

## Software Design, Modelling and Analysis in UML

### Lecture 14: Hierarchical State Machines II

2012-01-17

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- 14 - 2012-01-17 - main -

### Contents & Goals

#### Last Lecture:

- Putting It All Together: ODs define initial states
- Hierarchical State Machines: kind, region
- Initial pseudostate, final state

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#### Composite States

(formalisation follows [Damm et al., 2003])

#### This Lecture:

- Educational Objectives:** Capabilities for following tasks/questions.
  - What does this hierarchical State Machine mean? What **may happen** if I inject this event?
  - What is: AND-State, OR-State, pseudo-state, entry/exit/do, final state, ...

#### Content:

- Composite states
- Legal state configuration
- Lca, depth, ...
- Exit/Entry, internal transitions
- History and others

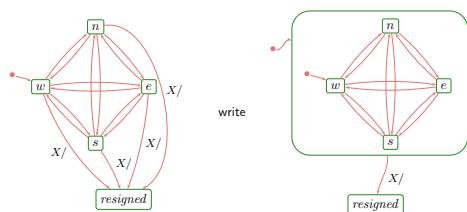
2/46

- 14 - 2012-01-17 - main -

3/46

### Composite States

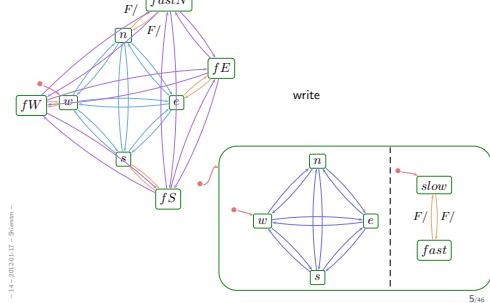
- In a sense, composite states are about **abbreviation, structuring, and avoiding redundancy**.
- Idea: in Tron, for the Player's Statemachine, instead of



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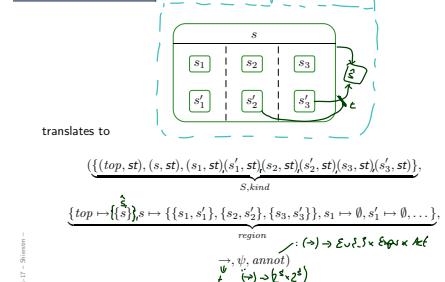
### Composite States

and instead of



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### Recall: Syntax



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6/46

4/46

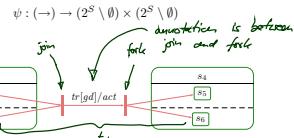
5/46

## Syntax: Fork/Join

SPECIAL CASE:  $(S) \xrightarrow{t_1 \text{ and } t_2} (S)$

maps to:  $t_1, t_2 \mapsto (S_1, S_2), S_1 \text{ to } S_2$

- For brevity, we always consider transitions with (possibly) multiple sources and targets, i.e.



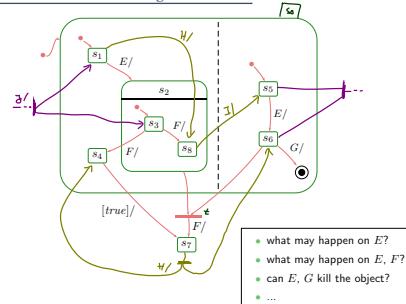
translates to

$$(S, kind, region, \underbrace{\{t_1\}}_{\psi}, \underbrace{\{t_1 \mapsto (\{s_2, s_3\}, \{s_5, s_6\})\}}_{\text{annot}}, \underbrace{\{t_1 \mapsto (tr, gd, act)\}}_{\text{annot}})$$

- Naming convention:  $\psi(t) = (\text{source}(t), \text{target}(t))$ .

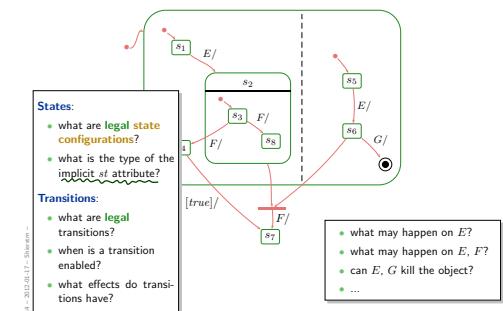
7/46

## Composite States: Blessing or Curse?



8/46

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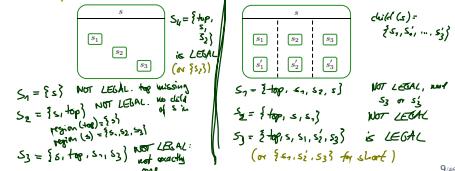
8/46

## States: st, (Legal) State Configurations

- The type of  $st$  is from now on a set of states, i.e.  $st : 2^S$
- A set  $S_1 \subseteq S$  is called **(legal) state configurations** if and only if
  - $\top \in S_1$ , and
  - for each state  $s \in S_1$  that has exactly one child, there is a non-empty region  $\emptyset \neq R \in \text{region}(s)$ , exactly one (non-pseudo-state) child of  $s$  is in  $S_1$ , i.e.  $\exists s' \in R \quad \{s\} \cap \text{kind}(s') \cap S_1 = 1$ .

$|\{s \in R \mid \text{kind}(s) \in \{st, fin\}\} \cap S_1| = 1$ .

### Examples:

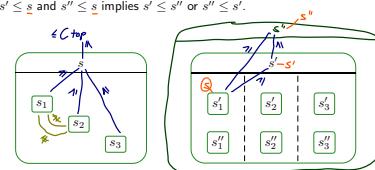


9/46

## Towards Transitions: A Partial Order on States

The substate- (or child-) relation induces a partial order on states:

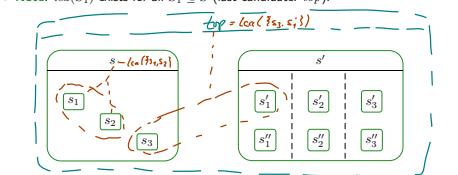
- $\top \leq s$ , for all  $s \in S$ ,
- $s \leq s'$ , for all  $s' \in \text{child}(s)$ ,
- transitive, reflexive, antisymmetric,
- $s' \leq s$  and  $s'' \leq s$  implies  $s' \leq s''$  or  $s'' \leq s'$ .



10/46

## Least Common Ancestor and Ting

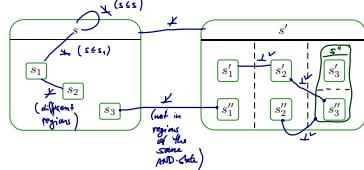
- ups, misleading name, better: closest, greatest, immediate
- The least common ancestor is the function  $lca : 2^S \rightarrow S$  such that
    - The states in  $S_1$  are (transitive) children of  $lca(S_1)$ , i.e.  $\forall s_1 \in S_1 \quad \forall s_2 \in S_1 \quad lca(S_1) \leq s_1 \wedge lca(S_1) \leq s_2 \Rightarrow lca(S_1) \leq s_1 \wedge s_2$
    - $lca(S_1)$  is minimal, i.e. if  $\hat{s} \leq s$  for all  $s \in S_1$ , then  $\hat{s} \leq lca(S_1)$
  - Note:  $lca(S_1)$  exists for all  $S_1 \subseteq S$  (last candidate:  $\top$ ).



11/46

## Least Common Ancestor and Ting

- Two states  $s_1, s_2 \in S$  are called **orthogonal**, denoted  $s_1 \perp s_2$ , if and only if
  - they are unordered, i.e.  $s_1 \not\leq s_2$  and  $s_2 \not\leq s_1$ , and
  - they live in different regions of an AND-state, i.e. $\exists s, \text{region}(s) = \{S_1, \dots, S_n\}, 1 \leq i \neq j \leq n : s_1 \in \text{child}(S_i) \wedge s_2 \in \text{child}(S_j)$ .



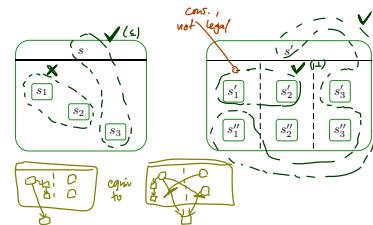
12/46

- 14 - 2012.01.17 - States.m4v -

## Least Common Ancestor and Ting

- A set of states  $S_1 \subseteq S$  is called **consistent**, denoted by  $\downarrow S_1$ , if and only if for each  $s, s' \in S_1$ ,
  - $s \leq s'$ , or
  - $s' \leq s$ , or
  - $s \perp s'$ .

CLAIM:  $\forall S_1 \subseteq S$  •  
 $S_1$  is layer state only  
 $\Rightarrow S_1$  is consistent



13/46

- 14 - 2012.01.17 - States.m4v -

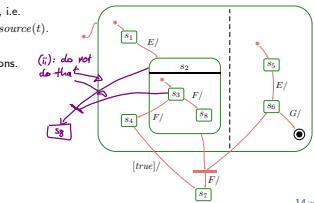
## Legal Transitions

- A hierarchical state-machine  $(S, \text{kind}, \text{region}, \rightarrow, \psi, \text{annot})$  is called **well-formed** if and only if for all transitions  $t \in \rightarrow$ ,
  - source and destination are consistent, i.e.  $\downarrow \text{source}(t)$  and  $\downarrow \text{target}(t)$ ,
  - source (and destination) states are pairwise **unordered**, i.e.
    - for all  $s, s' \in \text{source}(t)$  ( $\in \text{target}(t)$ ),  $s \perp s'$ ,

- the top state is neither source nor destination, i.e.
  - $\text{top} \notin \text{source}(t) \cup \text{source}(t)$ .
- Recall: final states are not sources of transitions.

Example:

CLAIM:  
 $(ii) \Rightarrow (i)$



14/46

- 14 - 2012.01.17 - States.m4v -

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- 14 - 2012.01.17 - States.m4v -

## References

45/46

46/46

- 14 - 2012.01.17 - main.m4v -