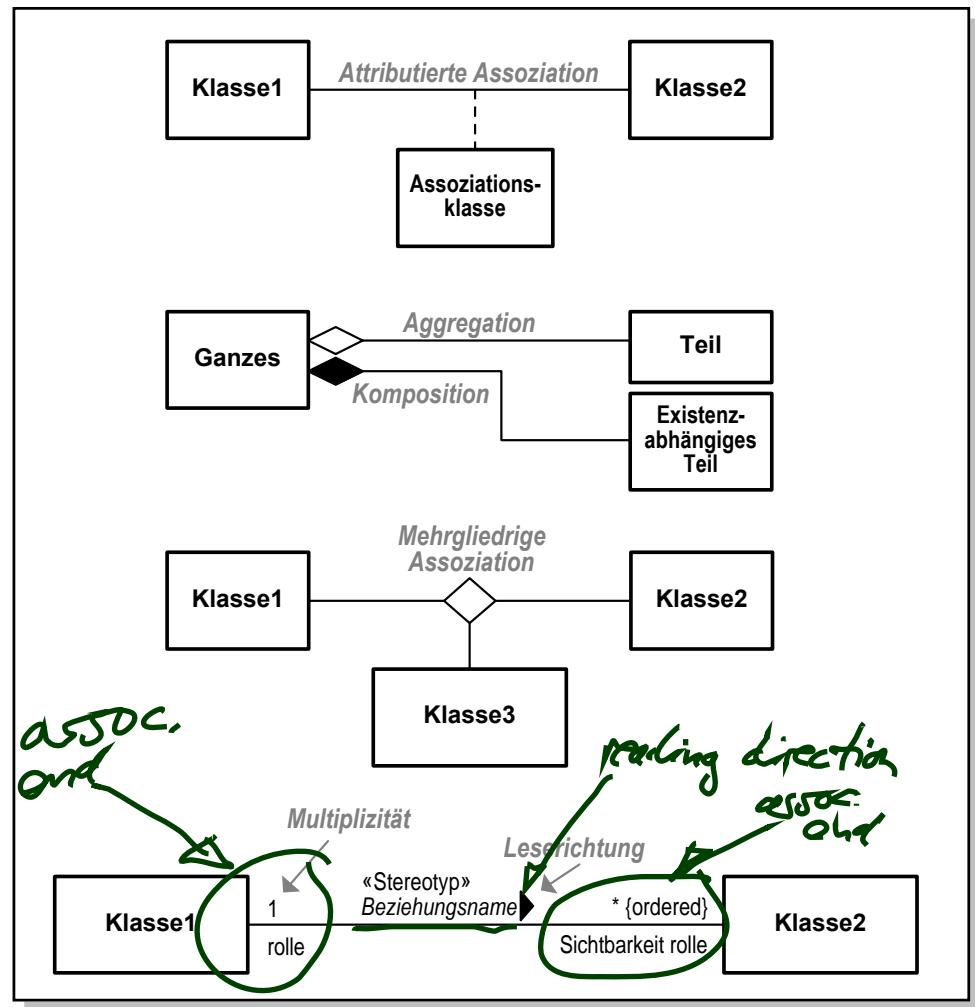
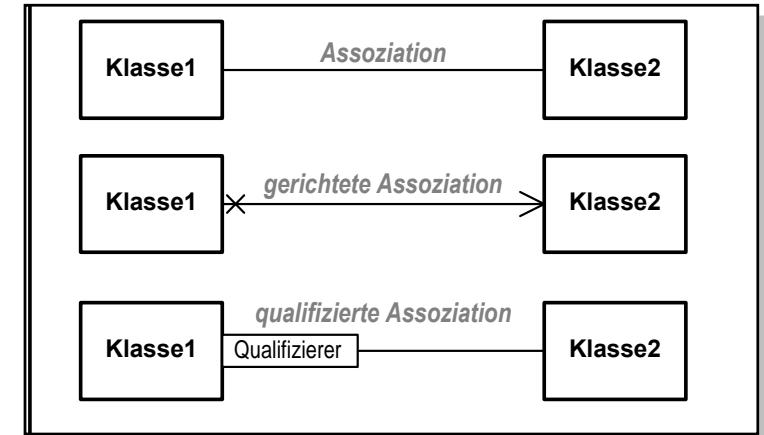
- a **name**,
- a **reading direction**, and
- at least two ends.

(Association)

Each **end** has

- a **role name**,
- a **multiplicity**,
- a set of **properties**,  
such as **unique**, **ordered**, etc.
- a **qualifier**, (we will not treat)
- a **visibility**,
- a **navigability**,
- an **ownership**,
- and possibly a **diamond**. (exercises)

**Wanted:** places in the signature to represent the information from the picture.



# (Temporarily) Extend Signature: Associations

**Only** for the course of Lectures 07/08 we assume that each attribute in  $V$

- **either** is  $\langle v : \tau, \xi, \text{expr}_0, P_v \rangle$  with  $\tau \in \mathcal{T}$  (as before),
- **or** is an **association** of the form

$$\langle r : \langle \text{role}_1 : C_1, \mu_1, P_1, \xi_1, \nu_1, o_1 \rangle \rangle,$$

*association* :

$$\langle \text{role}_n : C_n, \mu_n, P_n, \xi_n, \nu_n, o_n \rangle \rangle \rangle$$

*name*

where

- $n \geq 2$  (at least two ends),
- $r, \text{role}_i$  are just **names**,  $C_i \in \mathcal{C}, 1 \leq i \leq n$ ,
- the **multiplicity**  $\mu_i$  is an expression of the form

$$\mu ::= * \mid N \mid N..M \mid N..* \mid \mu, \mu \quad (N, M \in \mathbb{N})$$

- $P_i$  is a set of **properties** (as before),
- $\xi \in \{+, -, \#, \sim\}$  (as before),
- $\nu_i \in \{\times, -, >\}$  is the **navigability**,
- $o_i \in \mathbb{B}$  is the **ownership**.

# (Temporarily) Extend Signature: Associations

**Only** for the course of Lectures 07/08 we assume that each attribute in  $V$

- **either** is  $\langle v : \tau, \xi, expr_0, P_v \rangle$  with  $\tau \in \mathcal{T}$  (as before),
- **or** is an **association** of the form

$$\langle r : \langle role_1 : C_1, \mu_1, P_1, \xi_1, \nu_1, o_1 \rangle \rangle,$$

**Alternative syntax** for multiplicities:

$$\mu ::= N..M \mid N..* \mid \mu, \mu \quad (N, M \in \mathbb{N} \cup \{*\})$$

and define  $*$  and  $N$  as abbreviations.

**Note:**  $N$  could abbreviate  $0..N$ ,  $1..N$ , or  $N..N$ . We use last one.

- $r, role_i$  are just **names**,  $\cup_i \in \mathcal{C}$ ,  $1 \leq i \leq n$ ,
- the **multiplicity**  $\mu_i$  is an expression of the form

$$\mu ::= * \mid N \mid N..M \mid N..* \mid \mu, \mu \quad (N, M \in \mathbb{N})$$

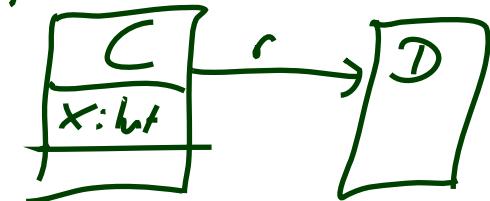
- $P_i$  is a set of **properties** (as before),
- $\xi \in \{+, -, \#, \sim\}$  (as before),
- $\nu_i \in \{\times, -, >\}$  is the **navigability**,
- $o_i \in \mathbb{B}$  is the **ownership**.

# (Temporarily) Extend Signature: Basic Type Attributes

Also only for the course of ~~this~~ lectures 07/08

- we only consider basic type attributes to “belong” to a class  $C$  (to appear in  $atr(C)$ ),
- associations are not “owned” by a particular class (do not appear in  $atr(C)$ ), but live on their own!

QD:



$$atr(C) = \{x, r\}$$



Formally: we only call

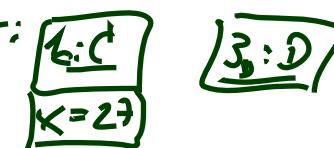
$$(\mathcal{T}, \mathcal{C}, V, atr)$$

a **signature (extended for associations)** if

$$atr : \mathcal{C} \rightarrow 2^{\{v \in V \mid v : \tau, \tau \in \mathcal{T}\}}.$$

basic type

07/08:

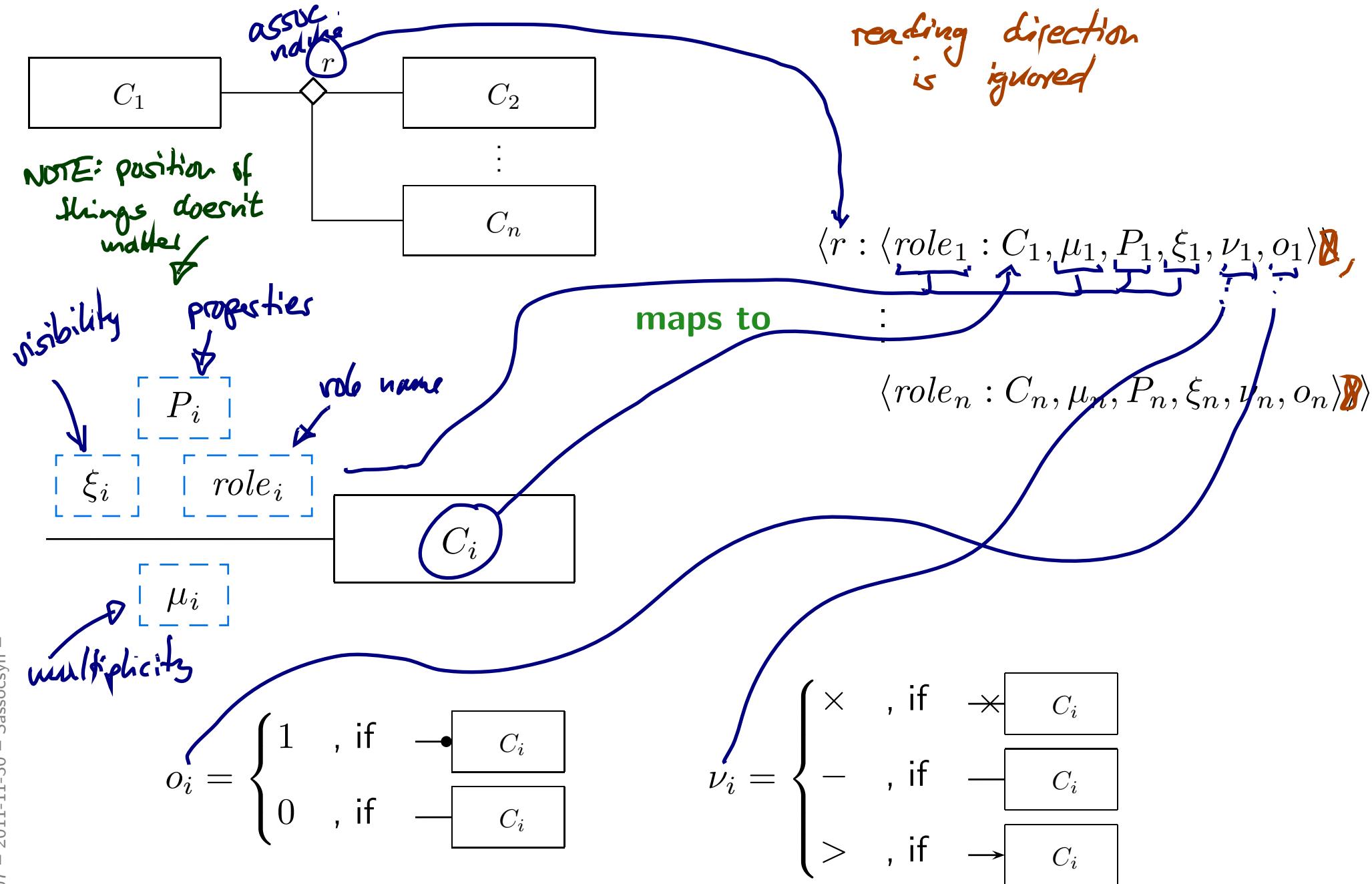


$$r : (x, 3)$$

NOW:  $v = \{ \dots, r : D_{0,1} \}$   
NOT:  $atr(C) = \{ \dots, r, \dots \}$

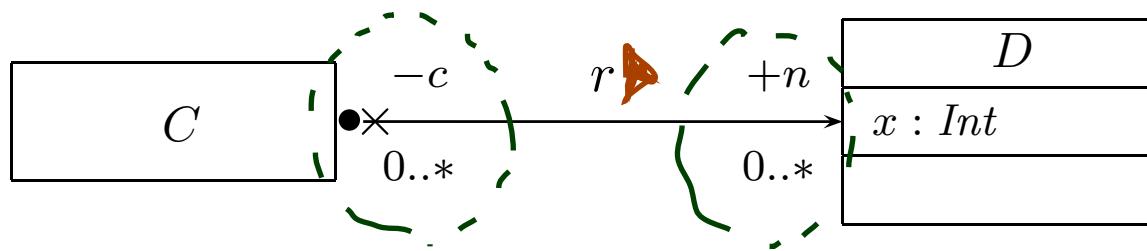
because  
is not of basic type

# From Association Lines to Extended Signatures



## Association Example

$\langle \text{role}_i : C_i, r, , \varphi_i, \xi_i, v_i, o_i \rangle$



**Signature:**

$$\mathcal{S} = (\{\text{Int}\}, \{C, D\}, \{x : \text{Int}, \text{Int}, \langle r : \langle \langle : C \rightarrow \{C\}, 0..*, \emptyset, -, x, 1 \rangle, \langle n : D, 0..*, \emptyset, +, o \rangle \rangle \}, \{C \rightarrow \{C\}, D \rightarrow \{x\}\})$$

now: only basic type attrs.  
are assigned by attr

# What If Things Are Missing?

Most components of associations or association end may be omitted.  
For instance [?, 17], Section 6.4.2, proposes the following rules:

- **Name**: Use

$$A\langle C_1 \rangle - \cdots - \langle C_n \rangle$$

if the name is missing.

**Example:**



- **Reading Direction**: no default.
- **Role Name**: use the class name at that end in lower-case letters

**Example:**



**Other convention**: (used e.g. by modelling tool Rhapsody)



# What If Things Are Missing?



$C:C, v = - - >$   
 $d:D, v = - > >$

- **Multiplicity:** 1

In my opinion, it's safer to assume 0..1 or \* if there are no fixed, written, agreed conventions ("expect the worst").

- **Properties:**  $\emptyset$

- **Visibility:** public

- **Navigability and Ownership:** not so easy. [?, 43]

OLD CONVENTION:



"Various options may be chosen for showing navigation arrows on a diagram.

In practice, it is often convenient to suppress some of the arrows and crosses and just show exceptional situations:

- Show all arrows and x's. Navigation and its absence are made completely explicit.
- Suppress all arrows and x's. No inference can be drawn about navigation.  
This is similar to any situation in which information is suppressed from a view.
- Suppress arrows for associations with navigability in both directions, and show arrows only for associations with one-way navigability.

In this case, the two-way navigability cannot be distinguished from situations where there is no navigation at all; however, the latter case occurs rarely in practice."

# Wait, If Omitting Things...

- ...**is causing so much trouble** (e.g. leading to misunderstanding), why does the standard say “**In practice, it is often convenient...**”?

Is it a good idea to trade **convenience** for **precision/unambiguity**?

**It depends.**

- Convenience as such is a legitimate goal.
- In UML-As-Sketch mode, precision “doesn’t matter”, so convenience (for writer) can even be a primary goal.
- In UML-As-Blueprint mode, **precision** is the **primary goal**. And misunderstandings are in most cases annoying.

**But:** (even in UML-As-Blueprint mode)

If all associations in your model have multiplicity \*, then it’s probably a good idea not to write all these \*’s.

**So:** tell the reader about it and leave out the \*’s.

# *Association Semantics*

# Overview

**What's left?** **Named** association with at least two typed **ends**, each having

- a **role name**,
- a **multiplicity**,
- a set of **properties**,
- a **visibility**,
- a **navigability**, and
- an **ownership**.

## The Plan:

- Extend **system states**, introduce so-called **links** as instances of associations — depends on **name** and on **type** and **number** of ends.
- Integrate **role name** and **multiplicity** into **OCL syntax/semantics**.
- Extend **typing rules** to care for **visibility** and **navigability**
- Consider **multiplicity** also as part of the **constraints** set  $Inv(\mathcal{CD})$ .
- **Properties**: for now assume  $P_v = \{\text{unique}\}$ .
- **Properties** (in general) and **ownership**: later.

# *Association Semantics: The System State Aspect*

# *Associations in General*

**Recall:** We consider associations of the following form:

$$\langle r : \langle role_1 : C_1, \mu_1, P_1, \xi_1, \nu_1, o_1 \rangle \rangle, \dots, \langle role_n : C_n, \mu_n, P_n, \xi_n, \nu_n, o_n \rangle \rangle$$

Only these parts are relevant for extended system states:

$$\langle r : \langle role_1 : C_1, -, P_1, -, -, - \rangle, \dots, \langle role_n : C_n, -, P_n, -, -, - \rangle \rangle$$

(recall: we assume  $P_1 = P_n = \{\text{unique}\}$ ).

The UML standard thinks of associations as **n-ary relations** which “**live on their own**” in a system state.

That is, **links** (= association instances)

- **do not** belong (in general) to certain objects (in contrast to pointers, e.g.)
- are “first-class citizens” **next to objects**,
- are (in general) **not** directed (in contrast to pointers).

# Links in System States

$$\langle r : \langle role_1 : C_1, \_, P_1, \_, \_, \_ \rangle, \dots, \langle role_n : C_n, \_, P_n, \_, \_, \_ \rangle \rangle$$

**Only** for the course of lectures 07/08 we change the definition of system states:

**Definition.** Let  $\mathcal{D}$  be a structure of the (extended) signature  $\mathcal{S} = (\mathcal{T}, \mathcal{C}, V, atr)$ .

A **system state** of  $\mathcal{S}$  wrt.  $\mathcal{D}$  is a pair  $(\sigma, \lambda)$  consisting of

- a type-consistent mapping

$$\sigma : \mathcal{D}(\mathcal{C}) \rightarrow (atr(\mathcal{C}) \rightarrow \mathcal{D}(\mathcal{T})),$$

*now: only basic types*

- a mapping  $\lambda$  which assigns each association

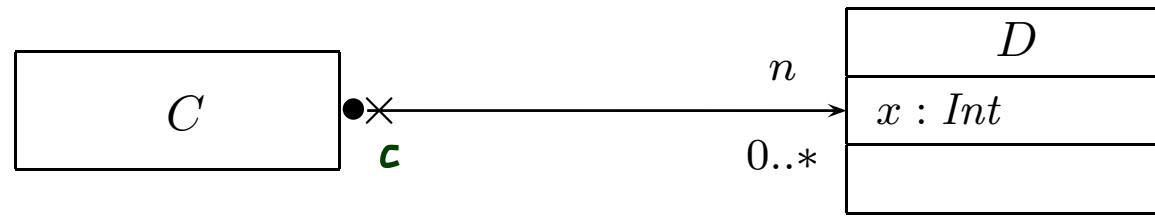
$$\langle r : \langle role_1 : C_1 \rangle, \dots, \langle role_n : C_n \rangle \rangle \in V \text{ a relation}$$

$$\lambda(r) \subseteq \mathcal{D}(C_1) \times \dots \times \mathcal{D}(C_n)$$

*set of n-tuples*

(i.e. a set of type-consistent  $n$ -tuples of identities).

# Association/Link Example



**Signature:**

$$\mathcal{S} = (\{\text{Int}\}, \{C, D\}, \{x : \text{Int},$$

$$\langle A\_C\_D : \langle c : \text{D}, 0..*, \{\text{unique}\}, \times, \text{D} \rangle, \langle n : \text{D}, 0..*, \{\text{unique}\}, >, \text{D} \rangle \rangle,$$

$$\{C \mapsto \emptyset, D \mapsto \{x\}\})$$

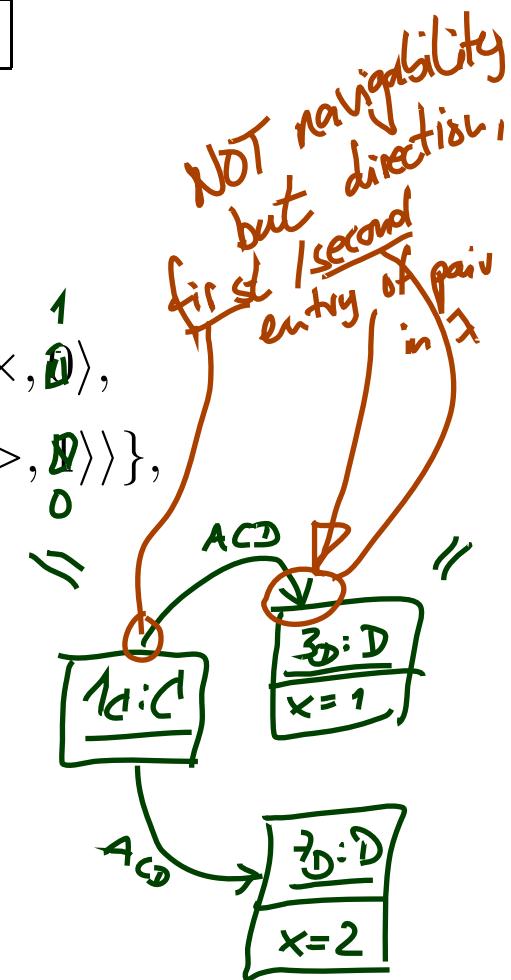
one instance of class  $C$

A **system state** of  $\mathcal{S}$  (some reasonable  $\mathcal{D}$ ) is  $(\sigma, \lambda)$  with:

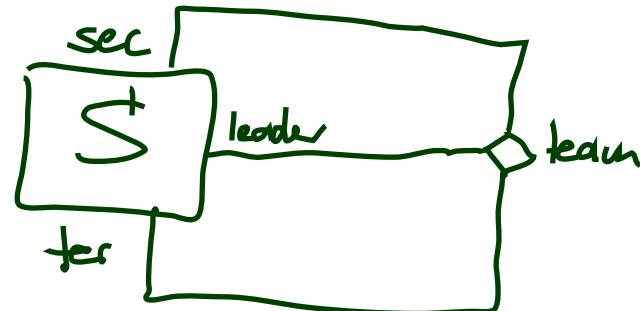
$$\sigma = \{1_C \mapsto \emptyset, 3_D \mapsto \{x \mapsto 1\}, 7_D \mapsto \{x \mapsto 2\}\}$$

$$\lambda = \{A\_C\_D \mapsto \{(1_C, 3_D), (1_C, 7_D)\}\}$$

$\underbrace{\quad}_{(A\_C\_D)}$



The order does matter...



$\varphi:$

$\langle \text{team} : \langle \text{ter}:S, \dots \rangle$   
 $\langle \text{sec}:S, \dots \rangle$   
 $\langle \text{ter}:S, \dots \rangle \rangle$

$$\sigma = \{ 1_s \mapsto \emptyset, 2_s \mapsto \emptyset, 5_s \mapsto \emptyset, 7_s \mapsto \emptyset \}$$

$$\lambda(t) = \{ (5_3, 2_s, 1_s), (1_s, 7_s, 5_s), (7_s, 7_s, 7_s) \}$$

$$\mathcal{D}(S) \times \mathcal{D}(S) \times \mathcal{D}(S)$$

OBJECT DIAGRAM WOULD NEED HYPEREDGES:



WE WILL NOT FORMALLY DEFINE THAT!

20.1.

# *Extended System States and Object Diagrams*

**Legitimate question:** how do we represent system states such as

$$\sigma = \{1_C \mapsto \emptyset, 3_D \mapsto \{x \mapsto 1\}, 7_D \mapsto \{x \mapsto 2\}\}$$

$$\lambda = \{A \_ C \_ D \mapsto \{(1_C, 3_D), (1_C, 7_D)\}\}$$

as **object diagram**?

- see page 20
- see page 20a

## *Associations and OCL*

# OCL and Associations: Syntax

**Recall:** OCL syntax as introduced in Lecture 03, interesting part:

$$\begin{aligned} \text{expr} ::= \dots & | r_1(\text{expr}_1) : \tau_C \rightarrow \tau_D & r_1 : D_{0,1} \in \text{atr}(C) \\ & | r_2(\text{expr}_1) : \tau_C \rightarrow \text{Set}(\tau_D) & r_2 : D_* \in \text{atr}(C) \end{aligned}$$

**Now becomes**

$$\begin{aligned} \text{expr} ::= \dots & | \text{role}(\text{expr}_1) : \tau_C \rightarrow \tau_D & \mu = 0..1 \text{ or } \mu = 1 \\ & | \text{role}(\text{expr}_1) : \tau_C \rightarrow \text{Set}(\tau_D) & \text{otherwise} \end{aligned}$$

if

$$\begin{aligned} & \langle r : \dots, \langle \text{role} : D, \mu, \_, \_, \_, \_, \_ \rangle, \dots, \langle \text{role}' : C, \_, \_, \_, \_, \_, \_ \rangle, \dots \rangle \in V \text{ or} \\ & \langle r : \dots, \langle \text{role}' : C, \_, \_, \_, \_, \_ \rangle, \dots, \langle \text{role} : D, \mu, \_, \_, \_, \_, \_ \rangle, \dots \rangle \in V, \text{role} \neq \text{role}' . \end{aligned}$$

**Note:**

- Association name as such doesn't occur in OCL syntax, role names do.
- $\text{expr}_1$  has to denote an object of a class which "participates" in the association.

## *References*

