# Software Design, Modelling and Analysis in UML

Lecture 09: Class Diagrams IV

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# Contents & Goals

#### Last Lectures

. Started to discuss "associations", the general case.

#### This Lecture:

- Educational Objectives: Capabilities for following tasks/questions.
- Cont'd: Please explain this class diagram with associations.
- When is a class diagram a good class diagram?
- What are purposes of modelling guidelines? (Example?)
- Discuss the style of this class diagram.
- Content
- Treat "the rest".
- Where do we put OCL constraints?
- Modelling guidelines, in particular for class diagrams (following [Ambler, 2005])

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Associations: The Rest

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## The Rest

Recapitulation: Consider the following association:

 $\langle r: \langle role_1: C_1, \mu_1, P_1, \xi_1, \nu_1, o_1 \rangle, \ldots, \langle role_n: C_n, \mu_n, P_n, \xi_n, \nu_n, o_n \rangle \rangle$ 

- Association name r and role names/types  $role_i/C_i$  induce extended system states  $\lambda.$
- Multiplicity  $\mu$  is considered in OCL syntax.
- Visibility  $\xi/\text{Navigability }\nu$ : well-typedness.

### Now the rest:

- Multiplicity  $\mu$ : we propose to view them as constraints.
- Properties  $P_i$ : even more typing.
- Ownership o: getting closer to pointers/references.
- Diamonds: exercise.

# Visibility

Not so surprising: Visibility of role-names is treated completely similar to visibility of attributes, namely by typing rules.

Question: given



is the following OCL expression well-typed or not (wrt. visibility):

context 
$$C$$
 inv:  $self$ -role. $x>0$  with typed allowys context  $D$  inv:  $self$ -role  $_2$ , role  $_2$  >0 with  $\omega$ - $\mathcal{E}$ . If  $\sigma$  is a simple context  $\sigma$ 

# Visibility

Not so surprising: Visibility of role-names is treated completely similar to visibility of attributes, namely by typing rules.

## Question: given



is the following OCL expression well-typed or not (wrt. visibility):

context 
$$C$$
 inv :  $self.role.x > 0$   
  $\times ( pole (x()) )$ 

Basically same rule as before: (analogously for other multiplicities)

$$\begin{array}{ll} (Assoc_1) & A, D \vdash expr_1 : \tau_C \\ A, D \vdash role(expr_1) : \tau_D \\ & (r : \dots \langle role : D, \mu, \neg \xi, \neg \rangle, \dots \langle role' : C, \neg \neg \neg \rangle, \dots \rangle \in V \end{array}$$

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## Navigability

Navigability is similar to visibility: expressions over non-navigable association ends ( $\nu = \times$ ) are basically type-correct, but forbidde

1 not well typed

Question: given

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2.Int	role	- D

is the following OCL expression well-typed or not (wrt. navigability):

context D inv : self.role.x > 0

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# The Rest of the Rest

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- Multiplicity μ: we propose to view them as constraints.
- Properties P<sub>i</sub>: even more typing.
- Ownership o: getting closer to pointers/references.
- · Diamonds: exercise.

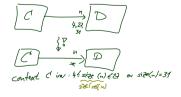
Navigability Navigability is similar to visibility: expressions over non-navigable ass ends  $(\nu = \times)$  are basically type-correct, but forbidden. Question: given is the following OCL expression well-typed or not (wrt. navigability): d giran ( context D inv : self.role.x > 0m UMC a The standard says: • 'x': navigation is not possible detricate • '-': navigation is possible · '>': navigation is efficient So: In general, UML associations are different from pointers/references! (\*) But: Pointers/references can faithfully be modelled by UML associations

## Multiplicities as Constraints

Recall: The multiplicity of an association end is a term of the form

$$\mu ::= \ast \mid N \mid N..M \mid N..\ast \mid \mu, \mu \tag{$N,M \in \mathbb{N}$}$$

Proposal: View multiplicities (except 0..1, 1) as additional invariants/constraints.



\* D makes no souse ...?

- o in general there is no OCI expression, involving of a subject is well-typed of for requirements, we may discrepant well-typedness and write landful ("in a statement will typedness and write landful ("in a statement of a statement
- is nivell-typedness of expris what about 1- and 3/
  - o in our formal, math. setting of UML models: there's no difference
  - a for the implementation: define what "efficient" means and tell it to the programmers

## Multiplicities as Constraints

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M = N. Hlym NHENU SX3

**Proposal**: View multiplicities (except 0..1, 1) as additional invariants/constraints.

Rocall: we can normalize each multiplicity  $\mu$  to the form  $e_{; 9}$  . 31 +6 Observe  $N_1..N_2, \ldots, N_{2k-1}..N_{2k}$ 

where  $N_i \leq N_{i+1}$  for  $1 \leq i \leq 2k$ ,  $N_1, \dots, N_{2k-1} \in \mathbb{N}$ ,  $N_{2k} \in \mathbb{N} \cup \{*\}$ . eg. \* + ð..¥

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## Multiplicities as Constraints

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# Why Multiplicities as Constraints?

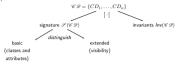
More precise, can't we just use types? (cf. Slide 26)

- $\mu=0..1$ ,  $\mu=1$ : many programming language have direct correspondences (the first corresponds to type pointer, the second to type reference) therefore treated specially.
- \* μ = \*.
  could be represented by a set data-structure type without fixed bounds no problem with our approach, we have μ<sub>OCL</sub> = true anyway.
- $\mu$  = 0..3: use array of size 4 if model behaviour (or the implementation) adds 5th identity, we'll get a runtime error, and thereby see that the constraint is violated. Principally acceptable, but: checks for array bounds everywhere...?
- μ = 0...Γ<sub>c</sub>
   could3f expresented by an array of size 7 but: few programming languages/data structure libraries allow lower bounds for arrays (other than 0).
   If we have 5 identities and the model behaviour removes one, this should be a violation of the constraints imposed by the model.

The implementation which does this removal is wrong. How do we see this...?

## Multiplicities as Constraints of Class Diagram

#### Recall/Later:



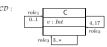
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$$\begin{split} \langle r:\dots,\langle role:D,\mu,\neg,\neg,\rangle,\dots,\langle role':C,\neg,\neg,\neg,\rangle,\dots\rangle \in V \text{ or } \\ \langle r:\dots,\langle role':C,\neg,\neg,\neg,\rangle,\dots,\langle role:D,\mu,\neg,\neg,\rangle,\dots\rangle \in V, \\ role \neq role',\mu \notin \{0.1\}\}. \end{split}$$

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## Multiplicities as Constraints Example

 $\mu_{\mathrm{OCL}}^C(role) = \mathrm{context}\ C \ \mathrm{inv}:$   $(N_1 \leq role \rightarrow \mathrm{size}() \leq N_2) \ \ \mathrm{or} \ \ \dots \ \ \mathrm{or} \ \ (N_{2k-1} \leq role \rightarrow \mathrm{size}() \leq N_{2k})$ 



#### Inv(CD) =

- {context C inv :  $4 \le role_2 \rightarrow \text{size}() \le 4 \text{ or } 17 \le role_2 \rightarrow \text{size}() \le 17$ } = {context C inv :  $role_2 \rightarrow \text{size}() = 4 \text{ or } role_2 \rightarrow \text{size}() = 17$ }
- $\cup \{\text{context } C \text{ inv } : 3 \leq role_3 \rightarrow \text{size}()\}$

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# Multiplicities Never as Types...?

Well, if the target platform is known and fixed, and the target platform has, for instance,

- reference types,
- range-checked arrays with positions  $0,\dots,N$ ,
- set types,

then we could simply restrict the syntax of multiplicities to

$$\mu ::= 1 \mid 0..N \mid *$$

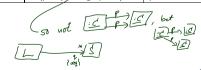
and don't think about constraints (but use the obvious 1-to-1 mapping to types)...

In general, unfortunately, we don't know.

# Properties

We don't want to cover association **properties** in detail, only some observations (assume binary associations):

Property	Intuition	Semantical Effect	
unique	one object has at most one $r$ -link to a single other object ${\bf e}_{\bf v}$	current setting	
bag	one object may have multiple $r$ -links to a single other object	have $\lambda(r)$ yield multi-sets	
ordered, sequence	an $r$ -link is a <b>sequence</b> of object identities (possibly including duplicates)	have $\lambda(r)$ yield sequences	



# Properties

We don't want to cover association **properties** in detail, only some observations (assume binary associations):

Property	Intuition	Semantical Effect	
unique	single other object	object has at most one $r$ -link to a current setting gle other object	
bag	one object may have $\displaystyle                                   $	$\begin{array}{ll} \text{have} & \lambda(r) & \text{yield} \\ \text{multi-sets} \end{array}$	
ordered, sequence	an $r$ -link is a sequence of object identities (possibly including duplicates)	have $\lambda(r)$ yield sequences	

Property	OCL Typing of expression $role(expr)$
unique	$\tau_D \rightarrow Set(\tau_C)$
bag	$\tau_D \rightarrow Bag(\tau_C)$
ordered, sequence	$\tau_D \rightarrow Seq(\tau_C)$

For subsets, redefines, union, etc. see [OMG, 2007a, 127].

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# Back to the main track:

Recall: on some earlier slides we said, the extension of the signature is **only** to study associations in "full beauty".

For the remainder of the course, we should look for something simpler...

#### Proposal

• from now on, we only use associations of the form



(And we may omit the non-navigability and ownership symbols.)

- $\bullet$  Form (i) introduces  $role:C_{0,1},$  and form (ii) introduces  $role:C_{\ast}$  in V.
- In both cases,  $role \in atr(C)$ .
- We drop  $\lambda$  and go back to our nice  $\sigma$  with  $\sigma(u)(role) \subseteq \mathcal{D}(D)$ .

## Ownership



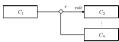
Intuitively it says:

Association r is not a "thing on its own" (i.e. provided by  $\lambda$ ), but association end 'role' is owned by C (!). (That is, it's stored inside C object and provided by  $\sigma$ ).

So: if multiplicity of role is 0.1 or 1, then the picture above is  $\underline{very}$   $\underline{close}$  to concepts of pointers/references.

Actually, ownership is seldom seen in UML diagrams. Again: if target platform is clear, one may well live without (cf. [OMG, 2007b, 42] for more details).

#### Not clear to me:



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# Back to the Main Track

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# Where Shall We Put OCL Constraints?

#### Numerous options:

- (i) Additional documents.
- (ii) Notes.
- (iii) Particular dedicated places.
- (ii) Notes:

A UML note is a picture of the form

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[test]

text can principally be everything, in particular comments and constraints.

Sometimes, content is explicitly classified for clarity:



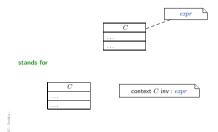
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OCL Constraints in (Class) Diagrams

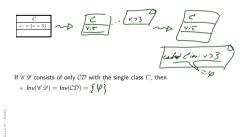
## OCL in Notes: Conventions



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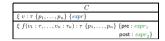
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# Invariant in Class Diagram Example

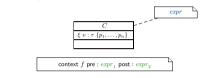


# Where Shall We Put OCL Constraints?

(ii) Particular dedicated places in class diagrams: (behav. feature: later)



For simplicity, we view the above as an abbreviation for



# Semantics of a Class Diagram

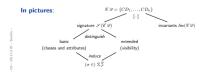
Definition. Let  $\mathscr{C}\mathscr{D}$  be a set of class diagrams. We say, the semantics of  $\mathscr{C}\mathscr{D}$  is the signature it induces and the set of

We say, the semantics of  $\mathscr{C}\mathscr{D}$  is the signature it induces and the set of OCL constraints occurring in  $\mathscr{C}\mathscr{D}$ , denoted

 $[\mathscr{C}\mathscr{D}]:=\langle \mathscr{S}(\mathscr{C}\mathscr{D}), \mathit{Inv}(\mathscr{C}\mathscr{D}) \rangle.$ 

Given a structure  $\mathscr{D}$  of  $\mathscr{S}$  (and thus of  $\mathscr{C}\mathscr{D}$ ), the class diagrams describe the system states  $\Sigma_{\mathscr{S}}^{\mathscr{D}}$ . Of those, **some** satisfy  $Inv(\mathscr{C}\mathscr{D})$  and some don't.

We call a system state  $\sigma \in \Sigma_{\mathscr{S}}^{\mathscr{D}}$  consistent if and only if  $\sigma \models \mathit{Inv}(\mathscr{C}\mathscr{D})$ .



Invariants of a Class Diagram

- Let  $\mathcal{CD}$  be a class diagram.
- As we (now) are able to recognise OCL constraints when we see them, we can define

Inv(CD)

as the set  $\{\varphi_1,\dots,\varphi_n\}$  of OCL constraints **occurring** in notes in  $\mathcal{CD}$  — after unfolding all abbreviations (cf. next slides).

- As usual:  $Inv(\mathscr{C}\mathscr{D}) := \bigcup_{\mathcal{CD} \in \mathscr{C}\mathscr{D}} Inv(\mathcal{CD}).$
- Principally clear: Inv(·) for any kind of diagram.

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## Pragmatics

Recall: a UML model is an image or pre-image of a software system.

A set of class diagrams  $\mathscr{CD}$  with invariants  $\mathit{Inv}(\mathscr{CD})$  describes the structure of system states.

Together with the invariants it can be used to state:

- $\bullet \ \ \, \textbf{Pre-image:} \ \, \textbf{Dear programmer, please provide an implementation which} \\ \ \ \, \textbf{uses only system states that satisfy} \ \, \textit{Inv}(\mathscr{CD}). \\$
- Post-image: Dear user/maintainer, in the existing system, only system states which satisfy  $Inv(\mathscr{C}\mathscr{D})$  are used.

(The exact meaning of "use" will become clear when we study behaviour — intuitively: the system states that are reachable from the initial system state(s) by calling methods or firing transitions in state-machines.)

Example: highly abstract model of traffic lights controller.



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# Constraints vs. Types

## Find the 10 differences:



- ullet x=4 is well-typed in the left context, a system state satisfying x=4 violates the constraints of the diagram.
- x=4 is not even well-typed in the right context, there cannot be a system state with  $\sigma(u)(x)=4$  because  $\sigma(u)(x)$  is supposed to be in  $\mathscr{D}(T)$  (by definition of system state).

### Rule-of-thumb:

- If something "feels like" a type (one criterion: has a natural correspondence in the application domain), then make it a type.
- $\bullet$  If something is a requirement or restriction of an otherwise useful type, then make it a constraint.

References

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# References

[Ambler, 2005] Ambler, S. W. (2005). The Elements of UML 2.0 Style. Cambridge University Press.

[OMG, 2007a] OMG (2007a). Unified modeling language: Infrastructure, version 2.1.2. Technical Report formal/07-11-04.

[OMG, 2007b] OMG (2007b). Unified modeling language: Superstructure, version 2.1.2. Technical Report formal/07-11-02.

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