Software Design, Modelling and Analysis in UML

Lecture 12: Core State Machines III

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Roadmap: Chronologically (5) E[\varphi]/od \sigma_{\varphi_1}

 $\mathcal{I} = (\mathcal{I}, \mathcal{C}, V, atr), SM$

(i) What do we (have to) cover?

UML State Machine Diagrams Syntax.

(ii) Def.: Signature with signals. (iii) Def.: Core state machine.

(iv) Map UML State Machine Diagrams to core state machines.

Semantics: The Basic Causality Model

(v) Def.: Ether (aka. event pool)

(vi) Def.: System configuration. (vii) Def.: Event.

(viii) Def.: Transformer.

(ix) Def.: Transition system, computation.

(x) Transition relation induced by core state ma-

(xi) Def.: step, run-to-completion step.

(xii) Later: Hierarchical state machines.

Contents & Goals

Last Lecture:

- The basic causality model
- · Ether, System Configuration, Event, Transformer

This Lecture

- Educational Objectives: Capabilities for following tasks/questions.
- What does this State Machine mean? What happens if I inject this event?
- . Can you please model the following behaviour.
- What is: Signal, Event, Ether, Transformer, Step, RTC.
- Content:
- Examples for transformer
- Run-to-completion Step
- Putting It All Together

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Transformer the deject "executing" the action. Let $\Sigma_{\mathcal{G}}^{\mathcal{G}}$ the set of system configurations over some \mathscr{G}_0 , \mathscr{G}_0 and Eth and ether. We call a relation

 $t \subseteq \mathscr{D}(\mathscr{C}) \times (\Sigma_{\mathscr{S}}^{\mathscr{D}} \times Eth) \times (\Sigma_{\mathscr{S}}^{\mathscr{D}} \times Eth)$ a (system configuration) **transformer**.

 \bullet In the following, we assume that each application of a transformer t to some system configuration (σ,ε) for object u_x is associated with a set of observations

$$Obs_t[u_x](\sigma,\varepsilon) \in 2^{\mathscr{D}(\mathscr{C}) \times Evs(\mathscr{E} \ \dot{\cup} \ \{*,+\},\mathscr{D}) \times \mathscr{D}(\mathscr{C})}.$$

* An observation $(u_{src},(E,\vec{d},u_{dst})\in Obs_t[u_x](\sigma,\varepsilon)$ represents the information that, as a "side effect" of u_x executing t, an event (!) (E,\vec{d}) has been sent from object u_{src} to object u_{dst} . Special cases: creation/destruction.

System Configuration, Ether, Transformer

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Why Transformers?

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    Recall the (simplified) syntax of transition annotations:
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 $annot ::= [\langle event \rangle \ ['[' \langle guard \rangle ']'] \ ['/' \langle action \rangle]]$

- Clear: ⟨event⟩ is from ℰ of the corresponding signature.
- But: What are $\langle guard \rangle$ and $\langle action \rangle$?
- UML can be viewed as being parameterized in expression language (providing $\langle guard \rangle$) and action language (providing $\langle action \rangle$).
- Examples:
- Expression Language:
- · OCL
- · Java, C++, ... expressions
- Action Language:
 - UML Action Semantics, "Executable UML"
- \cdot Java, C++, \dots statements (plus some event send action)

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Transformers as Abstract Actions!

In the following, we assume that we're given

- \bullet an expression language ${\it Expr}$ for guards, and
- \bullet an action language Act for actions,

and that we're given

• a semantics for boolean expressions in form of a partial function

$$I[\,\cdot\,](\,\cdot\,,\,\cdot\,): Expr \to ((\Sigma^{\mathscr{D}}_{\mathscr{S}} \times (\{\text{test}\} \to \mathscr{D}(\mathscr{C}))) \to \mathbb{B})$$

which evaluates expressions in a given system configuration,

Assuming I to be partial is a way to treat "undefined" during runtime. If I is not defined (for instance because of dangling-reference navigation or division-by-zero), we want to go to a designated "error" system configuration.

ullet a transformer for each action: For each $act \in Act$, we assume to have

$$t_{act} \subseteq \mathscr{D}(\mathscr{C}) \times (\Sigma_{\mathscr{S}}^{\mathscr{D}} \times Eth) \times (\Sigma_{\mathscr{S}}^{\mathscr{D}} \times Eth).$$

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pushial function I may not defined for some exps & Exps

Transformer Examples: Presentation

| abstract syntax | concrete syntax | |
|--|-----------------|--|
| op | | |
| intuitive semantics | | |
| *** | | |
| well-typedness | | |
| *** | | |
| semantics | | |
| $((\sigma, \varepsilon), (\sigma', \varepsilon')) \in t_{op}[u_x]$ iff | | |
| or | | |
| $t_{op}[u_x](\sigma, \varepsilon) = (\sigma', \varepsilon')$ where | | |
| observables | | |
| $Obs_{op}[u_x](\sigma, \varepsilon) = {}, \text{ not a relation, dep}$ | ends on choice | |
| (error) conditions | | |
| Not defined if | | |

Expression/Action Language Examples

We can make the assumptions from the previous slide because instances exist:

- for OCL, we have the OCL semantics from Lecture 03. Simply remove the pre-images which map to "\perp".
- for Java, the operational semantics of the SWT lecture uniquely defines transformers for sequences of Java statements.

We distinguish the following kinds of transformers:

- . skip: do nothing recall: this is the default action
- send: modifies ε interesting, because state machines are built around sending/consuming events
- create/destroy: modify domain of σ not specific to state machines, but let's discuss them here as we're at it

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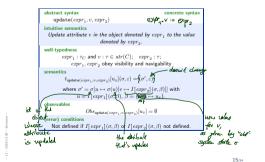
• update: modify own or other objects' local state — boring

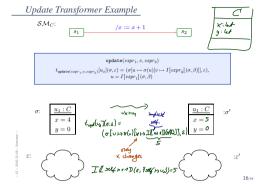
Transformer: Skip

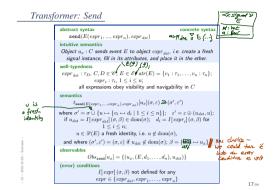
| abstract syntax skip | | concrete syntax |
|-------------------------|---|-----------------|
| intuitive semantics | do nothing | |
| well-typedness | ./. | |
| semantics | $t[u_x](\sigma, \varepsilon) = \{(\sigma, \varepsilon)\}$ | |
| observables | $Obs_{skip}[u_x](\sigma, \varepsilon) = \emptyset$ | |
| (error) conditions | | |

In the following we discuss

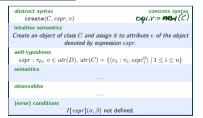
Transformer: Update







Transformer: Create

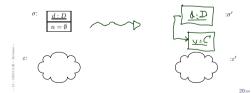


- We use an "and assign"-action for simplicity it doesn't add or remove expressive power, but moving creation to the expression language raises all kinds of other problems such as order of evaluation (and thus creation).
- Also for simplicity: no parameters to construction (~ parameters of constructor).
 Adding them is straightforward (but somewhat tedious).

$\mathtt{create}(C, \mathit{czpr}, v)$ $t_{\mathtt{create}(C, \mathit{czpr}, v)}(\sigma, \varepsilon) = \dots$

Create Transformer Example

SMC:



 s_2

Send Transformer Example

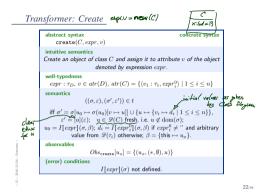
 \mathcal{SM}_C : $(s_1) \longrightarrow (f(x+1); \dots) \longrightarrow (s_2)$





How To Choose New Identities?

- \bullet Re-use: choose any identity that is not alive **now**, i.e. not in $dom(\sigma)$.
- Doesn't depend on history.
- May "undangle" dangling references may happen on some platforms.
- Fresh: choose any identity that has not been alive **ever**, i.e. not in $\mathrm{dom}(\sigma)$ and any predecessor in current run.
- Depends on history.
- Dangling references remain dangling could mask "dirty" effects of platform.



Transformer: Destroy

abstract syntax concrete syntax $\operatorname{destroy}(expr)$ intuitive semantics $\operatorname{Destroy} the object denoted by expression expr.$ well-typedness $expr: \tau_C, C \in \mathscr{C}$ semantics $\dots \\ observables$ $Obs_{\operatorname{destroy}}[u_x] = \{(u_x, (+, \emptyset), u)\}$ (error) conditions $I[expr](\sigma, \beta) \text{ not defined.}$

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Destroy Transformer Example

 \mathcal{SM}_C : $/\ldots; delete \ n;\ldots$ s_2

 $\begin{aligned} & \operatorname{destroy}(expr) \\ & t_{\operatorname{destroy}(expr)}[u_x](\sigma, \varepsilon) = \dots \end{aligned}$

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What to Do With the Remaining Objects?

Assume object u_0 is destroyed...

- object u_1 may still refer to it via association r:
- allow dangling references?
- or remove u_0 from $\sigma(u_1)(r)$?
- ullet object u_0 may have been the last one linking to object u_2 :
- leave u_2 alone?
- or remove u_2 also?
- . Plus: (temporal extensions of) OCL may have dangling references.

Our choice: Dangling references and no garbage collection!
This is in line with "expect the worst", because there are target platforms which don't provide garbage collection — and models shall (in general) be correct without assumptions on target platform.

But: the more "dirty" effects we see in the model, the more expensive it often is to analyse. Valid proposal for simple analysis: monotone frame semantics, no destruction at all.

Transformer: Destroy

abstract syntax concrete syntax destroy(expr) intuitive semantics Destroy the object denoted by expression <math>expr. well-typedness $expr: \tau c, C \in \mathscr{C}$ semantics $t[u_x](\sigma, \varepsilon) = (\sigma', \varepsilon)$ where $\sigma' = \sigma|_{\{\mathrm{dom}(\sigma)\} \in \mathbb{N}\}}$ with $u = I[expr](\sigma, \beta)$. observables $Obs_{\mathtt{destroy}}[u_x] = \{(u_x, (+, \emptyset), u)\}$ (error) conditions $I[expr](\sigma, \beta) \text{ not defined}.$

Sequential Composition of Transformers

 \bullet Sequential composition $t_1\circ t_2$ of transformers t_1 and t_2 is canonically defined as

 $(t_2\circ t_1)[u_x](\sigma,\varepsilon)=t_2[u_x](t_1[u_x](\sigma,\varepsilon))$

with observation

 $Obs_{(t_2\circ t_1)}[u_x](\sigma,\varepsilon) = Obs_{t_1}[u_x](\sigma,\varepsilon) \cup Obs_{t_2}[u_x](t_1(\sigma,\varepsilon)).$

• Clear: not defined if one the two intermediate "micro steps" is not defined.

X:=x1, 134:= 77, 4.07

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Transformers And Denotational Semantics

Observation: our transformers are in principle the denotational semantics of the actions/action sequences. The trivial case, to be precise.

Note: with the previous examples, we can capture

- · empty statements, skips,
- assignments,
- conditionals (by normalisation and auxiliary variables),/5
- create/destroy,

but not possibly diverging loops

Our (Simple) Approach: if the action language is, e.g. Java, then (syntactically) forbid loops and calls of recursive functions.

Other Approach: use full blown denotational semantics.

No show-stopper, because loops in the action annotation can be converted into transition cycles in the state machine

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while x >0 do xs/x-1

Active vs. Passive Classes/Objects

- . Note: From now on, assume that all classes are active for simplicity. We'll later briefly discuss the Rhapsody framework which proposes a way how to integrate non-active objects.
- Note: The following RTC "algorithm" follows [Harel and Gery, 1997] (i.e. the one realised by the Rhapsody code generation) where the standard is ambiguous or leaves choices.

Run-to-completion Step

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From Core State Machines to LTS

Definition. Let $\mathscr{S}_0=(\mathscr{T}_0,\mathscr{C}_0,V_0,atr_0)$ be a signature with signals (all classes active), \mathscr{D}_0 a structure of \mathscr{S}_0 , and $(Eth, ready, \oplus, \ominus, [\cdot])$ an ether over \mathscr{S}_0 and \mathscr{D}_0 . Assume there is one core state machine M_C per class $C \in \mathscr{C}$.

We say, the state machines induce the following labelled transition relation on states $S:=\Sigma^{\mathcal{G}}_{\mathcal{F}}\dot{\cup}\left\{\#\right\} \text{ with actions }A:=2^{\mathcal{G}(\mathcal{E})\times Ews(\mathcal{E},\mathcal{P})}\times 2^{\mathcal{G}(\mathcal{E})\times Ews(\mathcal{E},\mathcal{P})}\times \mathcal{D}(\mathcal{E}):$

$$(\sigma, \varepsilon) \xrightarrow{(cons,Snd)} (\sigma', \varepsilon')$$

- $\begin{array}{l} \mbox{if and only if} \\ \mbox{(i) an event with destination } u \mbox{ is discarded,} \end{array}$
- (ii) an event is dispatched to u, i.e. stable object processes an event, or
- (iii) run-to-completion processing by u commences, i.e. object u is not stable and continues to process an event,
- (iv) the environment interacts with object u,

 $s \xrightarrow{(cons,\emptyset)} #$

if and only if

(v) s = # and $cons = \emptyset$, or an error condition occurs during consumption of cons.

Transition Relation, Computation

Definition. Let A be a set of actions and S a (not necessarily finite) set of of states.

We call

 $\rightarrow \subseteq S \times A \times S$

a (labelled) transition relation.

Let $S_0 \subseteq S$ be a set of initial states. A sequence

$$s_0 \xrightarrow{a_0} s_1 \xrightarrow{a_1} s_2 \xrightarrow{a_2} \dots$$

with $s_i \in S$, $a_i \in A$ is called **computation** of the labelled transition system (S, \rightarrow, S_0) if and only if

- initiation: $s_0 \in S_0$
- consecution: $(s_i, a_i, s_{i+1}) \in \rightarrow$ for $i \in \mathbb{N}_0$.

Note: for simplicity, we only consider infinite runs.

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(i) Discarding An Event

$$(\sigma, \varepsilon) \xrightarrow{(cons,Snd)} (\sigma', \varepsilon')$$

• an E-event (instance of signal E) is ready in ε for m object of a class \mathscr{C} , i.e.

 $\Delta u \in dom(\sigma) \cap \mathcal{D}(C) \exists u_E \in \mathcal{D}(\mathcal{E}) : u_E \in ready(\varepsilon, u)$

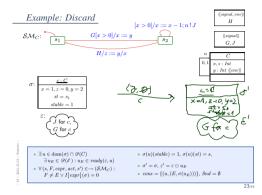
- u is stable and in state machine state s, i.e. $\sigma(u)(stable)=1$ and $\sigma(u)(st)=s$,
- · but there is no corresponding transition enabled (all transitions incident with current state of u either have other triggers or the guard is not satisfied)

 $\forall (s, F, expr, act, s') \in \rightarrow (SM_C) : F \neq E \lor I[expr](\sigma) = 0$

- the system configuration doesn't change, i.e. $\sigma' = \sigma$
- ullet the event u_E is removed from the ether, i.e.

consumption of u_E is observed, i.e.

$$cons = \{(u, (E, \sigma(u_E)))\}, Snd = \emptyset.$$



(iii) Commence Run-to-Completion

$$(\sigma,\varepsilon) \xrightarrow[u]{(cons.Snd)} (\sigma',\varepsilon')$$
 if
$$\bullet \text{ there is an unstable object} \text{ of a class } \mathscr{C}, \text{ i.e.}$$

$$\mathscr{B}u \in \text{dom}(\sigma) \cap \mathscr{P}(C) : \sigma(u)(stable) = 0$$

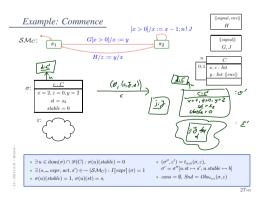
$$\bullet \text{ there is a transition without} \text{ there is a ball from the current state } s = \sigma(u)(st), \text{ i.e.}$$

$$\exists (s,\neg expr, act, s') \in \rightarrow (\mathcal{S}M_C) : I[expr](\sigma) = 1$$
 and
$$\bullet \quad (\sigma',\varepsilon') \text{ results from applying } t_{act} \text{ to } (\sigma,\varepsilon), \text{ i.e.}$$

$$(\sigma'',\varepsilon') \stackrel{\text{def}}{=} t_{act}(\sigma,\varepsilon), \quad \sigma' = \sigma''[u.st \mapsto s', u.stable \mapsto b]$$
 where b depends as before.
$$\bullet \text{ Only the side effects of the action are observed, i.e.}$$

$$cons = \emptyset, Snd = Obs_{tex}(\sigma,\varepsilon).$$

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(ii) Dispatch

and

a transition is enabled, i.e.

where $\tilde{\sigma} = \sigma[u.params_E$

where b depends:

Otherwise b = 0.

 $(\sigma, \varepsilon) \xrightarrow{(cons, Snd)} (\sigma', \varepsilon')$ if

• u is stable and in state machine state s, i.e. $\sigma(u)(stable)=1$ and $\sigma(u)(st)=s$,

• (σ', ε') results from applying t_{act} to (σ, ε) and removing u_E from the ether, i.e.

 $(\sigma'', \varepsilon') = t_{act}(\tilde{\sigma}, \varepsilon \ominus u_E),$ $\sigma' = (\sigma''[u.st \mapsto \underline{s'}, u.stable \mapsto b, u.params_E \mapsto \emptyset])|_{\mathscr{D}(\mathscr{C}) \backslash \{u_E\}}$

• If u becomes stable in s', then b=1. It does become stable if and only if there is no transition without trigger enabled for u in (σ', ε') .

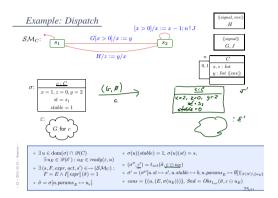
 $cons = \{(u, (E, \sigma(u_E)))\}, Snd = Obs_{t_{act}}(\tilde{\sigma}, \varepsilon \ominus u_E).$

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 \bullet Consumption of u_E and the side effects of the action are observed, i.e.

 $\exists \, (s, F, \mathit{expr}, \widehat{\mathit{act}}, \underline{s}') \in \rightarrow (\mathcal{SM}_C) : F = E \wedge I[\mathit{expr}](\bar{\sigma}) = 1$

• $\mathbf{M}u \in \text{dom}(\sigma) \cap \mathcal{D}(C) \exists u_E \in \mathcal{D}(\mathcal{E}) : u_E \in readu(\varepsilon, u)$



(iv) Environment Interaction

Assume that a set $\mathscr{E}_{env}\subseteq\mathscr{E}$ is designated as environment events and a set of attributes $v_{env} \subseteq V$ is designated as input attributes.

$$(\sigma, \varepsilon) \xrightarrow[env]{(cons,Snd)} (\sigma', \varepsilon')$$

- an environment event $E \in \mathscr{E}_{env}$ is spontaneously sent to an alive object $u \in \mathcal{D}(\sigma)$, i.e.

 $\sigma' = \sigma \mathrel{\dot{\cup}} \{u_E \mapsto \{v_i \mapsto d_i \mid 1 \leq i \leq n\}, \quad \varepsilon' = \varepsilon \oplus u_E$

where $u_E \notin dom(\sigma)$ and $atr(E) = \{v_1, \dots, v_n\}$.

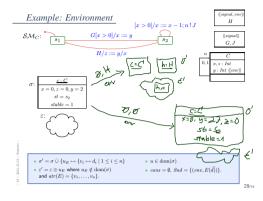
• Sending of the event is observed, i.e. $cons = \emptyset$, $Snd = \{(env, E(\vec{d}))\}$.

· Values of input attributes change freely in alive objects, i.e.

 $\forall v \in V \ \forall u \in dom(\sigma) : \sigma'(u)(v) \neq \sigma(u)(v) \implies v \in V_{env}$

and no objects appear or disappear, i.e. $dom(\sigma') = dom(\sigma)$.

ε' = ε.





Note: we call one evolution $(\sigma, \varepsilon) \xrightarrow[u]{(cons,Snd)} (\sigma', \varepsilon')$ a step.

Thus in our setting, a step directly corresponds to

one object (namely u) takes a single transition between regular states. (We have to extend the concept of "single transition" for hierarchical state machines.)

That is: We're going for an interleaving semantics without true parallelism.

Remark: With only methods (later), the notion of step is not so clear. For example, consider

- c_1 calls f() at c_2 , which calls g() at c_1 which in turn calls h() for c_2 .
- Is the completion of h() a step?
- Or the completion of f()?
- Or doesn't it play a role?

It does play a role, because constraints/invariants are typically (= by convention) assumed to be evaluated at step boundaries, and sometimes the convention is meant to admit (temporary) violation in between steps. (v) Error Conditions if, in (ii) or (iii), • I[expr] is not defined for σ , or t_{act} is not defined for (σ, ε), • consumption is observed according to (ii) or (iii), but $Snd = \emptyset$.

s_2 $(H,B') \rightarrow #$ • I[expr] not defined for σ , or · consumption according to (ii) or (iii) • t_{act} is not defined for (σ, ε) 31/43

G[x > 0]/x := y

Example: Error Condition

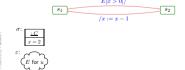
SMc:

Notions of Steps: The Run-to-Completion Step

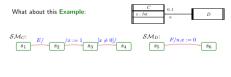
What is a run-to-completion step ...?

- . Intuition: a maximal sequence of steps, where the first step is a dispatch step and all later steps are commence steps.
- . Note: one step corresponds to one transition in the state machine. A run-to-completion step is in general not syntacically definable — one transition may be taken multiple times during an RTC-step.

Example:



Notions of Steps: The Run-to-Completion Step





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Notions of Steps: The Run-to-Completion Step Cont'd

Proposal: Let

$$(\sigma_0, \varepsilon_0) \xrightarrow[u_0]{(cons_0, Snd_0)} \dots \xrightarrow[u_{n-1}]{(cons_{n-1}, Snd_{n-1})} (\sigma_n, \varepsilon_n), \quad n > 0,$$

be a finite (!), non-empty, maximal, consecutive sequence such that

- object u is alive in σ₀,
- $u_0 = u$ and $(cons_0, Snd_0)$ indicates dispatching to u, i.e. $cons = \{(u, \vec{v} \mapsto \vec{d})\}$,
- ullet there are no receptions by u in between, i.e.

$$cons_i \cap \{u\} \times Evs(\mathcal{E}, \mathcal{D}) = \emptyset, i > 1,$$

• $u_{n-1} = u$ and u is stable only in σ_0 and σ_n , i.e.

$$\sigma_0(u)(stable) = \sigma_n(u)(stable) = 1$$
 and $\sigma_i(u)(stable) = 0$ for $0 < i < n$,

Let $0=k_1< k_2<\cdots< k_N=n$ be the maximal sequence of indices such that $u_{k_i}=u$ for $1\le i\le N$. Then we call the sequence

$$(\sigma_0(u) =)$$
 $\sigma_{k_1}(u), \sigma_{k_2}(u), \dots, \sigma_{k_N}(u) = \sigma_{n-1}(u)$

a (!) run-to-completion computation of u (from (local) configuration $\sigma_0(u)$) $_{35/4}$

Putting It All Together

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Divergence

We say, object u can diverge on reception cons from (local) configuration $\sigma_0(u)$ if and only if there is an infinite, consecutive sequence

$$(\sigma_0, \varepsilon_0) \xrightarrow{(cons_0, Snd_0)} (\sigma_1, \varepsilon_1) \xrightarrow{(cons_1, Snd_1)} \dots$$

such that u doesn't become stable again

Note: disappearance of object not considered in the definitions.
 By the current definitions, it's neither divergence nor an RTC-step.

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The Missing Piece: Initial States

Recall: a labelled transition system is (S, \rightarrow, S_0) . We have

- S: system configurations (σ, ε)
- \rightarrow : labelled transition relation $(\sigma, \varepsilon) \xrightarrow{(cons, Snd)} (\sigma', \varepsilon')$.

Wanted: initial states S_0 .

Proposal:

Require a (finite) set of **object diagrams** \mathcal{OD} as part of a UML model

 $(\mathcal{C}\mathcal{D}, \mathcal{SM}, \mathcal{OD}).$

And se

$$S_0 = \{(\sigma, \varepsilon) \mid \sigma \in G^{-1}(\mathcal{OD}), \mathcal{OD} \in \mathscr{OD}, \varepsilon \text{ empty}\}.$$

Other Approach: (used by Rhapsody tool) multiplicity of classes. We can read that as an abbreviation for an object diagram.

Run-to-Completion Step: Discussion.

What people may dislike on our definition of RTC-step is that it takes a global and non-compositional view. That is:

- In the projection onto a single object we still see the effect of interaction with other objects.
- Adding classes (or even objects) may change the divergence behaviour of existing ones.
- Compositional would be: the behaviour of a set of objects is determined by the behaviour of each object "in isolation".

 Our semantics and notion of RTC-step doesn't have this (often desired) property.

Can we give (syntactical) criteria such that any global run-to-completion step

is an interleaving of local ones?

Maybe: Strict interfaces.

(Proof left as eversion)

- (A): Refer to private features only via "self".
- (Recall that other objects of the same class can modify private attributes.)
- . (B): Let objects only communicate by events, i.e.
- don't let them modify each other's local state via links at all.

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Semantics of UML Model — So Far

The semantics of the UML model

 $\mathcal{M} = (\mathscr{CD}, \mathscr{SM}, \mathscr{OD})$

where

- some classes in $\mathscr{C}\mathscr{D}$ are stereotyped as 'signal' (standard), some signals and attributes are stereotyped as 'external' (non-standard),
- there is a 1-to-1 relation between classes and state machines
- O𝒯 is a set of object diagrams over 𝒞𝒯,

is the transition system (S, \rightarrow, S_0) constructed on the previous slide.

The computations of \mathcal{M} are the computations of (S, \rightarrow, S_0) .

OCL Constraints and Behaviour

- Let $\mathcal{M} = (\mathscr{CD}, \mathscr{SM}, \mathscr{OD})$ be a UML model.
- We call M consistent iff, for each OCL constraint expr ∈ Inv(ℰՋ),
- $\sigma \models expr$ for each "reasonable point" (σ, ε) of computations of \mathcal{M} .
- (Cf. exercises and tutorial for discussion of "reasonable point".)

Note: we could define $\mathit{Inv}(\mathscr{SM})$ similar to $\mathit{Inv}(\mathscr{CD})$.

Pragmatics:

• In UML-as-blueprint mode, if \mathscr{SM} doesn't exist yet, then $\mathcal{M}=(\mathscr{C}\mathscr{D},\emptyset,\mathscr{O}\mathscr{D})$ is typically asking the developer to provide \mathscr{SM} such that $\mathcal{M}'=(\mathscr{C}\mathscr{D},\mathscr{M},\mathscr{O}\mathscr{D})$ is consistent.

If the developer makes a mistake, then \mathcal{M}^\prime is inconsistent.

Not common: if SM is given, then constraints are also considered when choosing transitions in the RTC-algorithm. In other words: even in presence of mistakes, the SM never move to inconsistent configurations.

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References

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References

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