Software Design, Modelling and Analysis in UML

Lecture 17: Live Sequence Charts II

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Contents & Goals

Last Lecture:

- · Reflective vs. constructive description of behaviour
- · Live Sequence Charts: syntax, intuition

This Lecture:

- · Educational Objectives: Capabilities for following tasks/questions. • What does this LSC mean? Are this UML model's state machines consistent with the interactions?
- Please provide a UML model which is consistent with this LSC. What is: activation, hot/cold condition, pre-chart, etc.?

• Content:

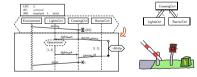
- Symbolic Büchi Automata (TBA) and its (accepted) language. LSC formal semantics.

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Recall: Live Sequence Charts Syntax

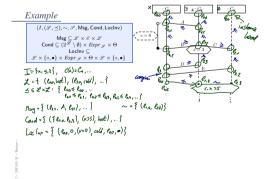
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Recall: Example



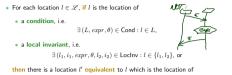
- Whenever the CrossingCtrl has consumed a 'secreg' event
- then it shall finally send 'lights_on' and 'barrier_down' to LightsCtrl and BarrierCtrl,
- if LightsCtrl is not 'operational' when receiving that event, the rest of this scenario doesn't apply; maybe there's another LSC for that case.
- if LightsCtrl is 'operational' when receiving that event, it shall reply with 'lights_ok' within 1–3 time units,
- the BarrierCtrl shall reply with 'barrier ok' within 1-5 time units, during this time (dispatch time not included) it shall not be in state 'MvUp',
- 'lights_ok' and 'barrier_ok' may occur in any order.
- After having consumed both, CrossingCtrl may reply with 'done' to the environment. 4/47

- Recall: LSC Body Abstract Syntax Let $\Theta = \{hot, cold\}$. An LSC body is a tuple $(I, (\mathscr{L}, \preceq), \sim, \mathscr{S}, \mathsf{Msg}, \mathsf{Cond}, \mathsf{LocInv})$ where • I is a finite set of instance lines, call asserved with a dass CEC (ℒ, ≤) is a finite, non-empty, partially ordered set of locations, each $\overline{l} \in \mathscr{L}$ is associated with a temperature $\theta(l) \in \Theta$ and an instance line $i_l \in I$, • $\sim \subseteq \mathscr{L} \times \mathscr{L}$ is an equivalence relation on locations, the simultaneity relation, 𝒴 = (𝒴,𝒴, 𝒱, 𝒱, atr, 𝑑) is a signature, • $\operatorname{Msg} \subseteq \mathscr{L} \times \mathscr{E}^{(\mathfrak{g})} \times \mathscr{L}$ is a set of asynchronous messages with $(l, b, l') \in \operatorname{Msg}$ only if $l \sim l'$, Not: instantaneous messages - could be linked to method/operation calls.
- Cond $\subseteq (2^{\mathcal{L}} \setminus \emptyset) \times Expr_{\mathcal{T}} \times \Theta$ is a set of conditions with $(L, expr, \theta) \in \text{Cond}$ only if $l \sim l'$ for all $l, l' \in L$, include the set of local invariants, LocInv $\subseteq \mathcal{L} \times \{\circ, \bullet\} \times Expr_{\mathcal{T}} \times \Theta \times \mathcal{L} \times \{\circ, \bullet\}$ is a set of local invariants,



Recall: Well-Formedness

Bondedness/no floating conditions: (could be relaxed a little if we wanted to)



a message, i.e.

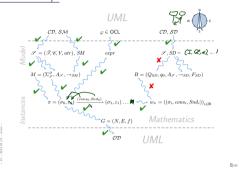
 $\exists \ (l_1,b,l_2) \in \mathsf{Msg}: l \in \{l_1,l_2\}, \text{ or}$ • an instance head, i.e. l' is minimal wrt. \preceq

Note: if messages in a chart are cyclic, then there doesn't exist a partial order (so such charts don't even have an abstract syntax).

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Course Map



Live Sequence Charts Semantics

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TBA-based Semantics of LSCs

Plan:

 $\bullet\,$ Given an LSC L with body

 $(I, (\mathscr{L}, \preceq), \sim, \mathscr{S}, \mathsf{Msg}, \mathsf{Cond}, \mathsf{LocInv})$

Construct a TBA B_L — taking the cuts of L as states.

 Define L(L) in terms of L(B_L), in particular taking activation condition and activation mode into account.

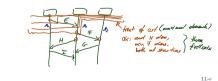
Formal LSC Semantics: It's in the Cuts

- Let $(I,(\mathscr{L},\preceq),\sim,\mathscr{S},\mathsf{Msg},\mathsf{Cond},\mathsf{LocInv})$ be an LSC body.
- A non-empty set

 $\label{eq:prod} \emptyset \neq C \subseteq \mathscr{L}$ is called a $\operatorname{\mathbf{cut}}$ of the LSC body if and only if

• it is downward closed, i.e. $\forall l, l' : l' \in C \land l \preceq l' \implies l \in C$,

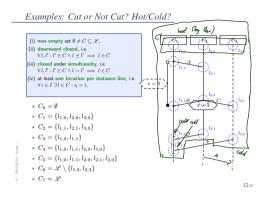
- it is closed under simultaneity, i.e. $\forall l, l' : l' \in C \land l \sim l' \implies l \in C$, and
- it comprises at least one location per instance line, i.e. ∀i ∈ I ∃l ∈ C : i_l = i.



Formal LSC Semantics: It's in the Cuts

- Let $(I, (\mathscr{L}, \preceq), \sim, \mathscr{S}, \mathsf{Msg}, \mathsf{Cond}, \mathsf{LocInv})$ be an LSC body.
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- it is closed under simultaneity, i.e. $\forall l, l' : l' \in C \land l \sim l' \implies l \in C$, and
- it comprises at least one location per instance line, i.e. ∀i ∈ I ∃l ∈ C : i_l = i.
- A cut C is called **hot**, denoted by $\theta(C) = \mathsf{hot}$, if and only if at least one of its <u>maximal elements</u> is hot, i.e. if
 - $\exists l \in C : \theta(l) = hot \land \nexists l' \in C : l \prec l'$

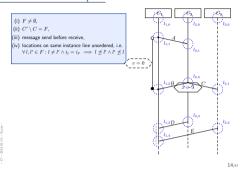
Otherwise, C is called **cold**, denoted by $\theta(C) = \text{cold}$.



A Successor Relation on Cuts

The partial order of (\mathscr{L}, \preceq) and the simultaneity relation "~" induce a direct successor relation on cuts of \mathscr{L} as follows: • Let $C, C' \subseteq \mathscr{L}$ bet cuts. C' is called direct successor of Cvia fired-set $F_{\mathbf{v}}$ denoted by $C \rightsquigarrow_F C'$, if and only if *F* ≠ ∅, 11 • $C' \setminus C = F$, • for each message reception in F, the corresponding sending is already in C. locations in F, that lie on the same instance line, are pairwise i.e. $\begin{aligned} & \epsilon \mathbf{I}, \text{ instance line of } \mathbf{I} \in \mathbf{I} \text{ instance line of } \mathbf{I} \\ & \forall l, l' \in F: l \neq l' \land i_l = i_{l'} \implies l \not \leq l' \land l' \not \leq l \end{aligned}$ unordered, i.e. • Note F is (magginately) closed under simultaneity. (~) • In other words: locations in F are direct \preceq -successors of locations in C, i.e. $\forall \, l' \in F \; \exists \, l \in C: l \prec l' \land \nexists \, l'' \in C: l' \prec l'' \prec l$ 13/47

Successor Cut Examples

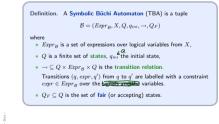


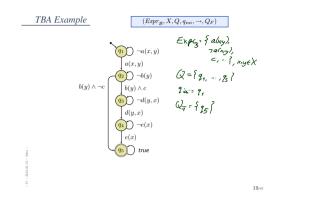
Idea: Accepting Words by Advancing the Cut

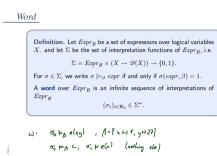
Let $w = (\sigma_i, cons_i, Snd_i)_{i \in \mathbb{N}_0}$ be a word over \mathscr{S} and \mathscr{D} .
Intuitively (and for now disregarding cold conditions),
an LSC body $(I, (\mathcal{L}, \prec), \sim, \mathcal{S}, Msg, Cond, LocInv)$ is supposed to accept w
(under variable)) if and only if there exists a sequence $\omega \times 1^{\circ}$.
which maps $C_0 \rightsquigarrow_{F_1} C_1 \rightsquigarrow_{F_2} C_2 \cdots \rightsquigarrow_{F_n} C_n$
(under valuation, 2) if and only if there exists a sequence u.b.C. methods: $C_0 \sim F_1 C_1 \sim F_2 C_2 \cdots \sim F_n C_n$ is the L that is the sequence of $C_1 \sim F_1 C_1 \sim F_2 C_2 \cdots \sim F_n C_n$ and indices $i_1 < \cdots < i_n$ such that $F_1 \sim F_2 C_2 \sim F_1 C_1 \sim F_2 C_2 \sim F_1 C_1$ $F_1 \sim F_1 C_1 \sim F_2 C_2 \sim F_1 C_1 \sim F_2 C_2 \sim F_1 C_1$
and indices $i_1 < \cdots < i_n$ such that
, - x:] hold
• C ₀ consists of the instance heads,
(• for all $1 \le j \le n$,
• for all $i_j \leq k \leq i_{j+1}$, $(\sigma_k, cons_k, Snd_k)$
satisfies (under β) the hold condition of C_{i-1} .
• $(\sigma_{i_j}, cons_{i_j}, Snd_{i_j})$ satisfies (under β)
the transition condition of F_j ,
• C_n is cold, $C_n = d$
• for all $i_n < k$, $(\beta_k, \mu_{i_1}, t_{i_2})$
satisfies (under β) the hold condition of C_n .
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Excursus: Symbolic Büchi Automata (over Signature)

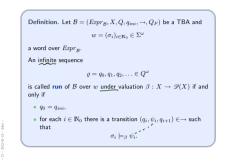
Symbolic Büchi Automata



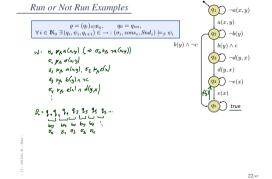




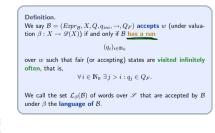
Run of TBA over Word

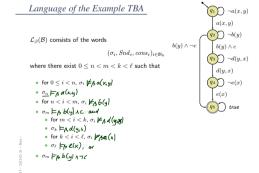


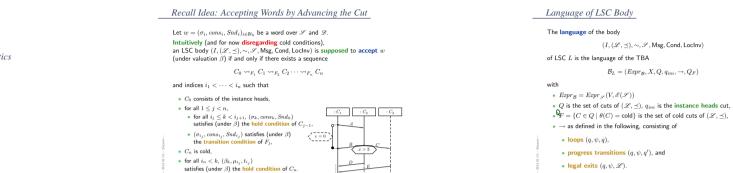
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The Language of a TBA

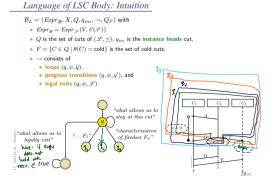






Back to Main Track: Live Sequence Charts Semantics





Signal and Integer Expressions

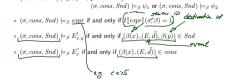
Let $\mathscr{S} = (\mathscr{T}, \mathscr{C}, V, atr)$ be a signature and X a set of logical variables. The signal and integer expressions $Expr_{\mathscr{S}}(V, \mathscr{E}(\mathscr{S}))$ over \mathscr{S} are defined by the grammar: $\psi ::= true \mid expr \mid (E_{x,y}^!) \mid (E_x^!) \neg \psi \mid \psi_1 \lor \psi_2,$

where $expr \in Expr_{\mathscr{S}}$, $E \in \mathscr{E}$, $x, y \in X$. constitues (x, E) send (x, E,y)

Satisfaction of Signal and Integer Expressions

Let $(\sigma, cons, Snd) \in \left(\Sigma^{\mathscr{D}}_{\mathscr{S}} \times 2^{\mathscr{D}(\mathscr{C}) \times Evs}(\mathscr{E}, \mathscr{D}) \times 2^{\mathscr{D}(\mathscr{C}) \times Evs}(\mathscr{E}, \mathscr{D}) \times \mathcal{S}^{(\mathscr{C})} \right)$ be a letter of a word over \mathscr{S} and \mathscr{D} and let $\beta : X \to \mathscr{D}(\mathscr{C})$ be a valuation of the logical variables in X.

- $(\sigma, cons, Snd) \models_{\beta} true$
- $\bullet \ (\sigma, \mathit{cons}, \mathit{Snd}) \models_{\beta} \neg \psi \text{ if and only if not } (\sigma, \mathit{cons}, \mathit{Snd}) \models_{\beta} \psi$
- (σ, cons, Snd) ⊨_β ψ₁ ∨ ψ₂ if and only if



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Satisfaction of Signal and Integer Expressions

Let $(\sigma, cons, Snd) \in (\Sigma^{\mathscr{D}}_{\mathscr{S}} \times 2^{\mathscr{G}(\mathbb{C}) \times Ews(\mathscr{E}, \mathscr{D})} \times 2^{\mathscr{G}(\mathbb{C}) \times Ews}(\mathscr{E}, \mathscr{D}) \times \mathscr{D}(\mathbb{C}))$ be a letter of a word over \mathscr{I} and \mathscr{D} and let $\beta : X \to \mathscr{D}(\mathscr{C})$ be a valuation of the logical variables in X.

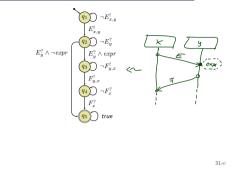
- $(\sigma, cons, Snd) \models_{\beta} true$
- $(\sigma, cons, Snd) \models_{\beta} \neg \psi$ if and only if not $(\sigma, cons, Snd) \models_{\beta} \psi$
- $\begin{array}{l} \ast \ (\sigma, \mathit{cons}, \mathit{Snd}) \models_{\beta} \psi_1 \lor \psi_2 \text{ if and only if} \\ (\sigma, \mathit{cons}, \mathit{Snd}) \models_{\beta} \psi_1 \text{ or } (\sigma, \mathit{cons}, \mathit{Snd}) \models_{\beta} \psi_2 \end{array}$
- $(\sigma, cons, Snd) \models_{\beta} expr$ if and only if $I[expr](\sigma, \beta) = 1$
- $(\sigma, cons, Snd) \models_{\beta} E_{x,y}^!$ if and only if $(\beta(x), (E, \vec{d}), \beta(y)) \in Snd$
- (σ, cons, Snd) ⊨_β E[?]_x if and only if (β(x), (E, d)) ∈ cons

Observation: if the semantics has "forgotten" the sender at consumption time, then we have to disregard it here (straightforwardly fixed if desired). Other view: we could choose to disregard the sender.

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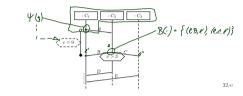






• Constraints relevant at cut q:

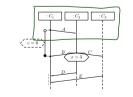
 $\psi(q) = \{\psi \mid \exists l \in q, l' \notin q \mid (l, \psi, \theta, l') \in \mathsf{LocInv} \lor (l', \psi, \theta, l) \in \mathsf{LocInv}\},\$



Some More Helper Functions

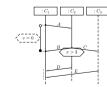
- Constraints relevant when moving from q to cut $q^\prime\colon$

$$\begin{split} \psi(q,q') &= \{\psi \mid \exists l \in q' \setminus q, l' \in \mathscr{L}, \theta \in \Theta \mid \\ (l, \bullet, expr, \theta, l') \in \operatorname{Loclm} \lor (l', expr, \theta, l, \bullet) \in \operatorname{Loclm} \rbrace \\ \cup \{\psi \mid \exists l \in q, l' \notin q', \theta \in \Theta \mid \\ (l, expr, \theta, l') \in \operatorname{Loclm} \lor (l', expr, \theta, l) \in \operatorname{Loclm} \rbrace \\ \cup \{\psi \mid \exists L \subseteq \mathscr{L}, \theta \in \Theta \mid (L, \psi, \theta) \in \operatorname{Cond} \land L \cap (q' \setminus q) \neq \emptyset \rbrace \end{split}$$



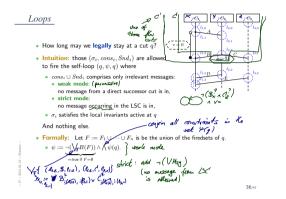
Even More Helper Functions

- + Cold constraints relevant when moving from q to cut $q^\prime :$
- $$\begin{split} \psi_{\mathsf{cold}}(q,q') &= \{\psi \mid \exists l \in q' \setminus q, l' \in \mathscr{L} \mid \\ &(l, \bullet, expr, \mathsf{cold}, l') \in \mathsf{LocInv} \lor (l', expr, \mathsf{cold}, l, \bullet) \in \mathsf{LocInv} \} \\ &\cup \{\psi \mid \exists l \in q, l' \notin q' \mid \\ &(l, expr, \mathsf{cold}, l') \in \mathsf{LocInv} \lor (l', expr, \mathsf{cold}, l) \in \mathsf{LocInv} \} \end{split}$$
 - $\cup \{ \psi \mid \exists L \subseteq \mathscr{L} \mid (L, \psi, \mathsf{cold}) \in \mathsf{Cond} \land L \cap (q' \setminus q) \neq \emptyset \}$



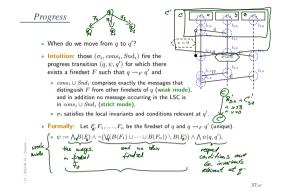
Recall: Intuition

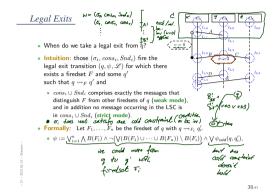
 $\mathcal{B}_L = (Expr_{\mathcal{B}}, X, Q, q_{ini}, \rightarrow, Q_F)$ with • $Expr_{\mathcal{B}} = Expr_{\mathscr{S}}(V, \mathscr{E}(\mathscr{S}))$ • Q is the set of cuts of $(\mathscr{L}, \preceq), \, q_{ini}$ is the instance heads cut, • $F = \{C \in Q \mid \theta(C) = \text{cold}\}$ is the set of cold cuts, $\bullet \ \rightarrow \ \text{consists of}$ loops (q, ψ, q), • progress transitions (q, ψ, q') , and G • legal exits (q, ψ, \mathcal{L}) . ć. not Breck : C₁ : C₂ "what allows us to Ċ. tay at this cut . Bard Vto B REW dres "what allows us to character0 G of firedset Fn" legally exit" 1 NCO true 🔿



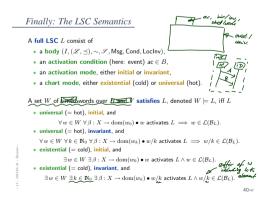
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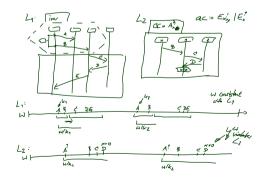
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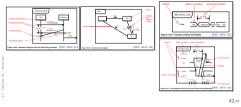






Back to UML: Interactions

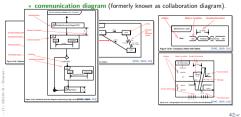
- In UML, reflective (temporal) descriptions are subsumed by interactions.
- A UML model $\mathcal{M} = (\mathscr{CD}, \mathscr{SM}, \mathscr{OD}, \mathscr{I})$ has a set of interactions \mathscr{I} .
- An interaction $\mathcal{I} \in \mathscr{I}$ can be (OMG claim: equivalently) diagrammed as
- sequence diagram, timing diagram, or
- communication diagram (formerly known as collaboration diagram).



Interactions as Reflective Description

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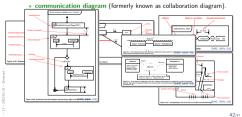




Interactions as Reflective Description

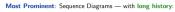
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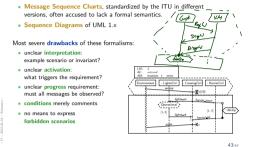
• sequence diagram, timing diagram, or





Why Sequence Diagrams?



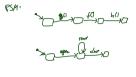


Thus: Live Sequence Charts

- SDs of UML 2.x address some issues, yet the standard exhibits unclarities and even contradictions [Harel and Maoz, 2007, Störrle, 2003]
- For the lecture, we consider Live Sequence Charts (LSCs) [Damm and Harel, 2001, Klose, 2003, Harel and Marelly, 2003], who
- have a common fragment with UML 2.x SDs [Harel and Maoz, 2007]
- Modelling guideline: stick to that fragment.

Side Note: Protocol Statemachines

Same direction: call orders on operations • "for each C instance, method f() shall only be called after g() but before h()" Can be formalised with protocol state machines.



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References

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References

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